# **Linear Regression & Neural Network**

2017.10.21

최건호



01

#### Linear Regression

- 정의
- Loss
- Gradient Descent
- 문제점

02

#### **Neural Network**

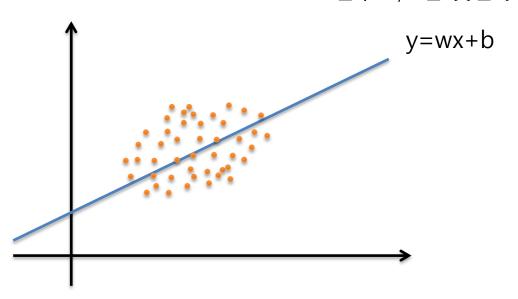
- 정의
- Deep?
- 활용

03

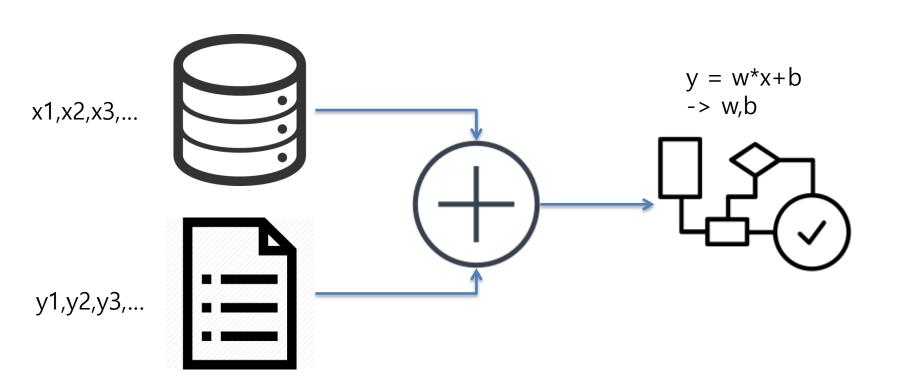
#### Propagation

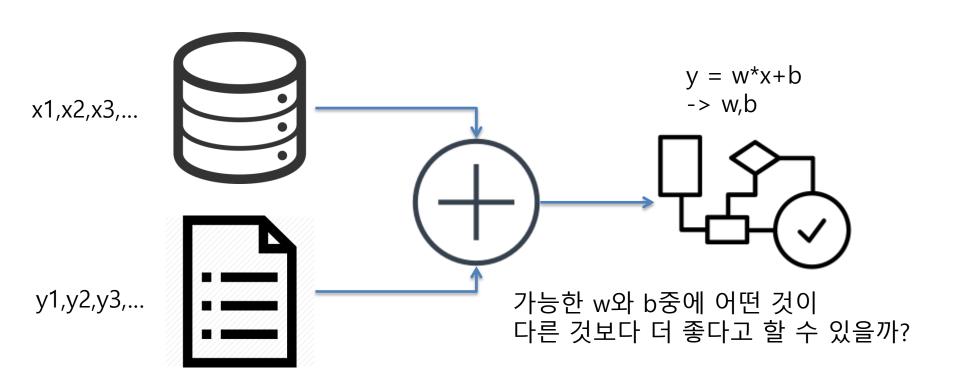
- 정의
- Forward Prop.
- Back Prop.

x에 대한 y값을 가장 잘 설명하는 변수 w, b를 찾는 것



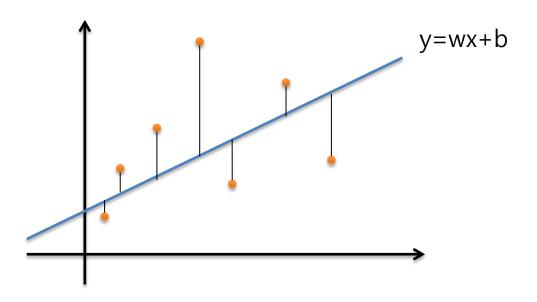
종속 변수 y와 한 개 이상의 독립 변수 X와의 선형 상관 관계를 모델링하는 회귀분석 기법





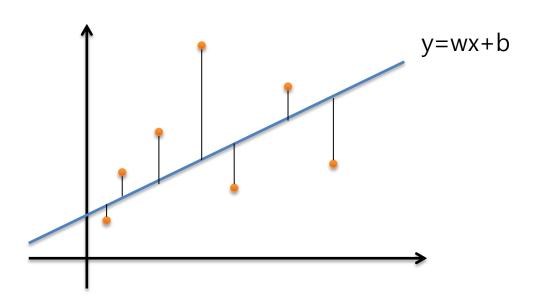
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Mean Squared Error(MSE)  $MSE = \frac{(x1-x2)^2}{n}$  두 값의 거리의 제곱의 평균

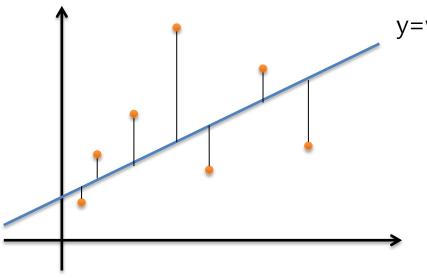


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Mean Squared Error(MSE)

$$MSE = \frac{(x1 - x2)^2}{n}$$

두 값의 거리의 제곱의 평균



y=wx+b

임의의 w\*,b\*를 초기값으로 한다면

Loss = 
$$\frac{(y^* - y)^2}{n} = \frac{(w^*x + b^* - y)^2}{n}$$

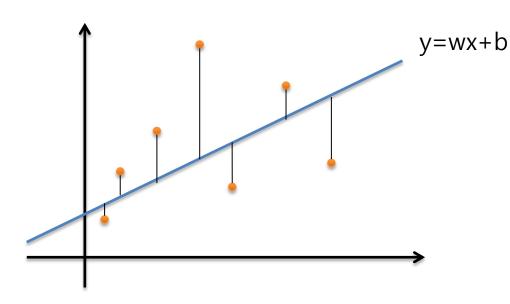
loss값은 고정된 x, y(데이터)에서 w\*,b\* 에 의해 구해짐

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$$MSE = \frac{(x1 - x2)^2}{n}$$

두 값의 거리의 제곱의 평균



예시) y = 0.5\*x+4 이고 w\*=2, b\*=2 일 때, x=3에서 loss는?

$$Loss = \frac{(8-5.5)^2}{n} = \frac{(2.5)^2}{n}$$

Loss를 minimize하는 w,b를 구하고 싶다.

-> Random Search?

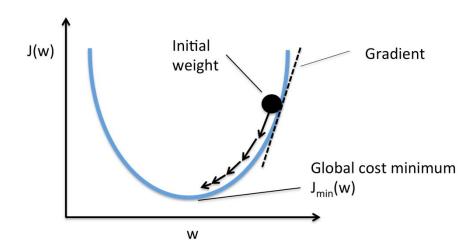
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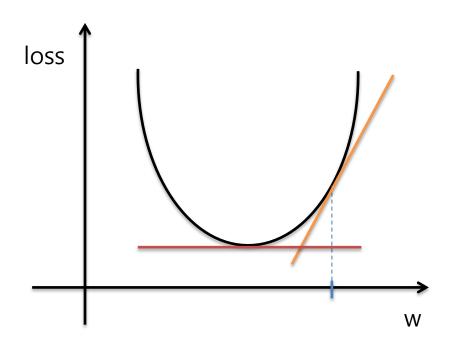
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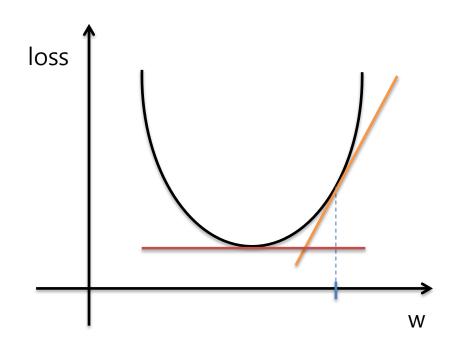
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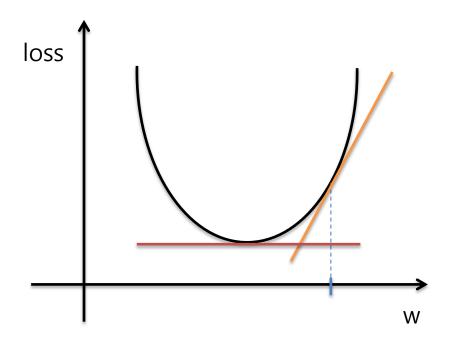


그냥 바로 loss를 w에 대해 미분 했을 때 그 값이 0이 되는 w를 찾으면 안될까?

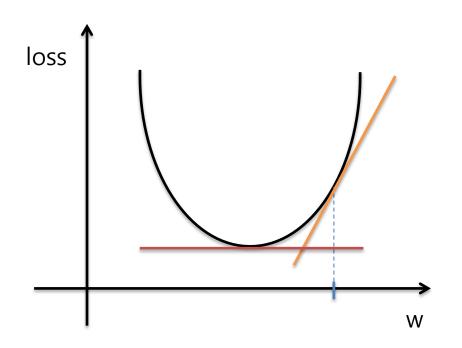


그냥 바로 loss를 w에 대해 미분 했을 때 그 값이 0이 되는 w를 찾으면 안될까?

loss를 minimize하는 w를 구하려면  $w = (x^T x)^{-1} x^T y$  식을 풀어야하는데, 변수가 많아지고 matrix가 커지면 복잡도가  $O(n^3)$  이기때문에 exponential 하게 증가한다. 변수가 많아질수록 계산이 거의 불가능.

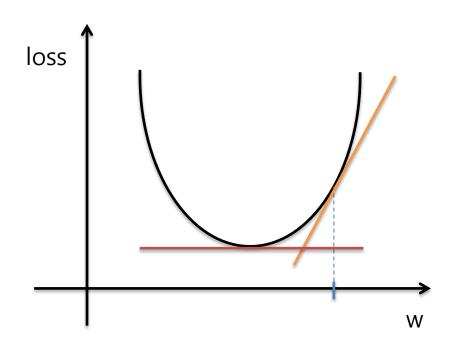


바로 minimum이 되는 지점을 구하기보다, 현재 loss에 대한 w의 gradient(경사도)를 구하여 gradient x learning rate만큼 w를 업데이트



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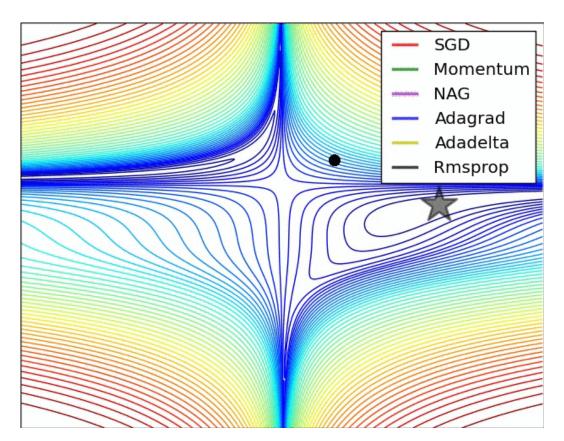
 $w_{t+1} = w_t - gradient * learning_rate$ 



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 $w_{t+1} = w_t - \frac{\text{gradient}}{\text{gradient}} * \text{learning\_rate}$ 

계속 업데이트 하다 보면 optimal 한 w에 근접하게 된다.



```
test.py
   import numpy as np
   import torch
   import torch.nn as nn
  import torch.optim as optim
   import torch.nn.init as init
   from torch.autograd import Variable
   from visdom import Visdom
   viz = Visdom()
10
   num data = 1000
    num epoch = 1000
14
   noise = init.normal(torch.FloatTensor(num data,1),std=0.2)
    x = init.uniform(torch.Tensor(num_data,1),-10,10)
   y = 2*x+3
  y_noise = y + noise
```

```
test.py
                                  import numpy as np
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```
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    model = nn.Linear(1,1)
21
    loss_func = nn.L1Loss()
    optimizer = optim.SGD(model.parameters(), tr=0.01)
24
25
    # train
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    loss arr =[]
    label = Variable(y_noise)
28
    for i in range(num_epoch):
        optimizer.zero grad()
29
        output = model(Variable(x))
30
31
32
        loss = loss func(output,label)
33
        loss.backward()
        optimizer.step()
34
        if i % 10 == 0:
35
36
            print(loss)
        loss arr.append(loss.data.numpy()[0])
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38
    param_list = list(model.parameters())
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training 이후 파라미터 값 확인

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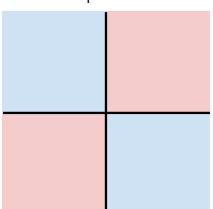
#### Hard cases for a linear classifier

#### Class 1:

number of pixels > 0 odd

#### Class 2:

number of pixels > 0 even

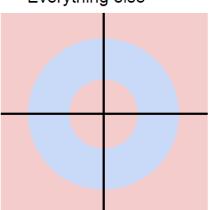


#### Class 1:

1 <= L2 norm <= 2

#### Class 2:

Everything else

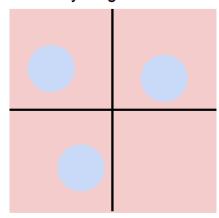


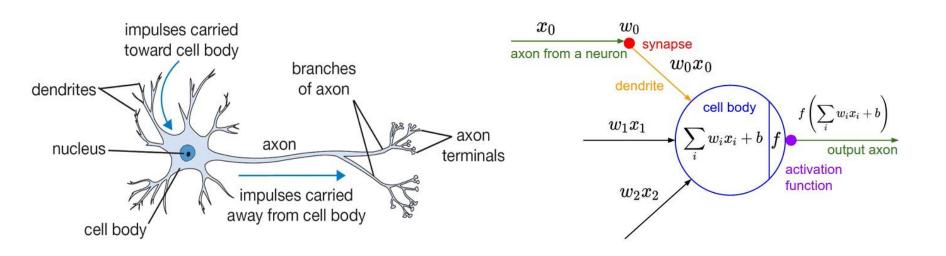
#### Class 1:

Three modes

#### Class 2

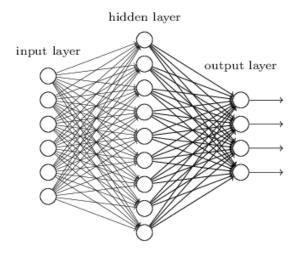
Everything else





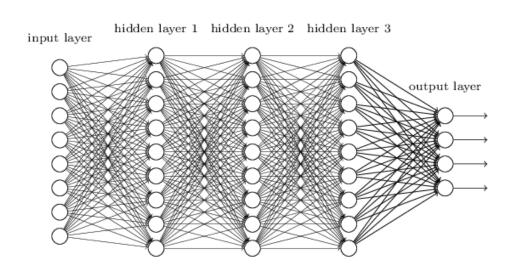
여러 자극이 들어오고 일정 기준을 넘으면 이를 다른 뉴런에 전달하는 구조

#### "Non-deep" feedforward neural network

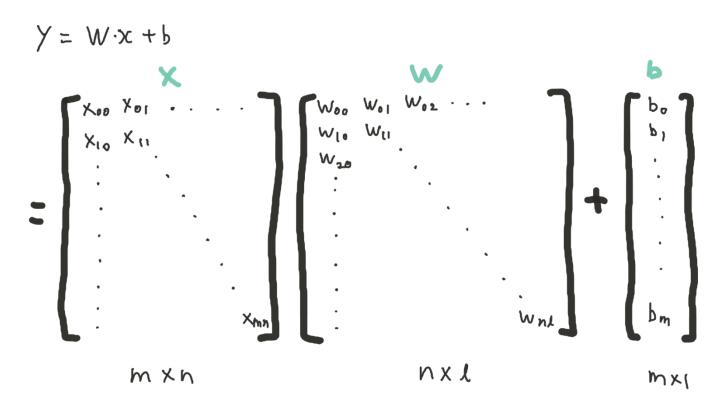


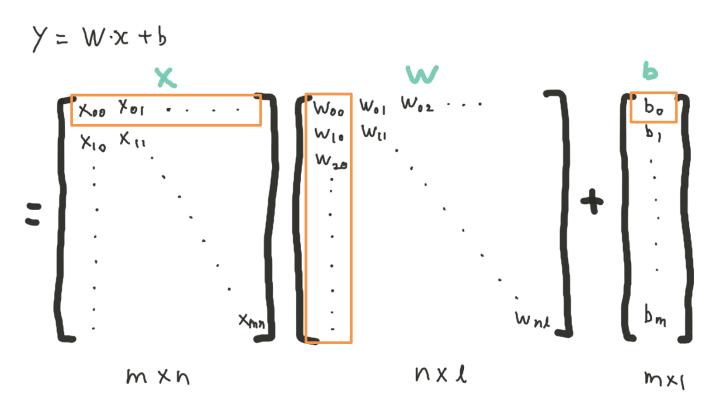
$$y = w2(act(w1 * input + b1)) + b2$$

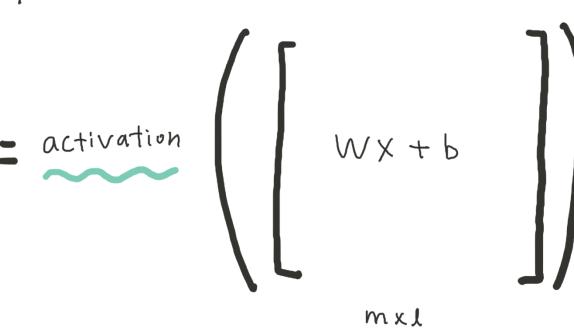
#### Deep neural network



$$y = w4(act(w3(act(w2(act(w1*input + b1)) + b2)) + b3)) + b4$$







만약 activation function이 없다면 아래의 식은 결국 linear function.

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activation function으로 non-linearity를 추가해야 함

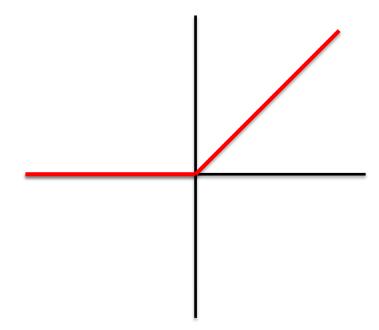
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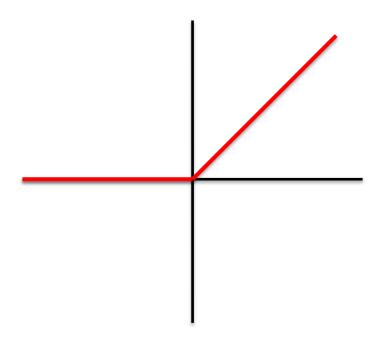
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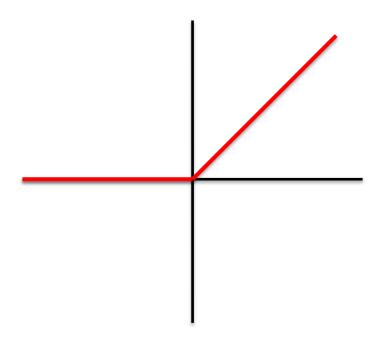
그렇다면 어떤 activation function을 써야 할까?

Activation function	Equation	Example	1D Graph			
Unit step (Heaviside)	$\phi(z) = \begin{cases} 0, & z < 0, \\ 0.5, & z = 0, \\ 1, & z > 0, \end{cases}$	Perceptron variant				
Sign (Signum)	$\phi(z) = \begin{cases} -1, & z < 0, \\ 0, & z = 0, \\ 1, & z > 0, \end{cases}$	Perceptron variant				
Linear	$\phi(z) = z$	Adaline, linear regression	-			
Piece-wise linear	$\phi(z) = \begin{cases} 1, & z \ge \frac{1}{2}, \\ z + \frac{1}{2}, & -\frac{1}{2} < z < \frac{1}{2}, \\ 0, & z \le -\frac{1}{2}, \end{cases}$	Support vector machine				
Logistic (sigmoid)	$\phi(z) = \frac{1}{1 + e^{-z}}$	Logistic regression, Multi-layer NN				
Hyperbolic tangent	$\phi(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$	Multi-layer NN				



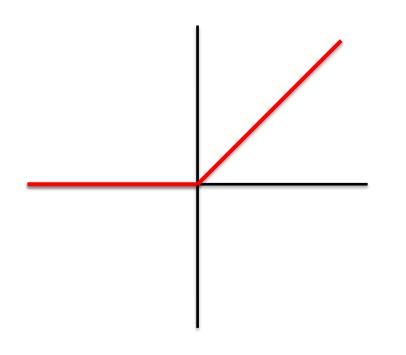


Rectified Linear Unit (ReLU)



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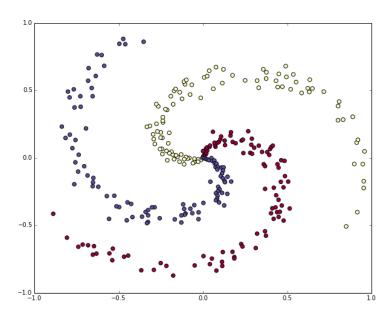
$$f(x) = max(0,x)$$

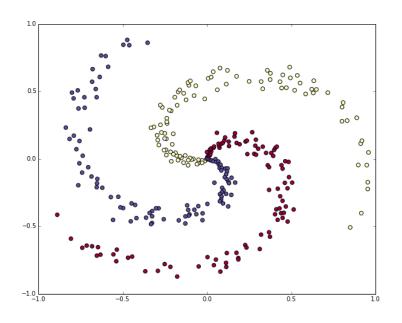


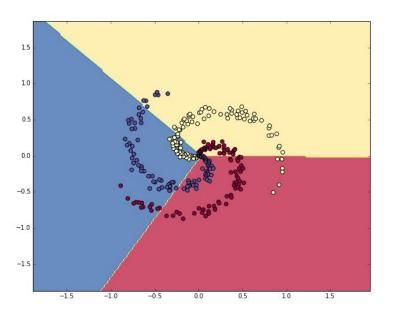
Rectified Linear Unit (ReLU)

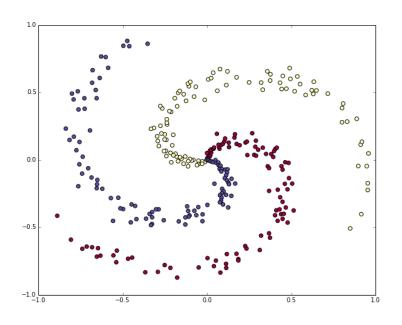
 $f(x) = \max(0,x)$ 

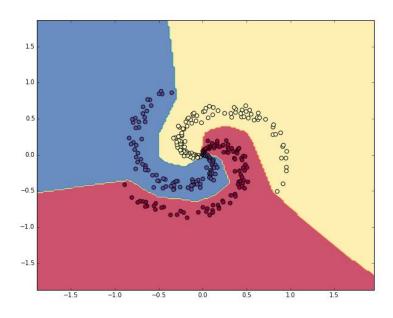
기존의 sigmoid와 tanh로는 학습이 잘 안됐었는데 relu는 gradient의 전달이 좋아서 default로 사용되고 있음

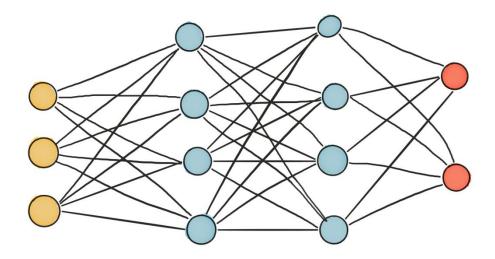


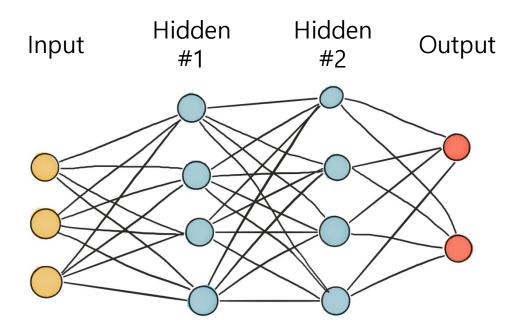


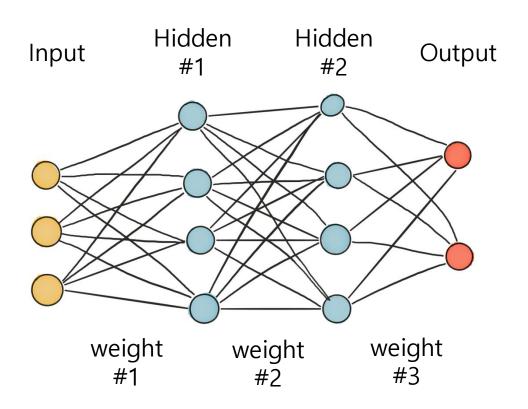


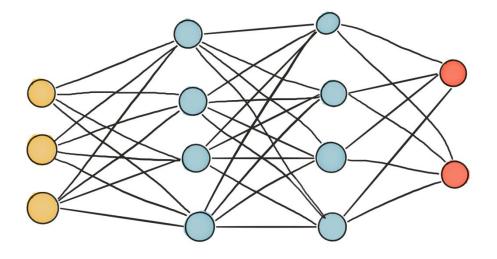


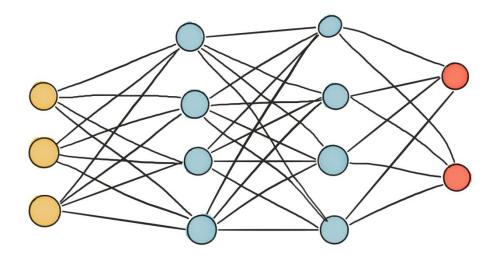




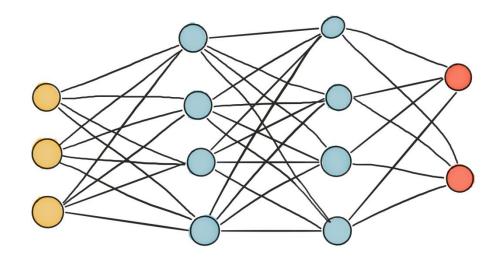






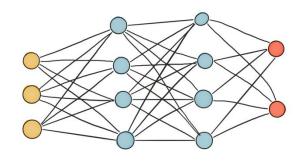


$\begin{bmatrix} w_{oo} \\ w_{10} \end{bmatrix}$	$W_{01}$	$W_{02}$ $W_{12}$	$\begin{bmatrix} w_{03} \\ w_{13} \end{bmatrix}$	V	$\begin{bmatrix} w_{oo} \\ w_{10} \end{bmatrix}$	$w_{01}$	$w_{02} = w_{12}$	$\begin{bmatrix} w_{03} \\ w_{13} \end{bmatrix}$		$\begin{bmatrix} w_{00} \\ w_{10} \\ w_{20} \end{bmatrix}$	$\begin{bmatrix} w_{01} \\ w_{11} \end{bmatrix}$	
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	3>	<b>&lt;</b> 4				4)	x4			4>	κ2	

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

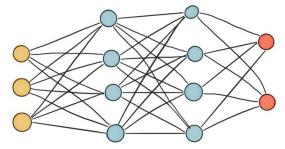


쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$



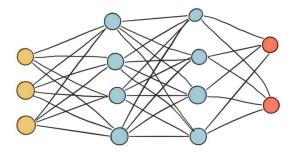
쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$

$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$



쉽게 이해되도록 loss = 예측값-실제로 설정

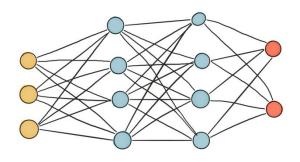
$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$

$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$

$$\frac{\partial loss}{\partial b3} = 1$$



쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

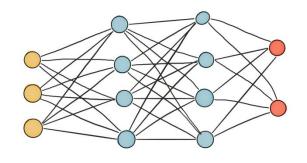
$$loss = y^* - y$$

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$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$

$$\frac{\partial loss}{\partial b3} = 1$$

$$\frac{\partial loss}{\partial w2} = ??$$



쉽게 이해되도록 loss = 예측값-실제로 설정

$$y^* = w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3$$

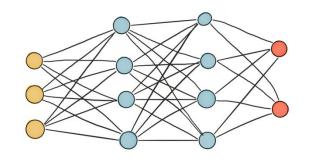
$$loss = y^* - y$$

$$= w3 * sig(w2 * sig(w1 * x + b1) + b2) + b3 - y$$

$$\frac{\partial loss}{\partial w3} = sig(w2 * sig(w1 * x + b1) + b2)$$

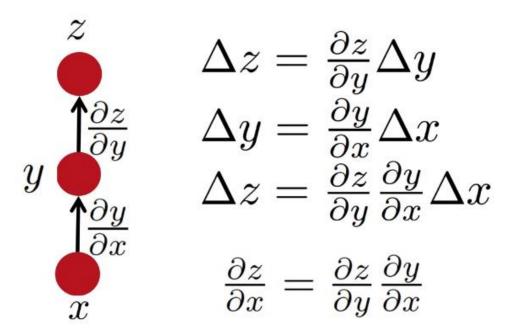
$$\frac{\partial loss}{\partial b3} = 1$$

$$\frac{\partial loss}{\partial w2} = chain rule!!$$



쉽게 이해되도록 loss = 예측값-실제로 설정

#### Simple Chain Rule

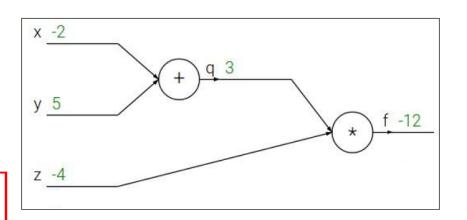


Backpropagation: a simple example

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y \qquad rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

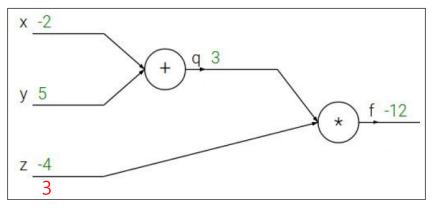


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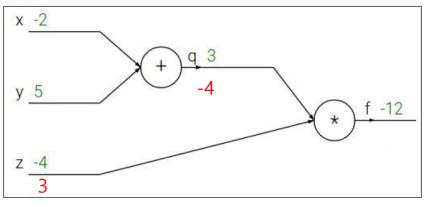
$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

Backpropagation: a simple example

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y \qquad rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

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$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$
$$\frac{\partial f}{\partial q} = z = -4$$

Backpropagation: a simple example

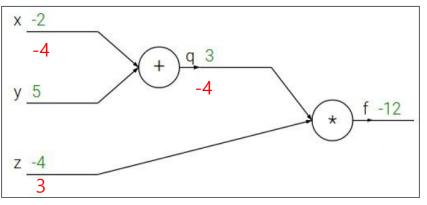
$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

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$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want:

$$\frac{\partial f}{\partial x}$$
,  $\frac{\partial f}{\partial y}$ ,  $\frac{\partial f}{\partial z}$ 



$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

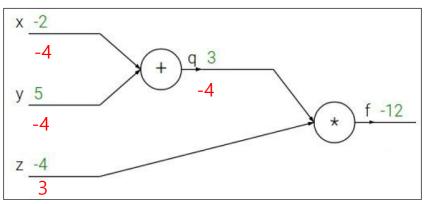
$$\frac{\partial f}{\partial q} = z = -4 \qquad \frac{\partial f}{\partial x} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial x} = -4 * 1 = -4$$

Backpropagation: a simple example

$$f(x, y, z) = (x + y)z$$
  
e.g.  $x = -2$ ,  $y = 5$ ,  $z = -4$ 

$$q=x+y \qquad rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

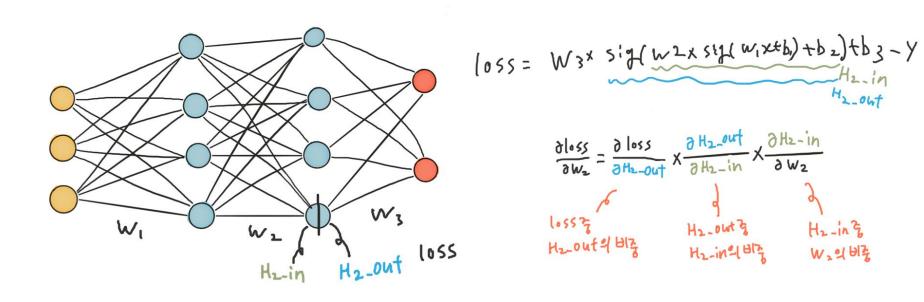
$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

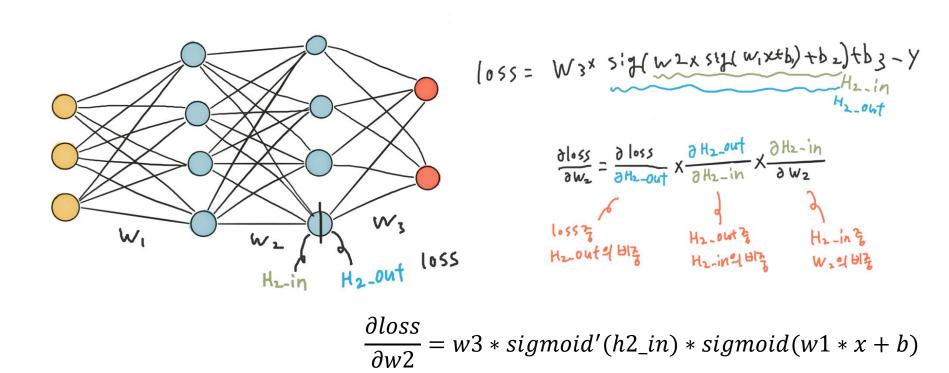


$$\frac{\partial f}{\partial z} = q = x + y = -2 + 5 = 3$$

$$\frac{\partial f}{\partial q} = z = -4 \qquad \frac{\partial f}{\partial x} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial x} = -4 * 1 = -4$$

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial y} = -4 * 1 = -4$$





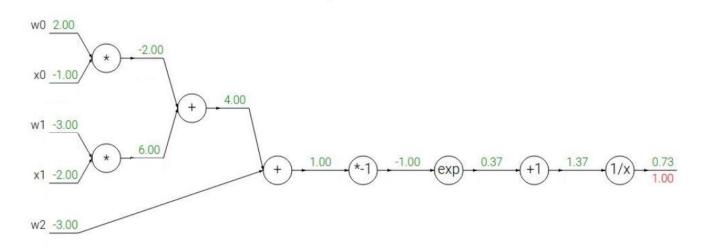
(참고) sigmoid 함수의 미분

$$\sigma(x)' = \frac{\delta\{1 + e^{-x}\}^{-1}}{\delta x} = -(1 + e^{-x})^{-2} - e^{-x} = \frac{e^{-x}}{(1 + e^{-x})^2}$$

$$\sigma(x)(1 - \sigma(x)) = \frac{1}{1 + e^{-x}}(1 - \frac{1}{1 + e^{-x}}) = \frac{1}{1 + e^{-x}}(\frac{e^{-x}}{1 + e^{-x}}) = \frac{e^{-x}}{(1 + e^{-x})^2}$$

Another example: 
$$f(w,x) = f(w,x)$$

$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$

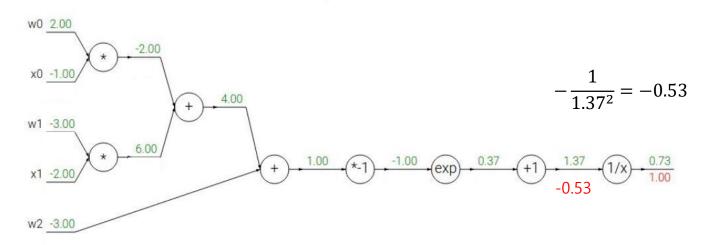


$$egin{aligned} f(x) = e^x & 
ightarrow & rac{df}{dx} = e^x \ & & \ f_a(x) = ax & 
ightarrow & rac{df}{dx} = a \end{aligned}$$

$$f(x)=rac{1}{x} \qquad \qquad 
ightarrow \qquad rac{df}{dx}=-1/x \ f_c(x)=c+x \qquad \qquad 
ightarrow \qquad rac{df}{dx}=1$$

Another example:  $f(w,x) = \frac{1}{1}$ 

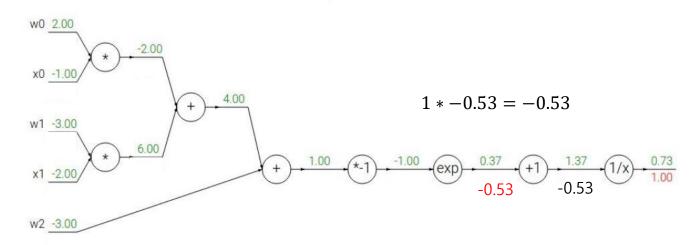
$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$egin{aligned} f(x) = e^x & 
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ightarrow & rac{df}{dx} = a \end{aligned}$$

$$egin{aligned} rac{df}{dx} = e^x & f(x) = rac{1}{x} & 
ightarrow & rac{df}{dx} = -1/x \ rac{df}{dx} = a & f_c(x) = c + x & 
ightarrow & rac{df}{dx} = 1 \end{aligned}$$

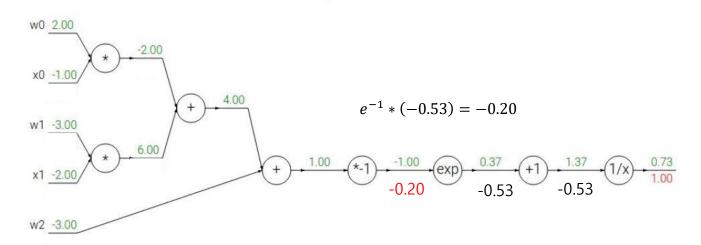
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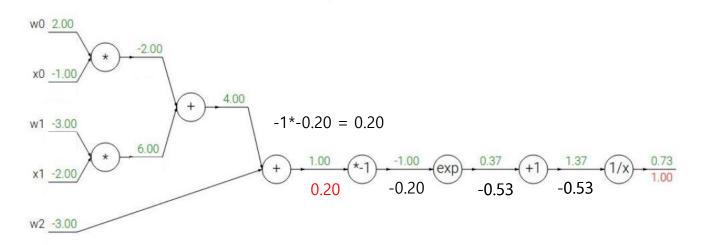
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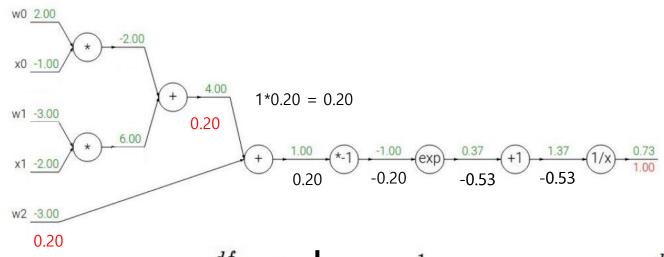
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ightarrow \qquad rac{df}{dx}=1$$

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$

$$\frac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

$$f(x) = \frac{1}{2}$$

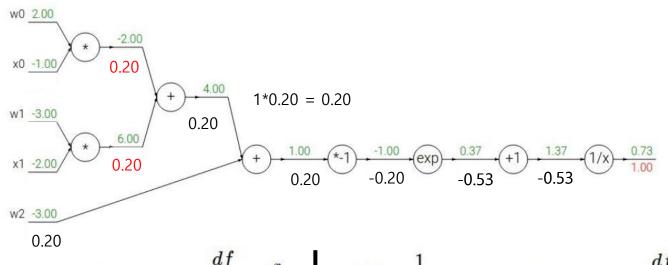
$$f(x) = c \perp x$$

$$\rightarrow$$

$$\frac{df}{dx}$$

$$\frac{df}{dx} = 1$$

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$
  $ightharpoonup$ 

$$rac{df}{dx} = e^x$$

$$\frac{df}{dx} = a$$

$$f(x) = \frac{1}{2}$$

$$f_c(x) = c + x$$

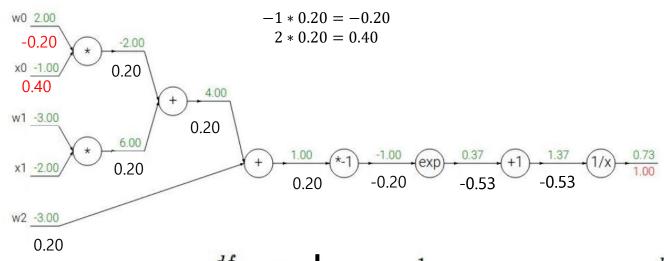
$$\rightarrow$$

$$\rightarrow$$

$$\frac{df}{dx} = -1/x$$

$$\frac{df}{dr} = 1$$

$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$
  $o$ 

$$\frac{df}{dx} = e^x$$

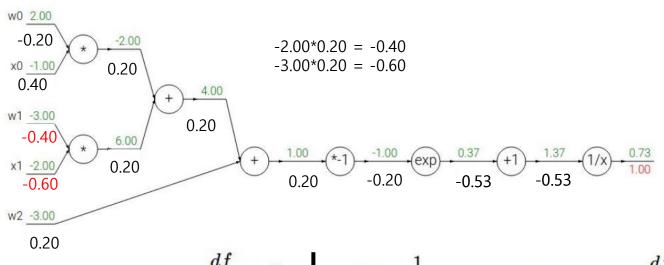
$$rac{df}{dx}=a$$

$$f(x) = \frac{1}{2}$$

$$f_c(x) = c + x$$

$$\frac{df}{dx} =$$

$$f(w,x) = rac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x) = e^x$$
  $\rightarrow$ 

$$f_a(x) = ax$$

$$\frac{df}{dx} = e^x$$

$$rac{df}{dx} = a$$

$$f(x) = \frac{1}{x}$$

$$f_c(x) = c + s$$

$$\frac{df}{dx} =$$

$$y = \frac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}} = \left[1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}\right]^{-1}$$

$$w_0 = 2$$

$$w_1 = -3$$

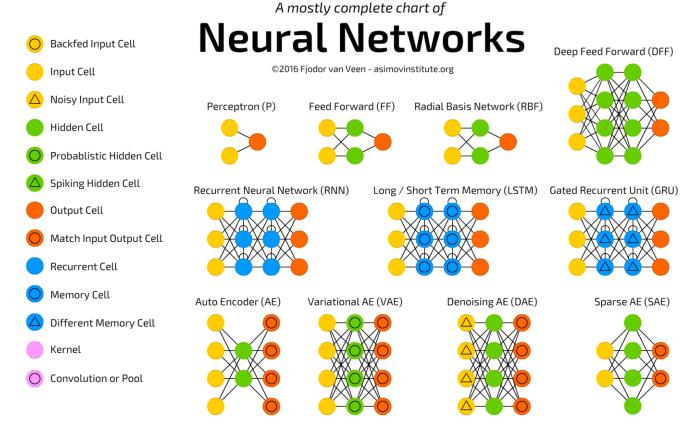
$$w_2 = -3$$

$$x_0 = -1$$

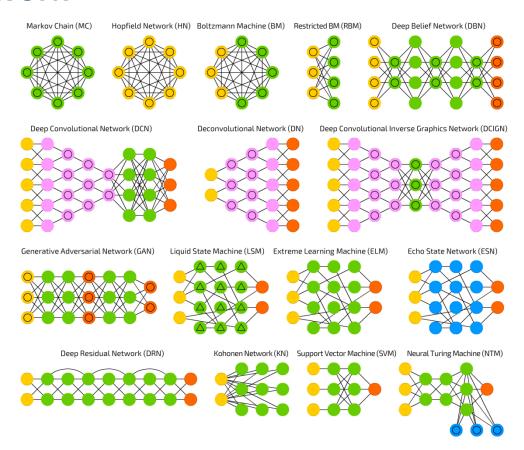
$$x_1 = -2$$

$$\frac{1}{2} = \frac{1}{2} = \frac{1}$$

#### **Neural Network**



#### **Neural Network**



```
test.py
    import numpy as np
 2 import torch
 3 import torch.nn as nn
 4 import torch.optim as optim
 5 import torch.nn.init as init
 6 from torch.autograd import Variable
 7 from visdom import Visdom
   viz = Visdom()
10
    num data = 1000
11
    num epoch = 5000
12
    x = init.uniform(torch.Tensor(num data,1),-15,15)
    y = 8*(x**2) + 7*x + 3
15
    noise = init.normal(torch.FloatTensor(num data,1),std=1)
    y_noise = y + noise
```

```
필요한 라이브러리
```

```
test.py
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필요한 라이브러리
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   데이터 생성
                             14
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                             16
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```

```
model = nn.Sequential(
22
            nn.Linear(1,10),
            nn.ReLU(),
23
            nn.Linear(10,6),
            nn.ReLU(),
            nn.Linear(6,1),
26
        ).cuda()
    loss_func = nn.L1Loss()
    optimizer = optim.SGD(model.parameters(), tr=0.001)
31
    loss arr =[]
    label = Variable(y_noise.cuda())
    for i in range(num_epoch):
        output = model(Variable(x.cuda()))
        optimizer.zero_grad()
38
        loss = loss_func(output,label)
39
        loss.backward()
        optimizer.step()
        if i % 100 ==0:
            print(loss)
        loss_arr.append(loss.cpu().data.numpy()[0])
44
    param_list = list(model.parameters())
    print(param_list)
```

Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

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Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

- <training 단계>
- 1. 모델로 결과값 추정
- 2. loss 및 gradient 계산
- 3. 모델 업데이트

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Neural Network 모델 생성

loss function 및 gradient descent optimizer 생성

- <training 단계>
- 1. 모델로 결과값 추정
- 2. loss 및 gradient 계산
- 3. 모델 업데이트

training 이후 파라미터 값 확인

```
model = nn.Sequential(
        nn.Linear(1,10),
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        nn.Linear(10,6),
        nn.ReLU(),
        nn.Linear(6,1),
    ).cuda()
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optimizer = optim.SGD(model.parameters(), Lr=0.001)
loss arr =[]
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for i in range(num_epoch):
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    optimizer.zero_grad()
    loss = loss func(output,label)
    loss.backward()
    optimizer.step()
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        print(loss)
    loss_arr.append(loss.cpu().data.numpy()[0])
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```

# Q&A