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强化训练
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多6.9 f(a)=f(b)=0 祖 Yx6(a,b), を6(a,b)使f(z)=2+(x)(x-b)
          多 k= (x-0)(x-b) 关键
        Fit) = fiti - k(t-onit-b) 月由题 Fin=Fin=Fib=0
  罗尔定理 E,E(a,x) F(E)=D Exe(x,b) F(E)=D
                             836 (E1, E2) F(2) = 0
                                      P fit - 2k = 0
                             得到. 「(公) = 2 (六-0)(水-6) *
$ 6.17 1E(0, 1) 12 Sint > 1/005x
   \overline{F}(x) = \cos x \cdot (\cos x)^{-\frac{1}{3}} + \sin x \cdot (x + \frac{1}{3})(\cos x)^{-\frac{1}{3}} \cdot (x + \sin x) - 1
             = (\cos x)^{\frac{1}{3}} + \sin x \cdot (\frac{1}{3}) \cdot (\cos x)^{\frac{1}{3}} - 1
            = (\cos x)^{\frac{3}{5}} \left[ 1 + \frac{1}{5} \left( 1 - \cos x \right) \cdot \cos x \right] - 1
            =(\cos x)^{\frac{3}{5}}[1+\frac{1}{3}\cos^2 x-\frac{1}{3}]-1=\frac{1}{3}(\cos x)^{-\frac{1}{3}}+\frac{2}{3}(\cos x)^{\frac{1}{3}}-1
       F(7) = [- 4 ( cosx) - 3 + 4 ( cosx) - 3 ] (- sinx)
            = \frac{4}{9}(\cos x)^{-\frac{3}{2}}(-\sin x)(-\sin x)^{2} = \frac{4}{9}(\cos x)^{-\frac{3}{2}}\cdot(\sin x)^{3} > 0
         ··Fin>Fin>Fin>Fin>Fin>Fin>A
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6.18 B: ex+e-x > 2x2+2cosx -00<x<+00 今fix)= ex+ex-2x2-2cosx 偶函数 只需证 x20 fix=0 => fix)=e7-e-x-4x+2sinx $f(\omega) = f(\omega) = f(\omega)$ = $f(\omega) = f(\omega) = 0$ fix) = ex+ e-x-4+ 2005x fin = e7-e-x-2sinx $f_{(1)}^{(4)} = e^{x} + e^{-x} - 2\cos x > 0.$ $f(x) = f(x) + f(x) \cdot x + \frac{f(x)}{2} x^2 + \frac{f(x)}{3!} x^3 + \frac{f(x)}{4!} x^4 > 0$ · fun 20. 得祖 # \$6.19. fin = fib = 0 12: & & (a, b) | fix | 7 (b-a)2 | fib) - fia) 表勤. $f(x) = f(a) + \frac{f(a)}{2}(x-a) + \frac{f(a)}{2}(x-a)^2$ & \(\epsilon(a, x)\) $f(x) = f(b) + \frac{f(b)}{2}(x-b) + \frac{f(b)}{2}(x-b)^2$ & & & (b, x) D-0得 D=f(b)-f(a)+f(x2)(x-b)2-f(x)(x-a)2. (a+b) (file) - f(a) + (a+b) (file) = 0 $\frac{4|f(b)-f(a)|}{(b-a)^2} = \frac{1}{2}(f(a) - f(a)) \leq \frac{1}{2}||f(a)| + |f(a)|$ { | fc/2) | 3 max | fc/2) , fc/2) }

$$[2] \frac{4|f(b)-f(a)|}{(b-a)^2} \le \frac{1}{2} \cdot 2 \cdot |f(a)| = |f(a)|$$

\$ 6.1 f(a) = f(b) = 0. f(n) + cosf(n) = e f(n)

1. (C) 【解析】由题设知,f(x) 在[a,b]上连续,故必有最大值 M与最小值m,若 $\exists x_0 \in (a,b)$,使得 $f(x_0) > 0$,则 f(x) 的最大值 M > 0,记最大值点为 ξ ,则 $f(\xi) = M > 0$,且由费马定理有 $f'(\xi) = 0$. 代人题设方程,有 $f''(\xi) = e^{f(\xi)} - \cos f'(\xi) = e^{M} - 1 > 0$,则 $x = \xi$ 为极小值点,矛盾,故 $f(x) \leq 0$, $x \in (a,b)$.

同理,若 $\exists x_1 \in (a,b)$,使得 $f(x_1) < 0$,则 f(x) 的最小值 m < 0,记最小值点为 η ,则 $f(\eta) = m < 0$,且由费马定理有 $f'(\eta) = 0$. 代入题设方程,有 $f''(\eta) = e^{f(\eta)} - \cos f'(\eta) = e^m - 1 < 0$,则 $x = \eta$ 为极大值点,亦矛盾,故 $f(x) \ge 0$, $x \in (a,b)$.

综上所述, $f(x) \equiv 0, x \in [a,b]$.

\$6.3 f(a) = f(b) = 0 $\frac{2}{2} 2 [f(\epsilon_i)]^2 + f(\epsilon_i) f(\epsilon_i) = 0$ $(\epsilon_i = 1, 2)$

\$ 6.4 | $f(x) | \le 1$, $0 < |f(x)| \le 2$, $x \in [0, +\infty)$ $\frac{1}{12} : |f(x)| \le 2\sqrt{2}$.

\$ \f(x) | \in \f(x) + \f(x) + \f(x) \cdot \f(x) + \f(x) \cdot \f(

 $\leq \frac{1}{h} [|f(x+h)| + |f(h)|] + \frac{h}{2} |f(x)| \leq \frac{2}{h} + h$

当上江时 f的三江成之

於

 $\frac{8}{5} 67 \quad \overline{f}(x) = \int_{-1}^{1} |x-t| e^{-t^{2}} dt - \frac{1}{2} (e^{-1} + 1)$ $\overline{f}(x) = \int_{-1}^{x} e^{-t^{2}} dt - \int_{x}^{1} e^{-t^{2}} dt = \int_{-1}^{x} e^{-t^{2}} dt + \int_{-x}^{-1} e^{-u^{2}} du = \int_{-x}^{x} e^{-t^{2}} dt$ $\overline{f}(x) = e^{-x^{2}} + e^{-x^{2}} = 2e^{-x^{2}} > 0 \quad \text{fin} \quad \overline{f}(x) = 0$ $= 2 \int_{0}^{x} e^{-t^{2}} dt$ $= 2 \int_{0}^{x} e^{-t^{2}} dt$

$$F(-1) = \int_{-1}^{1} \frac{de^{-t^{2}}}{de^{-t^{2}}} dt - \frac{1}{2}(e^{-t}+1) \qquad -e^{-t^{2}}$$

$$= 0 + 2\int_{0}^{1} e^{-t^{2}} dt - \frac{1}{2}(e^{-t}+1) > 2\int_{0}^{1} e^{-t^{2}} dt - \frac{1}{2}(e^{-t}+1) = \frac{1}{2} - \frac{1}{2}e^{-t} > 0$$

$$F(0) = \int_{-1}^{1} |t| e^{-t^{2}} dt - \frac{1}{2}(e^{-t}+1) = 2\int_{0}^{1} t e^{-t^{2}} dt - \frac{1}{2}(e^{-t}+1)$$

$$= -e^{-t} + |-\frac{1}{2}e^{-t}| - \frac{1}{2} = -\frac{3}{2}e^{-t} + \frac{1}{2} < 0$$

$$F(1) = \int_{0}^{1} e^{-t^{2}} dt - \int_{0}^{1} t e^{-t^{2}} dt - \frac{1}{2}(e^{-t}+1)$$

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$$= 2\int_{0}^{1} e^{-t^{2}} dt - \int_{0}^{1} t e^{-t^{2}} dt -$$

 $\frac{3}{4} = \frac{3}{4} = \frac{3$

即的北震点

호 (μπ)= fin + [fin)2. 자기 (ca.) ≤ 2 Y(2n) ≤ 2.
: Y(x)=4. 渡を財取(を1、を2)と(-2,2)上的 Y(x)max. 円均有 Y(x) > 4 耳 Y(x)=0	
由于 fix1=1 Yce724 : fix	
得過.	