

Name	Gitanjali Gangurde
UID	2021300034
Class	SE-Comps A Batch-B
Experiment No.	3
AIM:	Use divide and conquer strategy: Strassen's matrix multiplication.
THEORY:	<p>Divide and Conquer method to multiply two square matrices:</p> <ol style="list-style-type: none"> 1. Divide matrices A and B in 4 sub-matrices of size $N/2 \times N/2$ as shown in the below diagram. 2. Calculate following values recursively. $ae + bg$, $af + bh$, $ce + dg$ and $cf + dh$. $ \begin{bmatrix} a & b \\ c & d \end{bmatrix} \times \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} ae + bg & af + bh \\ ce + dg & cf + dh \end{bmatrix} $ <p style="text-align: center;"> A B C </p> <p> A, B and C are square matrices of size $N \times N$ a, b, c and d are submatrices of A, of size $N/2 \times N/2$ e, f, g and h are submatrices of B, of size $N/2 \times N/2$ </p>

CODE:

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#include <stdio.h>
#include <time.h>
int main()
{ int i,j; int a[2][2], b[2][2], c[2][2]; int
  s[10], p[8]; clock_t start, end; printf("Enter
  the elements of first matrix:"); for(int
  i=0;i<2;i++)
  { for (int j = 0; j <2; j++)
    { scanf("%d",&a[i][j]);
    }
  }
```

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    }

    printf("Enter the elements of second matrix:");
    for(int i=0;i<2;i++)
    { for (int j = 0; j <2; j++)
        { scanf("%d",&b[i][j]);
          } }

    s[0]=b[0][1]-b[1][1]; s[1]=a[0][0]+a[0][1];
    s[2]=a[1][0]+a[1][1]; s[3]=b[1][0]-b[0][0];
    s[4]=a[0][0]+a[1][1]; s[5]=b[0][0]+b[1][1];
    s[6]=a[0][1]-a[1][1]; s[7]=b[1][0]+b[1][1];
    s[8]=a[0][0]-a[1][0]; s[9]=b[0][0]+b[0][1];

    for(int i=0;i<10;i++)
    { printf("S%d: %d", (i+1), s[i]);
      printf("\n");
    }

    p[0]=s[0]*a[0][0];
    p[1]=s[1]*b[1][1];
    p[2]=s[2]*b[0][0];
    p[3]=s[3]*a[1][1];
    p[4]=s[4]*s[5]; p[5]=s[6]*s[7];
    p[6]=s[8]*s[9];

    printf("\n"); for(i=0;i<7;i++)
    { printf("P%d:
    %d", (i+1), p[i]);
    printf("\n");
    }

```

```
c[0][0]=p[4]+p[3]-p[1]+p[5];
c[0][1]=p[0]+p[1];
c[1][0]=p[2]+p[3];
c[1][1]=p[4]+p[0]-p[2]-p[6];

printf("\nMatrix A =");
for(i=0;i<2;i++)
{
printf("\n");
for(j=0;j<2;j++)
{
printf("%d\t",a[i][j]);
}
}
printf("\n\nMatrix B =");
for(i=0;i<2;i++)
{
printf("\n");

for(j=0;j<2;j++)
{
printf("%d\t",b[i][j]);
}
}
printf("\n\nMatrix C =");
for(i=0;i<2;i++)
{
printf("\n");
for(j=0;j<2;j++)
{
printf("%d\t",c[i][j]);
}
}
printf("\n");
end=clock();
double diff=(double)((end-start)/CLOCKS_PER_SEC);
return 0;
}
```

OUTPUT:

Enter the elements of first matrix:1

2

3

4

Enter the elements of second matrix:5

6

7

8

S1: -2

S2: 3

S3: 7

S4: 2

S5: 5

S6: 13

S7: -2

S8: 15

S9: -2

S10: 11

P1: -2

P2: 24

P3: 35

P4: 8

P5: 65

P6: -30

P7: -22

Matrix A =

1 2

3 4

Matrix B =

5 6

7 8

Matrix C =

19 22

43 50

CONCLUSION:	<ol style="list-style-type: none"> 1. Time complexity of normal matrix multiplication is given as : $T(N) = 8T(N/2) + O(N^2)$ 2. From Master's Theorem, time complexity of above method is $O(N^3)$ 3. Normal matrix multiplication method has 8 recursive calls, the idea of Strassen's method is to reduce the number of recursive calls to 7. 4. Time Complexity of Strassen's Method : $T(N) = 7T(N/2) + O(N^2)$ 5. From Master's Theorem, time complexity of above method is $O(N \log 7)$ which is approximately $O(N^{2.8074})$.
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