$$\begin{split} &\sin^3\theta\cos^2\theta \\ &= \left(\frac{e^{i\theta} - e^{-i\theta}}{2i}\right)^3 \left(\frac{e^{i\theta} + e^{-i\theta}}{2}\right)^2 \\ &= -\frac{e^{5ix}}{32i} + \frac{e^{3ix}}{32i} + \frac{e^{ix}}{16i} \\ &+ \frac{e^{-5ix}}{32i} - \frac{e^{-3ix}}{32i} - \frac{e^{-ix}}{16i} \\ &= \frac{1}{16} \left(2\sin\theta + \sin 3\theta - \sin 5\theta\right). \end{split}$$