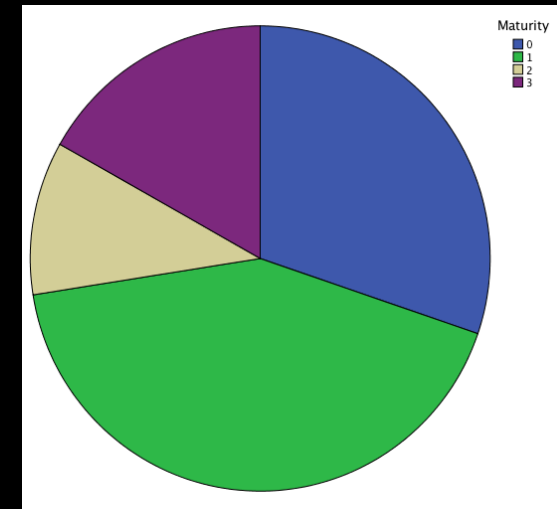
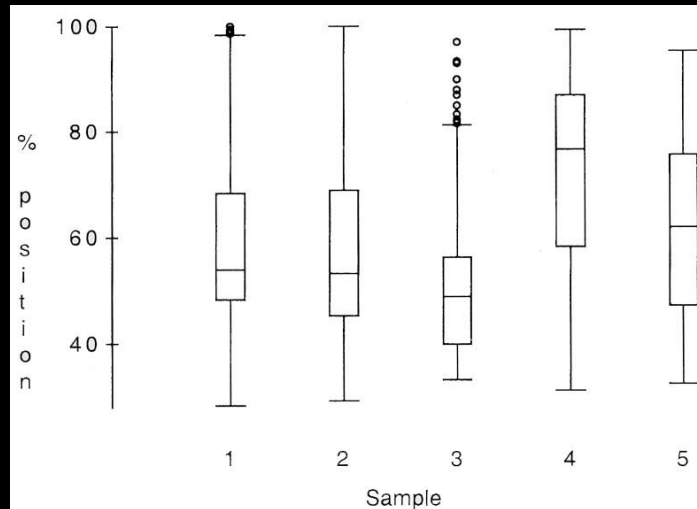
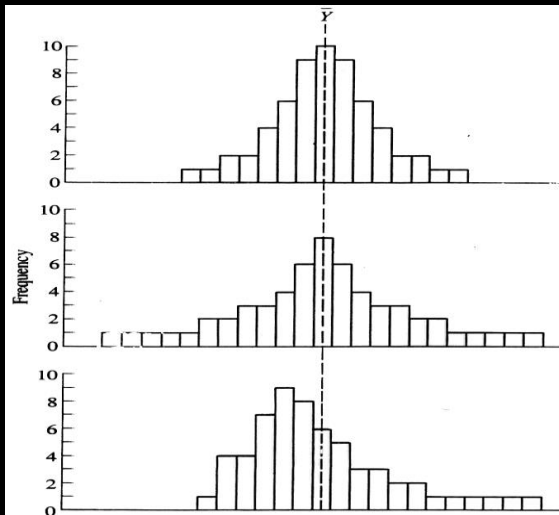


Data Handling :

A practical approach



Lecture 7 Chi-Square Test

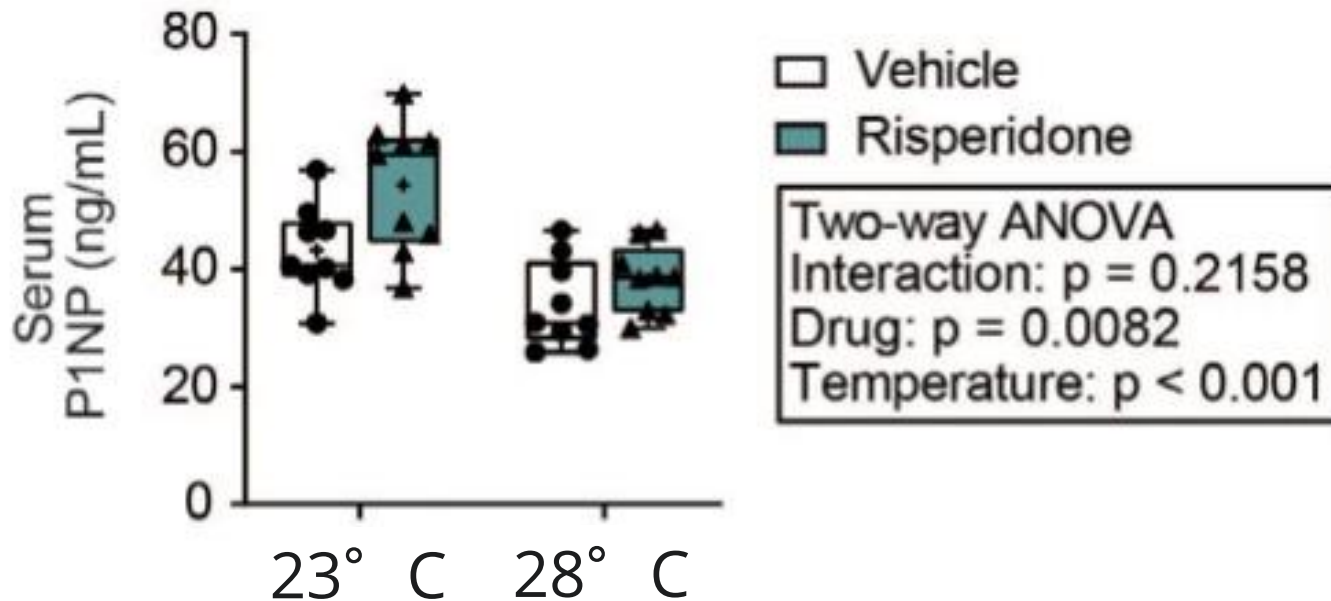
Dr Yu Mo, Zoology

moyu@tcd.ie | <https://github.com/github-moyu/Teaching>

Summary of lecture 5/6

- Moving from comparing 2 means to more than 2 means
- Simple one-way analysis of variance (ANOVA)
- Generation of F ratio (within versus between group variation), p value and 2 types of degrees of freedom
- More complex designs – concept of an interaction term

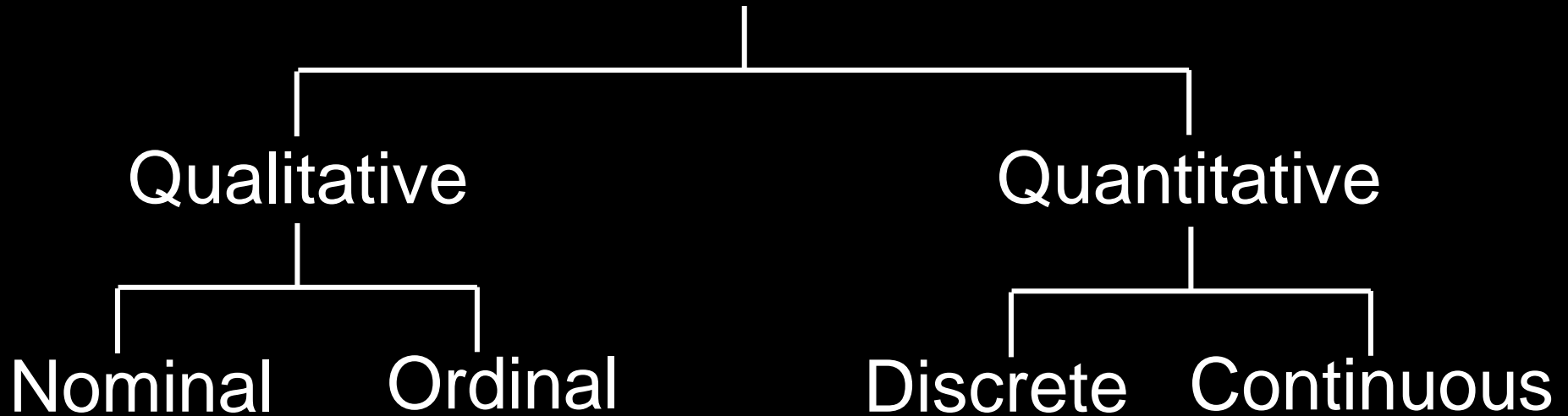
Effect of housing temperature on drug-induced bone loss



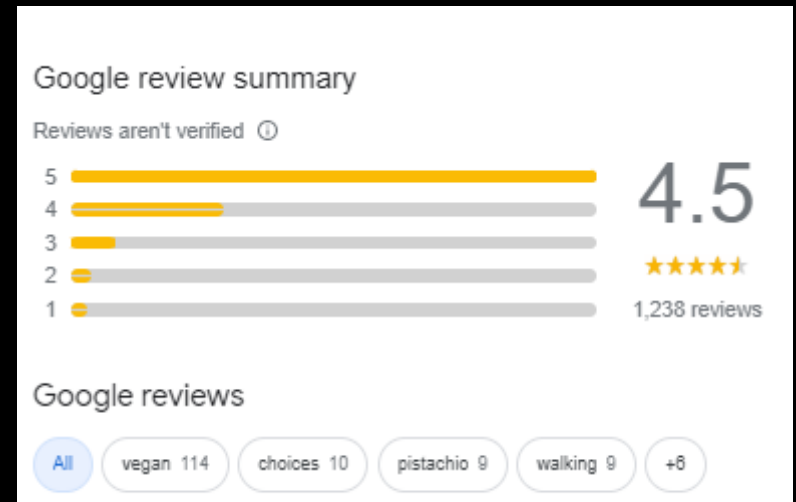
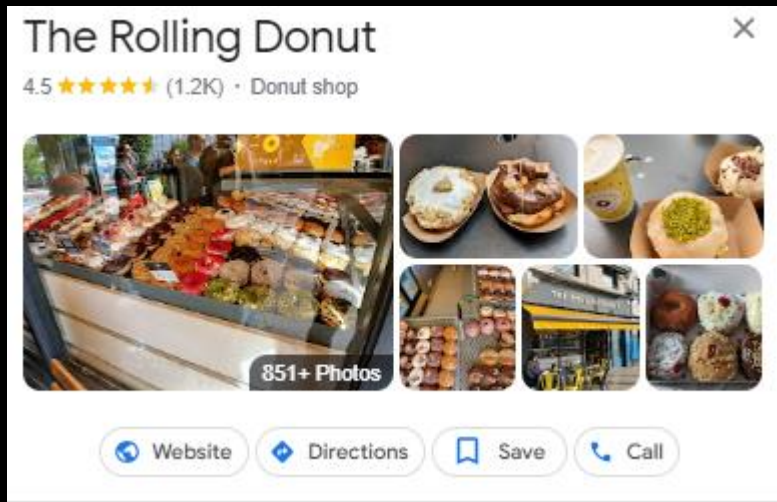
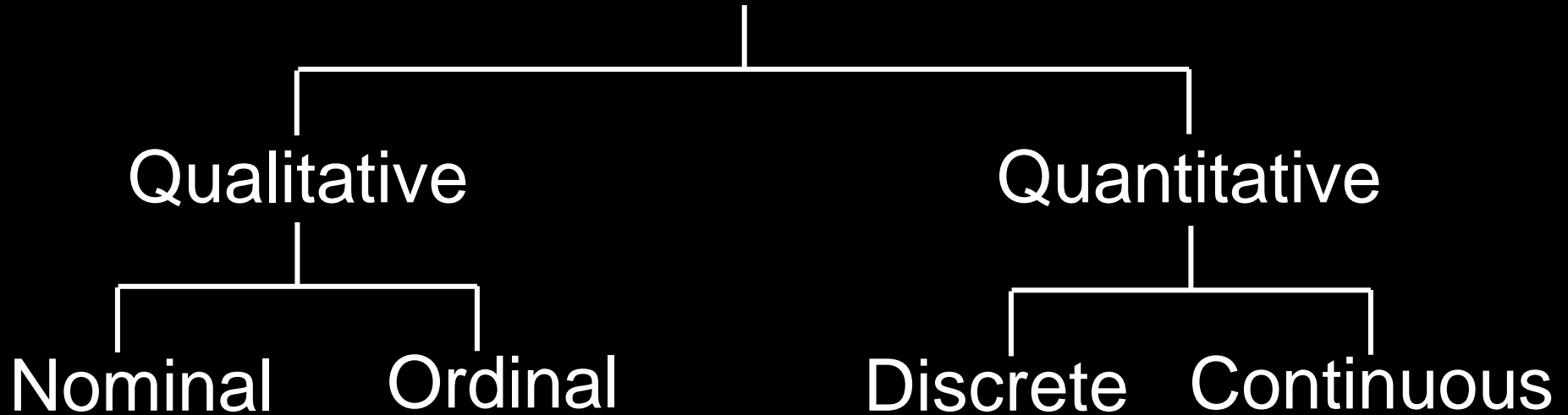
And now for something a little
different

How to interpret, plot and
analyse frequency data

Type of data



Type of data



Analysis of frequency data

Type of data

- Frequency
 - Categorical
-
- Independent observations
 - Random sampling
 - Presentation of data

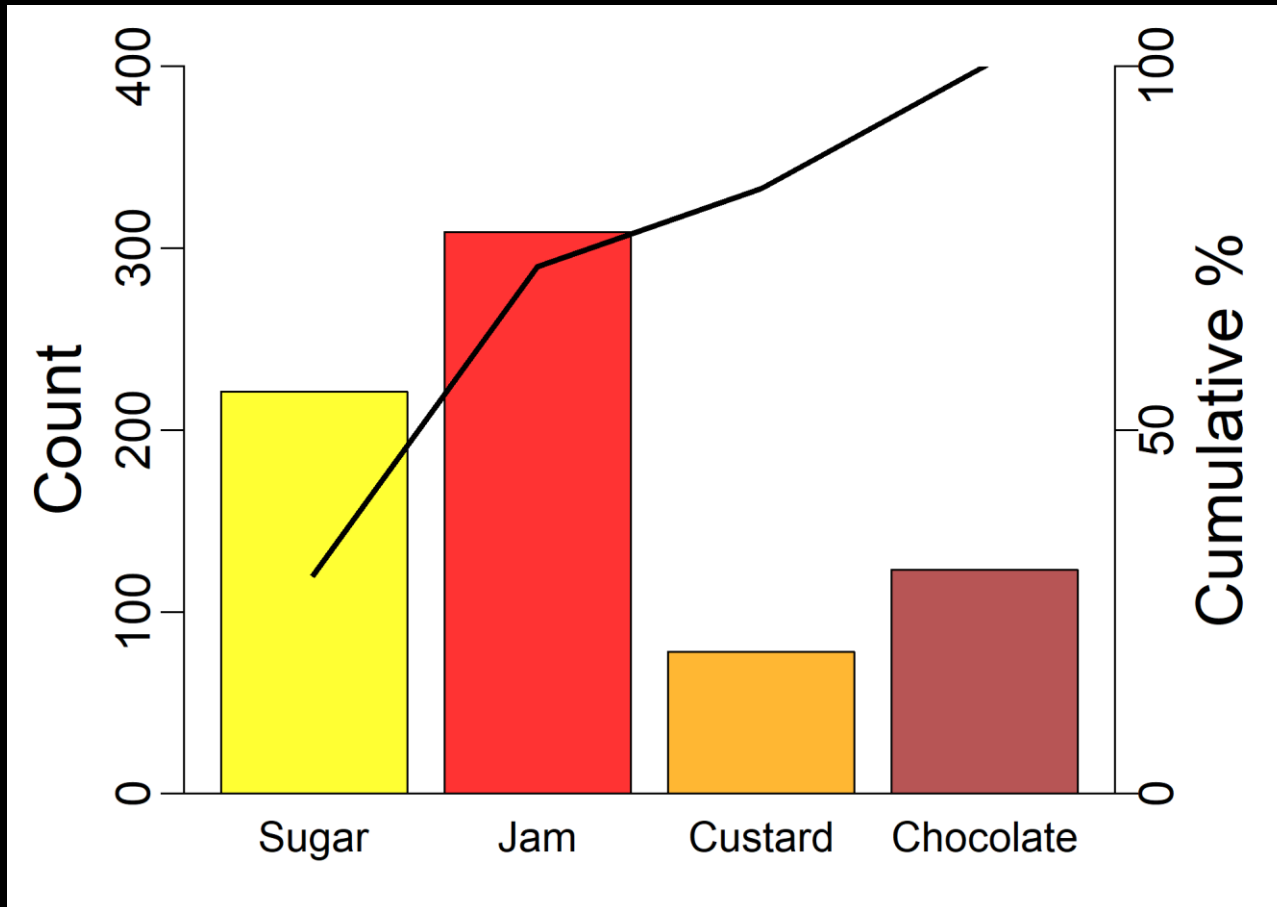
Doughnuts sold today

Frequency breakdown by type: 4 categories

Category	Frequency	Percent	Cumulative percent
Sugar	221	30.2	30.2
Jam	309	42.3	72.5
Custard	78	10.7	83.2
Chocolate	123	16.8	100
Total	731	100	-



Doughnuts sold today



The relationship between
college & doughnut type

College and doughnut type

H_0 : There is no association between college & the type of doughnut students like

- Proportion of students that like jam doughnut in zoology is equal to the proportion of students in geography that like jam doughnut

H_1 : There is an association between college & the type of doughnut students like

- Proportion of students that like jam doughnut in zoology is **NOT** equal to the proportion of students in geography that like jam doughnut

College and doughnut type

	Zoology	Geography	Total
Jam	21	36	57
Custard	102	69	171
Total	123	105	228

Calculation of expected values

	Zoology	Geography	Total
Jam	21	36	57
Custard	102	69	171
Total	123	105	228

- What do we expect if the null hypothesis is true?
- Overall $57/228 = 25\%$ students are jam-liking

- If there is no difference between zoology & geography, we would expect 25% of each
- Zoology:
 $25\% \text{ of } 123 = 30.75$
- Geography:
 $25\% \text{ of } 105 = 26.25$

Calculation of expected values

	Zoology	Geography	Total
Jam	21	36	57
Custard	102	69	171
Total	123	105	228

Custard-liking zoologists:

$$123 * 171 / 228 = 92.25$$

Custard-liking geographers:

$$105 * 171 / 228 = 78.75$$

Similarly we work out the expected values for the other two cells (custard)

Expected values = Column total * Row total / total number of obs.

H_0

Observed values

	Zoology	Geography
Jam	21	36
Custard	102	69

Expected values

	Zoology	Geography
Jam	30.75	26.25
Custard	92.25	78.75

Calculation of Chi-squared statistic

We now need a measure of the difference between the **observed** and the **expected**

$\chi^2 = \text{Sum of } (\text{Observed frequency} - \text{Expected frequency})^2 / \text{Expected frequency}$

Observed

	Zoology	Geography
Jam	21	36
Custard	102	69

Expected

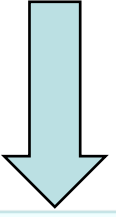
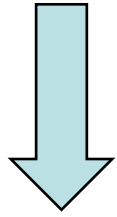
	Zoology	Geography
Jam	30.75	26.25
Custard	92.25	78.75

$\chi^2 = \text{Sum of } (\text{Observed frequency} - \text{Expected frequency})^2 / \text{Expected frequency}$

$$\begin{aligned}\chi^2 &= (21-30.75)^2/30.75 + (102-92.25)^2/92.25 \\ &\quad + (36-26.25)^2/26.25 + (69-78.75)^2/78.75 \\ &= 3.09 + 1.03 + 3.02 + 1.21 = 8.35\end{aligned}$$

$$\begin{aligned}df &= (\text{number of rows}-1) * (\text{number of columns}-1) \\ &= (2-1)*(2-1) = 1\end{aligned}$$

alpha



Degrees of freedom

V	0.975	0.9	0.5	0.1	0.05	0.025	0.01	0.005	0.001
1	0.000	0.016	0.445	2.706	3.841	5.02	6.64	7.88	10.82
2									
3									
4									
5									
30									
100									

Critical values of the chi-square distribution

Examine the critical values of the Chi-squared distribution

- Power of the test
0.05 (95%)
- Critical value at $df = 1$
3.84

- Any value > 3.84
Reject null hypothesis
- Any value < 3.84 **Do not reject** null hypothesis
- Since $8.35 > 3.84$
we reject the null hypothesis

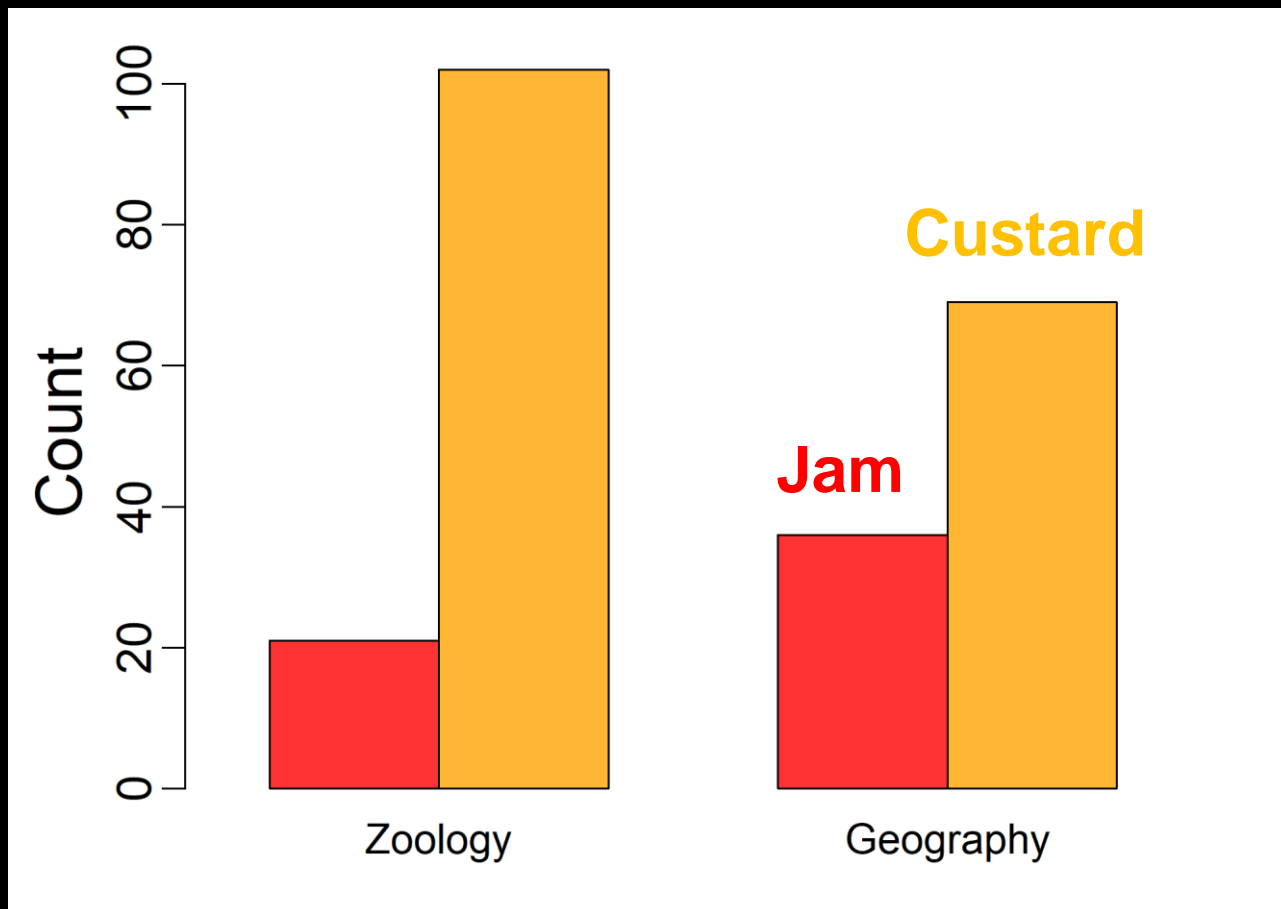
```
> chisq.test(d, correct=FALSE)
```

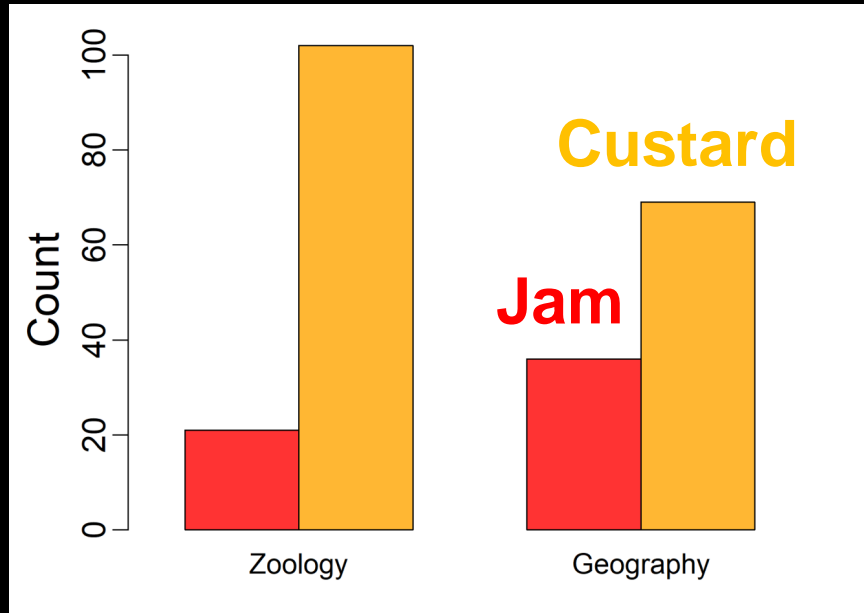
Pearson's Chi-squared test

data: d

X-squared = 8.9505, df = 1, p-value = 0.002774

There is an ASSOCIATION between college and doughnut preference





Chi-test

Frequency data (discrete)

+

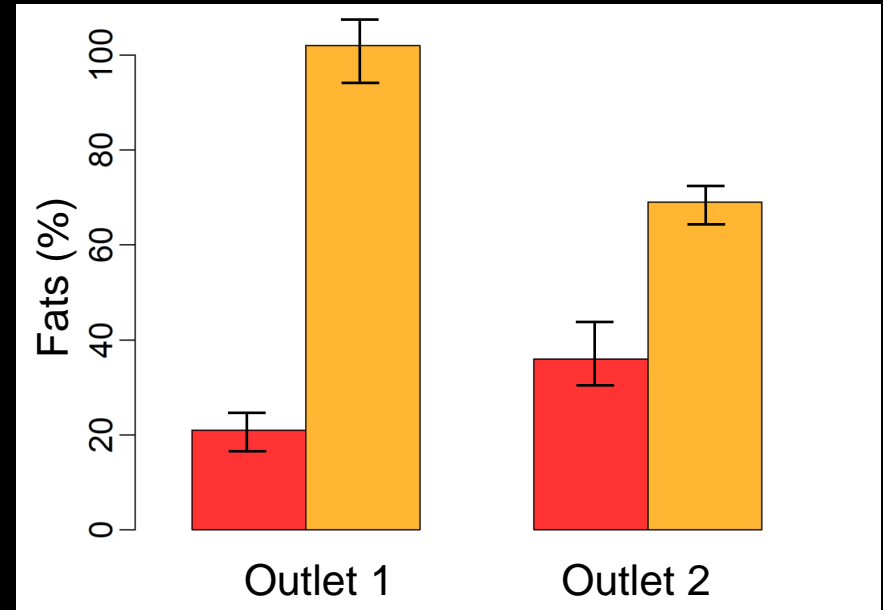
Categorical

ANOVA

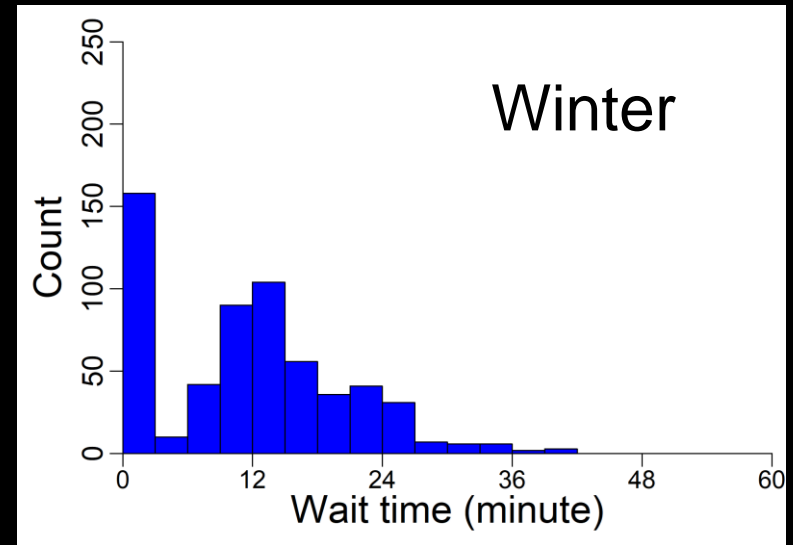
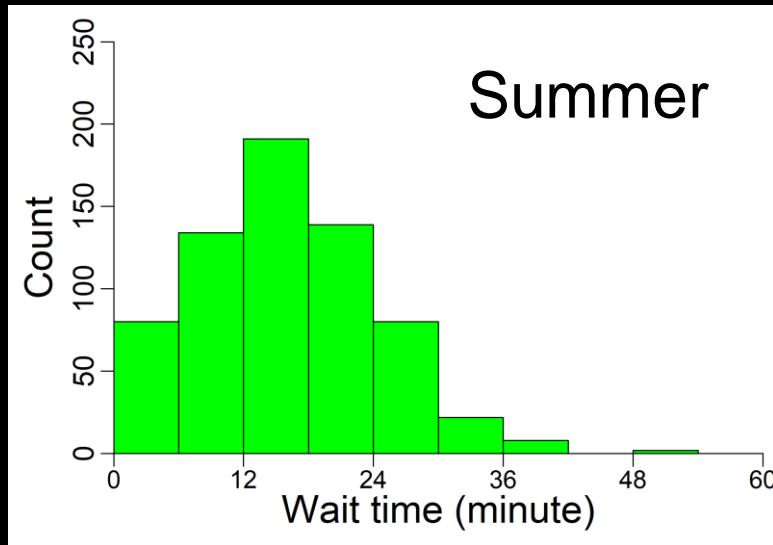
Continuous data

+

Categorical



Analysis influence of season on waiting time

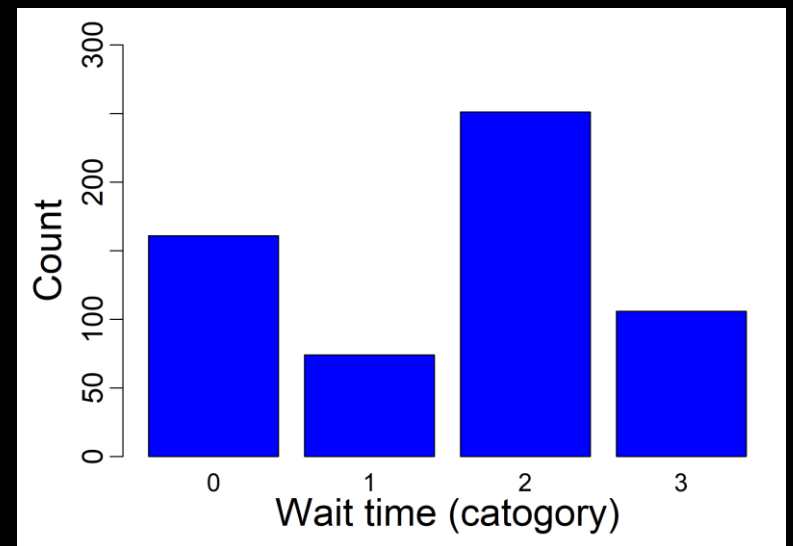
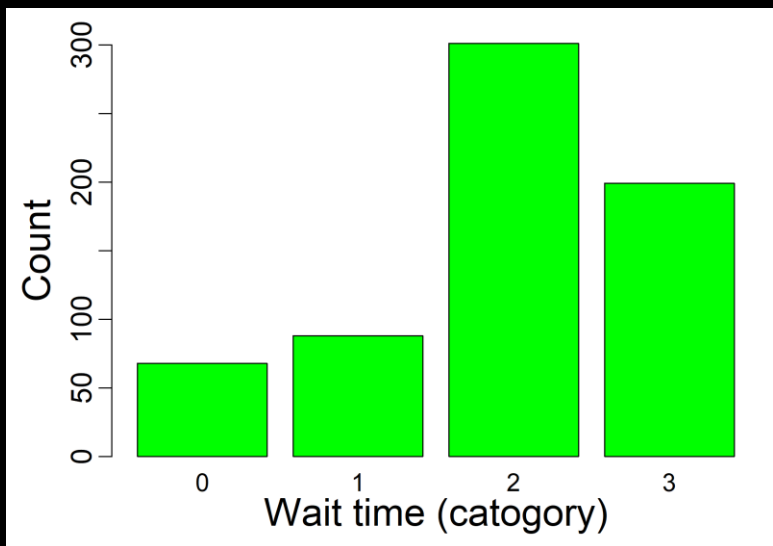
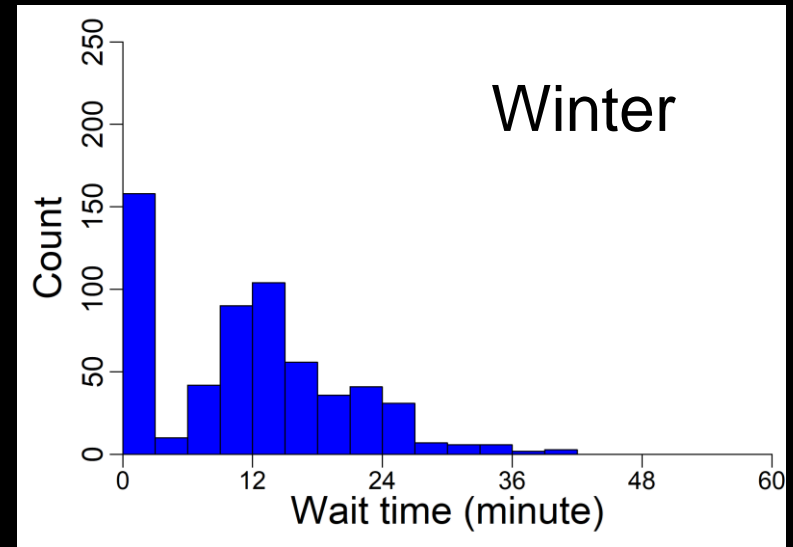
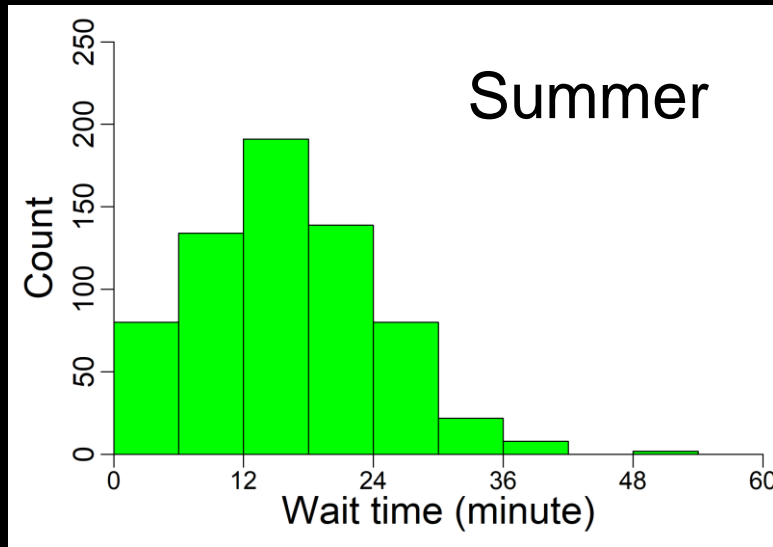


Data extremely skewed (**not t-test**)

Solution: create categories

Status coded: 0 (<5), 1 (<10), 2 (<20) & 3 (rest)

Analysis influence of season on waiting time



Analysis influence of season on waiting time

	0	1	2	3
Summer	68	88	301	199
Winter	161	74	251	106

```
> chisq.test(data_wait$Season,data_wait$cat, correct=FALSE)
```

Pearson's Chi-squared test

data: data_wait\$Season and data_wait\$cat
X-squared = 68.764, df = 3, p-value = 7.852e-15

$$\begin{aligned} df &= (\text{number of rows}-1) * (\text{number of columns}-1) \\ &= (2-1) * (4-1) = 3 \end{aligned}$$

Not more than 20% of the cells
should have an n less than 5

Solution: combine categories
for 2X2 tables can use Fisher's exact
test

Review

	Data	df
t-test	Continuous (two means)	n-1
ANOVA	Continuous (more than two means)	num df = denom df=
CHI	Discrete (frequency)	$(\# \text{ cat1} - 1) * (\# \text{ cat2} - 1)$