

## Homework #10

Solutions

MOSFET Amplifiers and Single-Stage MOSFET IC – *100 points*  
**DUE @ Beginning of Class: Tuesday, November 28**

- 1) E-Book, problem 4.31 (*10 points*)
- 2) E-Book, problem 4.44 (*15 points*)
- 3) E-Book, problem 4.52 (*10 points*)
- 4) E-Book, problem 4.53; hint: see Ex. 4.11 (*15 points*)
- 5) E-Book, problem 4.59 (*20 points*)
- 6) E-Book, problem 4.61 (*15 points*)
- 7) E-Book, problem 4.65; hint:  $I_{dD} = I_Q = I_{dL}$  (*15 points*)

1) E-Book, problem 4.31 (10 points)

- 4.31 The open-circuit ( $R_L = \infty$ ) voltage gain of the ac equivalent source-follower circuit shown in Figure P4.31 is  $A_v = 0.98$ . When  $R_L$  is set to 1 k $\Omega$ , the voltage gain is reduced to  $A_v = 0.49$ . What are the values of  $g_m$  and  $r_o$ ?

Source-follower, so:

$$A_v = \frac{g_m (R_s || r_o)}{1 + g_m (R_s || r_o)} \left( \frac{R_L}{R_s + R_L} \right), \quad R_s = R_o$$

$$\therefore A_v = \frac{g_m (R_L || r_o)}{1 + g_m (R_L || r_o)} \quad 2$$

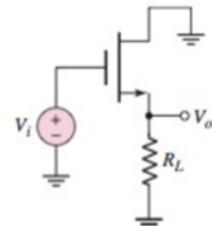


Figure P4.31

If  $R_L = \infty$  then:

$$0.98 = \frac{g_m r_o}{1 + g_m r_o} \Rightarrow g_m r_o = 49 \quad 2$$

If  $R_L = 1k\Omega$ :

$$0.49 = \frac{g_m (R_L || r_o)}{1 + g_m (R_L || r_o)} = \frac{g_m \left( \frac{R_L r_o}{R_L + r_o} \right)}{1 + g_m \left( \frac{R_L r_o}{R_L + r_o} \right)} = \frac{g_m (R_L r_o)}{R_L + r_o + g_m (R_L r_o)}$$

$$0.49 = \frac{(49)(1k\Omega)}{1k\Omega + r_o + (49)(1k\Omega)} = \frac{49k\Omega}{50k\Omega + r_o}$$

$$\Rightarrow r_o = 50k\Omega \quad 4$$

$$g_m = \frac{49}{r_o} = 0.98 \text{ mA/V} \quad 2$$

2) E-Book, problem 4.44 (15 points)

- 4.44 The transistor in the circuit in Figure P4.44 has parameters  $V_{TN} = 0.4$  V,  $K_n = 0.5 \text{ mA/V}^2$ , and  $\lambda = 0$ . The circuit parameters are  $V_{DD} = 3$  V and  $R_i = 300 \text{ k}\Omega$ . (a) Design the circuit such that  $I_{DQ} = 0.25 \text{ mA}$  and  $V_{DSQ} = 1.5$  V. (b) Determine the small-signal voltage gain and the output resistance  $R_o$ .

Source-follower amplifier

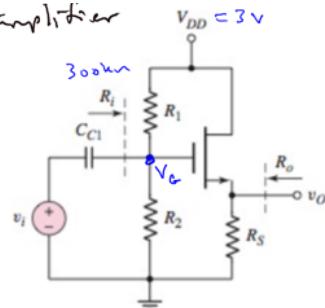


Figure P4.44

a) DC analysis,  $\text{KVVL}$ :

$$V_{DQ} = V_{DSQ} + I_{DQ} R_s$$

$$3 \text{ V} = 1.5 \text{ V} + (0.25 \text{ mA}) R_s$$

$$\Rightarrow R_s = 6 \text{ k}\Omega \quad 3$$

$$V_s = (0.25 \text{ mA}) / (6 \text{ k}\Omega) = 1.5 \text{ V}$$

$$I_{DQ} = K_n (V_{GSA} - V_{TN})^2$$

$$0.25 \text{ mA} = (0.5 \text{ mA/V}^2) (V_{GSA} - 0.4 \text{ V})^2$$

$$\Rightarrow V_{GSA} = 1.107 \text{ V}$$

$$\text{KVVL: } V_G = V_{GSA} + V_s = 1.107 \text{ V} + 1.5 \text{ V} = 2.607 \text{ V}$$

voltage divider:

$$V_G = \left( \frac{R_2}{R_1 + R_2} \right) V_{DD} = \frac{1}{R_1} R_{in} V_{DD}$$

$$2.607 \text{ V} = \frac{1}{R_1} (300 \text{ k}\Omega) (3 \text{ V}) \Rightarrow R_1 = 345.2 \text{ k}\Omega \quad 4$$

$$\therefore R_2 = 2.29 \text{ M}\Omega \quad 4$$

b) Assuming no  $r_o$ ; also there is no  $R_s$ :

$$\therefore A_v = \frac{g_m R_s}{1 + g_m R_s}$$

$$\downarrow g_m = 2 \sqrt{K_n I_{DQ}} = 2 \sqrt{(0.5 \text{ mA/V}^2)(0.25 \text{ mA})} = 0.707 \text{ mA/V}$$

$$A_v = \frac{(0.707 \text{ mA/V})(6 \text{ k}\Omega)}{1 + (0.707 \text{ mA/V})(6 \text{ k}\Omega)} = 0.809 \quad 2$$

$$R_o = \frac{1}{g_m} || R_s = \frac{1}{0.707 \text{ mA/V}} || 6 \text{ k}\Omega = 1.14 \text{ k}\Omega \quad 2$$

3) E-Book, problem 4.52 (10 points)

- 4.52 For the common-gate amplifier in Figure 4.35 in the text, the PMOS transistor parameters are  $V_{TP} = -0.8 \text{ V}$ ,  $K_p = 2.5 \text{ mA/V}^2$ , and  $\lambda = 0$ . The circuit parameters are  $V^+ = 3.3 \text{ V}$ ,  $V^- = -3.3 \text{ V}$ ,  $R_G = 100 \text{ k}\Omega$ , and  $R_L = 4 \text{ k}\Omega$ . (a) Determine  $R_S$  and  $R_D$  such that  $I_{DQ} = 1.2 \text{ mA}$  and  $V_{SDQ} = 3 \text{ V}$ . (b) Determine the small-signal voltage gain  $A_v = v_o/v_i$ .

a)

$$I_{DQ} = K_p (V_{SGQ} + V_{TP})^2$$

$$1.2 \text{ mA} = (2.5 \text{ mA/V}^2)(V_{SGQ} - 0.8 \text{ V})^2$$

$$\Rightarrow V_{SGQ} = 1.493 \text{ V}$$

$$R_S = \frac{V^+ - V_{SGQ}}{I_{DQ}} = \frac{3.3 \text{ V} - 1.493 \text{ V}}{1.2 \text{ mA}} = 1.51 \text{ k}\Omega \quad 4$$

KVL:

$$V_{SDQ} = V^+ - V^- - I_{DQ}(R_S + R_D)$$

$$3 \text{ V} = 6.6 \text{ V} - (1.2 \text{ mA})(1.51 \text{ k}\Omega + R_D) \Rightarrow R_D = 1.49 \text{ k}\Omega \quad 2$$

b)

$$A_v = \frac{g_m(R_D || R_L)}{1 + g_m R_S} \quad (R_{Si} = 0 \text{ in this case}) = g_m(R_D || R_L)$$

$$g_m = 2\sqrt{K_p I_{DQ}} = 2\sqrt{(2.5 \text{ mA/V}^2)(1.2 \text{ mA})} = 3.46 \text{ mA/V}$$

$$A_v = (3.46 \text{ mA/V})(1.49 \text{ k}\Omega || 4 \text{ k}\Omega) = 3.76 \quad 4$$

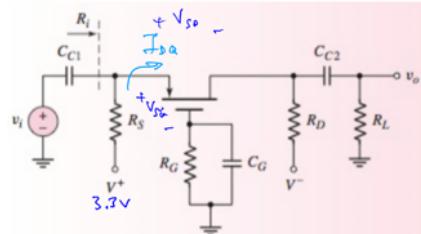


Figure 4.35 Figure for Exercise Ex 4.10

4) E-Book, problem 4.53; hint: see Ex. 4.11 (15 points)

- 4.53 Consider the NMOS amplifier with saturated load in Figure 4.39(a). The transistor parameters are  $V_{TND} = V_{TNL} = 0.6 \text{ V}$ ,  $k'_n = 100 \mu\text{A/V}^2$ ,  $\lambda = 0$ , and  $(W/L)_L = 1$ . Let  $V_{DD} = 3.3 \text{ V}$ . (a) Design the circuit such that the small-signal voltage gain is  $|A_v| = 5$  and the  $Q$ -point is in the center of the saturation region. (b) Determine  $I_{DQ}$  and  $V_{DSDQ}$ .

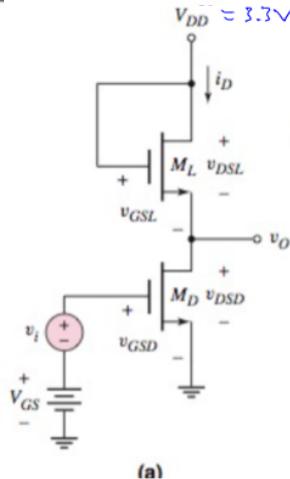
$$\text{a)} |A_v| = \frac{(W/L)_D}{(W/L)_L} = 5 \Rightarrow (W/L)_D = 25 \quad 2$$

From Ex. 4.11:

$$V_{GS0t} = \frac{(V_{DD} - V_{TNt}) + V_{TNt}(1 + |A_v|)}{1 + |A_v|} = 1.05 \text{ V}$$

$$V_{GS0a} = \frac{V_{GS0b} - V_{TN0}}{2} + V_{TN0} = 0.825 \text{ V} \quad 3$$

↑  
cut-off point



$Q$ -point centered in sat. region of driver

$$\text{b)} I_{DQ} = \left(\frac{k'_n}{2}\right) \left(\frac{W}{L}\right)_D (V_{GS0a} - V_{TN})^2 = \left(\frac{0.1 \text{ mA/V}^2}{2}\right) (25) (0.825 \text{ V} - 0.6 \text{ V})^2 = 0.063 \text{ mA} \quad 4$$

$$\text{Since } I_{DQ} = I_{DL}$$

$$\left(\frac{W}{L}\right)_D (V_{GS0a} - V_{TN})^2 = \left(\frac{W}{L}\right)_L (V_{GSL} - V_{TN})^2$$

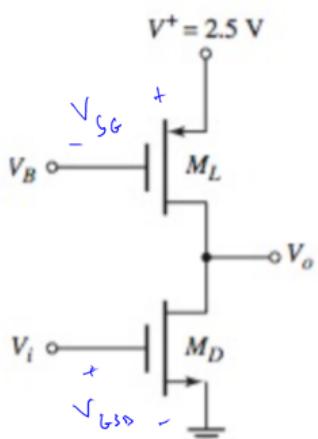
$$5 (V_{GS0a} - V_{TN}) = V_{DD} - V_o - V_{TN} \sim KV_L$$

$$5 (0.825 \text{ V} - 0.6 \text{ V}) = 3.3 \text{ V} - V_o - 0.6 \text{ V}$$

$$\Rightarrow V_o = V_{GS0a} = 1.575 \text{ V} \quad 6$$

5) E-Book, problem 4.59 (20 points)

- 4.59 The transistor parameters for the common-source circuit in Figure P4.59 are  $V_{TND} = 0.4 \text{ V}$ ,  $V_{TPL} = -0.4 \text{ V}$ ,  $(W/L)_L = 50$ ,  $\lambda_D = 0.02 \text{ V}^{-1}$ ,  $\lambda_L = 0.04 \text{ V}^{-1}$ ,  $k'_n = 100 \mu\text{A/V}^2$ , and  $k'_p = 40 \mu\text{A/V}^2$ . At the  $Q$ -point,  $I_{DQ} = 0.5 \text{ mA}$ . (a) Determine  $(W/L)_D$  such that the small-signal voltage gain is  $A_v = V_o/V_i = -40$ . (b) What is the required value of  $V_B$ ? (c) What is the value of  $V_{GSDQ}$ ?



$$a) A_v = -g_m n \left( r_{on} \| r_{od} \right) = -40$$

$$\begin{aligned} r_{od} &= \frac{1}{\lambda_D I_{DQ}} = \frac{1}{(0.02 \text{ V}^{-1})(0.5 \text{ mA})} = 100 \text{ k}\Omega \\ r_{on} &= \frac{1}{\lambda_L I_{DQ}} = 50 \text{ k}\Omega \\ r_{on} \| r_{od} &= 33.3 \text{ k}\Omega \end{aligned}$$

Figure P4.59

assume lamda negligible contribution

b) DC analysis:

$$I_{DQ} = \left(\frac{k'_n}{2}\right) \left(\frac{w}{L}\right)_L \left(V_{SGQ} + V_{TP}\right)^2$$

$$0.5 \text{ mA} = \left(\frac{0.04 \text{ mA/V}^2}{2}\right) \left(50\right) \left(V_{SGQ} - 0.4 \text{ V}\right)^2$$

$$\Rightarrow V_{SGQ} = 1.107 \text{ V} = V^+ - V_B$$

$$1.107 \text{ V} = 2.5 \text{ V} - V_B$$

$$\Rightarrow V_B = 1.393 \text{ V}$$

8

$$g_m n = 2 \sqrt{\left(\frac{k'_n}{2}\right) \left(\frac{w}{L}\right)_D I_{DQ}}$$

$$1.20 \text{ mA/V} = 2 \sqrt{\left(\frac{0.1 \text{ mA/V}^2}{2}\right) \left(\frac{w}{L}\right)_D (0.5 \text{ mA})}$$

$$\Rightarrow \left(\frac{w}{L}\right)_D = 14.4 \quad 8$$

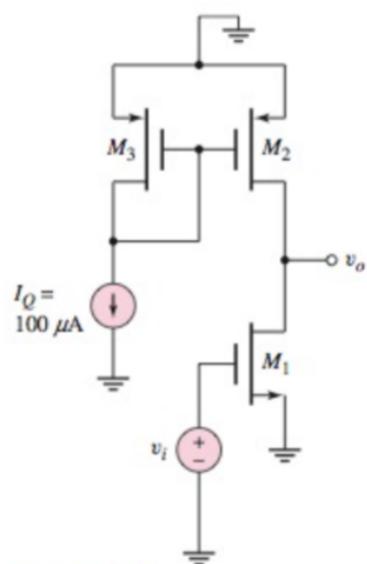
$$c) I_{DQ} = \left(\frac{k'_n}{2}\right) \left(\frac{w}{L}\right)_D \left(V_{GSDQ} - V_{TNQ}\right)^2$$

$$\Rightarrow V_{GSDQ} = 1.233 \text{ V}$$

4

6) E-Book, problem 4.61 (15 points)

- 4.61 The ac equivalent circuit of a CMOS common-source amplifier is shown in Figure P4.61. The transistor parameters for  $M_1$  are  $V_{TN} = 0.5$  V,  $k'_n = 85 \mu\text{A/V}^2$ ,  $(W/L)_1 = 50$ , and  $\lambda = 0.05 \text{ V}^{-1}$ , and for  $M_2$  and  $M_3$  are



Determine  $A_v$ .

$$A_v = -g_m1 (r_{o1} \parallel r_{o2})$$

$$\begin{aligned} g_{m1} &= 2 \sqrt{k_n I_{D1}} \\ &= 2 \sqrt{\left(\frac{85 \mu\text{A/V}^2}{2}\right)(50)(100 \mu\text{A})} = 0.922 \text{ mA/V} \end{aligned}$$

$$r_{o1} = \frac{1}{\lambda_1 I_{D1}} = \frac{1}{(0.05 \text{ V}^{-1})(0.1 \text{ mA})} = 200 \text{ k}\Omega \quad 2$$

$$r_{o2} = \frac{1}{\lambda_2 I_{D2}} = \frac{1}{(0.075 \text{ V}^{-1})(0.1 \text{ mA})} = 133.3 \text{ k}\Omega \quad 2$$

$$A_v = - (0.922 \text{ mA/V}) (200 \text{ k}\Omega \parallel 133.3 \text{ k}\Omega)$$

$$= -73.7 \quad 9$$

Figure P4.61

7) E-Book, problem 4.65; hint:  $I_{dD} = I_Q = I_{dL}$  (15 points)

- 4.65 Figure P4.65 shows a common-gate amplifier. The transistor parameters are  $V_{TN} = 0.6 \text{ V}$ ,  $V_{TP} = -0.6 \text{ V}$ ,  $K_n = 2 \text{ mA/V}^2$ ,  $K_p = 0.5 \text{ mA/V}^2$ , and  $\lambda_n = \lambda_p = 0$ . (a) Find the values of  $V_{SGLQ}$ ,  $V_{GSDQ}$ , and  $V_{DSDQ}$ . (b) Derive the expression for the small-signal voltage gain in terms of  $K_n$  and  $K_p$ . (c) Calculate the value of the small-signal voltage gain  $A_v = V_o/V_i$ .

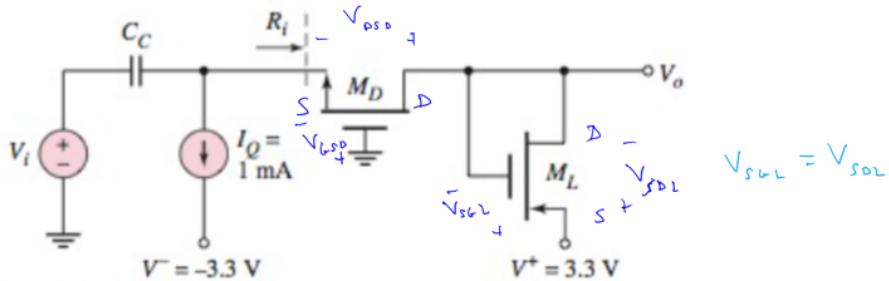


Figure P4.65

$$a) I_{DQ} = K_n (V_{GSDQ} - V_{TN})^2 = I_Q$$

$$1 \text{ mA} = (2 \text{ mA/V}^2)(V_{GSDQ} - 0.6 \text{ V})^2 \Rightarrow V_{GSDQ} = 1.307 \text{ V} \quad 3$$

$$I_{DQ} = K_p (V_{SGLQ} + V_{TP})^2$$

$$1 \text{ mA} = (0.5 \text{ mA/V}^2)(V_{SGLQ} + 0.6 \text{ V})^2 \Rightarrow V_{SGLQ} = 2.014 \text{ V} \quad 3$$

$$V_o = 3.3 \text{ V} - V_{sdlQ} = 3.3 \text{ V} - 2.014 \text{ V} = 1.286 \text{ V}$$

$$\text{KVL: } V_{psdq} = V_o + V_{GSDQ} = 1.286 \text{ V} + 1.307 \text{ V} = 2.593 \text{ V} \quad 3$$

$$b) i_{DQ} = i_{D2} \quad \text{from small signal equiv circuit}$$

$$g_{mD} V_i = g_{mL} V_o$$

$$A_v = \frac{V_o}{V_i} = \frac{g_{mD}}{g_{mL}} = \sqrt{\frac{K_n}{K_p}} \quad 4$$

$$c) A_v = \sqrt{\frac{2}{0.5}} = 2 \quad 2$$