Problem Set #4

Quiz, 5 questions

Congratulations! You passed!

Next Item



points

How many different minimum cuts are there in a tree with n nodes (ie.

n-1 edges)?



Each edge defines a distinct minimum cut (with one crossing

- n
- $2^{n}-2$

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Problem Set #29ints

Quiz, 5 questions

2.

Let "output" denote the cut output by Karger's min cut algorithm on a given connected graph with n vertices, and let $p=\frac{1}{\binom{n}{2}}$. Which of the

following statements are true?

For hints on this question, you might want to watch the short optional video on "Counting Minimum Cuts".

There exists a graph G with n nodes and a min cut (A, B) of G such that

$$Pr[out = (A, B)] \leq p.$$



Take G to be an n-cycle. How many different minimum cuts does it have?

For every graph G with n nodes and every min cut (A, B),

$$Pr[out = (A, B)] \le p.$$

This should not be selected

Recall the first problem of this problem set.

For every graph G with n nodes, there exists a min cut (A,B) such that

$$Pr[out = (A, B)] \le p.$$

This should not be selected

Recall the first problem of this problem set.

For every graph G with n nodes, there exists a min cut (A,B) of G such that

$$Pr[out = (A, B)] \ge p.$$



1/1 points

Quiz, 5 questions

3.

Let $.5 < \alpha < 1$ be some constant. Suppose you are looking for the median element in an array using RANDOMIZED SELECT (as explained in lectures). What is the probability that after the first iteration the size of the subarray in which the element you are looking for lies is $\le \alpha$ times the size of the original array?

- $\alpha \frac{1}{2}$
- $1-\alpha$
- $1-\frac{\alpha}{2}$
- 2*α 1

Correct

Precisely, as the pivot selected should lie between $1-\alpha$ and α times the original array.

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1/1 points

Quiz, 5 questions

4.

Let $0<\alpha<1$ be a constant, independent of n. Consider an execution of RSelect in which you always manage to throw out at least a $1-\alpha$ fraction of the remaining elements before you recurse. What is the maximum number of recursive calls you'll make before terminating?

$$-\frac{\log(n)}{\log(\frac{1}{2}+\alpha)}$$

$$-\frac{\log(n)}{\log(\alpha)}$$

Correct

Equivalently, log base 1/alpha of n.

$$-\frac{\log(n)}{\log(1-\alpha)}$$

$$-\frac{\log(n)}{\alpha}$$

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1/1 points

Quiz, 5 questions

5.

The minimum s-t cut problem is the following. The input is an undirected graph, and two distinct vertices of the graph are labelled "s" and "t". The goal is to compute the minimum cut (i.e., fewest number of crossing edges) that satisfies the property that s and t are on different sides of the cut.

Suppose someone gives you a subroutine for this s-t minimum cut problem via an API. Your job is to solve the original minimum cut problem (the one discussed in the lectures), when all you can do is invoke the given min s-t cut subroutine. (That is, the goal is to reduce the min cut problem to the min s-t cut problem.)

Now suppose you are given an instance of the minimum cut problem -- that is, you are given an undirected graph (with no specially labelled vertices) and need to compute the minimum cut. What is the minimum number of times that you need to call the given min s-t cut subroutine to guarantee that you'll find a min cut of the given graph?



$$n-1$$

Correct

Call an arbitrary vertex s, let t range over all other n-1 vertices, and return the best of the s-t min cuts founds.

2"

 \bigcirc n

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