Exercise 1b

Exercise 1b

Deadline: 27.11.2020, 16:00

In this exercise, you will implement the k-nearest-neighbor classifier and estimate its accuracy on unseen test data and via cross-validation. Moreover, you learn how to speed-up Python code using "vectorization".

Regulations

Provide your comments for last week's homework in the files

- monte-carlo-commented.ipynb and monte-carlo-commented.html for feedback to your solution,
- monte-carlo-cross-commented.ipynb and monte-carlo-cross-commented.html for crossfeedback.

Solutions for this week's tasks shall be handed in as nearest-neighbor.ipynb and exported to nearest-neighbor.html. Zip all files into a single archive with naming convention (sorted alphabetically by last names):

lastname1-firstname1_lastname2-firstname2_ex01b.zip

or (if you work in a team of three)

lastname1-firstname1_lastname2-firstname2_lastname3-firstname3_ex01b.zip and upload this file to Moodle before the given deadline.

1 Comment on your solution to Exercise 1a

Study the sample solution monte-carlo-solution.html provided on Moodle and use it to comment on your own solution to this exercise. Specifically, copy your original notebook monte-carlo.ipynb to monte-carlo-commented.ipynb and insert comments as markdown cells starting with

```
<span style="color:green;font-weight:bold">Comment</span>
```

so that we can clearly distinguish your comments from the other cell types. Insert comment cells at the appropriate places according to the following rules:

- If your code is incorrect, identify the bugs and make brief suggestions for possible fixes (don't include a full corrected solution).
- If your solution is slow, identify inefficient code sections (e.g. Python loops) and suggest possible improvements.
- If your code is correct, but differs from the sample solution, briefly explain why your solution is a valid alternative and where either solution is more elegant.
- If your code is essentially equal to the sample solution, explicitly say so.

Export the commented notebook to monte-carlo-commented.html and hand in both files.

Note: If you fail to hand in monte-carlo-commented.html, we will deduct 50% of the points from your solution to exercise 1.

2 Comment on others' solution to Exercise 1a

You will, via email, receive the solution handed in by another group. Please give feedback to their solution according to the same criteria as above. Remember that throughout the semester you will have to give meaningful cross-feedback at least four times in order to be accepted to the final project.

3 Nearest Neighbor Classification on Real Data

3.1 Exploring the Data (3 points)

Scikit-learn (usually abbreviated sklearn) provides a collection of standard datasets that are suitable for testing a classification algorithm (see http://scikit-learn.org/stable/datasets/ for a list of the available datasets and usage instructions). In this exercise, we want to recognize handwritten digits, which is a typical machine learning application. The dataset digits consists of 1797 small images with one digit per image.

Load the dataset from sklearn and extract the data:

Note that data is a flattened (1-dimensional) version of images. What is the size of these images (the numpy attribute shape might come in handy)? Visualize one image of a 3 using the imshow function from matplotlib.pyplot:

```
import numpy as np
import matplotlib.pyplot as plt

img = ...

assert 2 == len(img.shape)

plt.figure()
plt.gray()
plt.imshow(img, interpolation="nearest") # also try interpolation="bicubic"
plt.show()
```

Moreover, sklearn provides a convenient function to separate the data into a training and a test set.

3.2 Distance function computation using loops (3 points)

A naive implementation of the nearest neighbor classifier uses loops to determine the required minimum distances. Implement this approach in a python function dist_loop(training, test), which computes the Euclidean distance between all instances in the training and test set (in the feature space). The input should be the $N \times D$ and $M \times D$ training and test matrices with D pixels per image and N respectively M instances in the training and test set. The output should be a $N \times M$ distance matrix. For the calculation of the Euclidean distance you might want to use numpy.square(), numpy.sum() and numpy.sqrt() or numpy.linalg.norm().

3.3 Distance function computation using vectorization (8 points)

Since loops are rather slow in python, and we will need efficient code later in the semester, write a second python function dist_vec(training, test) for computing the distance function which relies on vectorization and does not use for loops. Consult https://www.safaribooksonline.com/library/view/python-for-data/9781449323592/ch04.html and https://softwareengineering.stackexchange.com/questions/254475/how-do-i-move-away-from-the-for-loop-school-of-thought for information on how to do this. Verify that the new function returns the same distances as the loop-based version. Now compare the run times of the two implementations using jupyter's %timeit command (the vectorized version should be significantly faster).

Note: It is absolutely critical that you understand vectorization, because the code for subsequent homeworks will otherwise be too slow for meaningful experimentation. We will therefore grade this task very strictly.

3.4 Implement the k-nearest neighbor classifier (6 points)

Revise your code from the previous homework to implement a k-nearest neighbor classifier. It should work for arbitrary k (number of neighbors to include in the majority vote), N (training set size) and D (number of features). Use your classifier to distinguish the digit $\bf 3$ from the digit $\bf 9$. To do so, filter out these digits from the training and test sets and use your function from subproblems $\bf 3.2$ or $\bf 3.3$ to compute distances. Vary the value for k (try the values $\bf 1, \, 3, \, 5, \, 9, \, 17$ and $\bf 33$) and compute the error rates. Describe the dependency of the classification performance on k.

4 Cross-validation (8 points)

In subproblem 3.4, we measured the performance of the nearest neighbor classifier on a predefined test set. To be able to do this, we had to put aside test data and thus reduced the size of the training set. This may lead to increased error because some relevant training instances might not end up in the training set. Another way to estimate whether the trained classifier is able to generalize to unseen data is cross-validation (see https://en.wikipedia.org/wiki/Cross-validation_(statistics)).

Write a function

X_folds, y_folds = split_folds(data, target, L)

to randomly split the given data and labels into L folds (parts of roughly equal size). The numpy-functions numpy.random.permutation() and numpy.array_split() may be useful here. In each subsequent cross-validation iteration, you use one of the L subparts as test set and the remaining ones as corresponding training set.

Use the same splits to evaluate your implementation from subtask 3.4 and the pre-defined solution in sklearn.neighbors.KNeighborsClassifier(). The latter is trained with the fit() function and classifies new data via the predict() function (see http://scikit-learn.org/stable/modules/generated/sklearn.neighbors.KNeighborsClassifier.html for more details).

Return the mean error rate as well as its standard deviation over the L repetitions. Cross-validate your k-nearest neighbor classifier with k=1 and a suitable bigger k, as well as its sklearn counterparts, on the full digits dataset for $L \in \{2,5,10\}$. Compare the algorithms' performance. How do the results depend on L?