

Review and Extension — Divisibility and Congruences

Andres Buritica Monroy

1 Key concepts for this term

- Induction, strong induction, well-ordering
- If $a \mid b$ and $a \mid c$ then for any integers x and y , $a \mid bx + cy$
- Division algorithm, Euclid's algorithm, Bezout's identity
- Fundamental Theorem of Arithmetic
- GCD, LCM in terms of prime factorisations
- Factorise expressions
- Take out the GCD
- Basic properties of \mathbb{Z}_p : operations, inverses, Wilson, Fermat, GCD trick
- Multiplicative and completely multiplicative functions
- Formulas for d , σ and φ
- Prove a problem for prime powers first
- Basic properties of \mathbb{Z}_n : operations, inverses, Euler, GCD trick, Chinese Remainder Theorem, generalised Wilson
- How to choose a mod
- Modular contradictions
- Quadratic discriminant is a perfect square

2 Homework

Solve and submit any three problems from the Problems sections of this term's handouts that weren't covered in class.

Also complete the feedback form: <https://forms.gle/fR78jMzBeHKWy7nM7>