

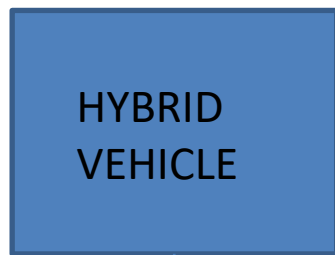
# CONTROL OF H.E.V USING FUZZY LOGIC

FINAL-SEMESTER PRESENTATION

Abishek Krishnan 2011B5A3511H

S Murali Krishna Sai 2011B3AA375H

# HYBRID ELECTRIC VEHICLE

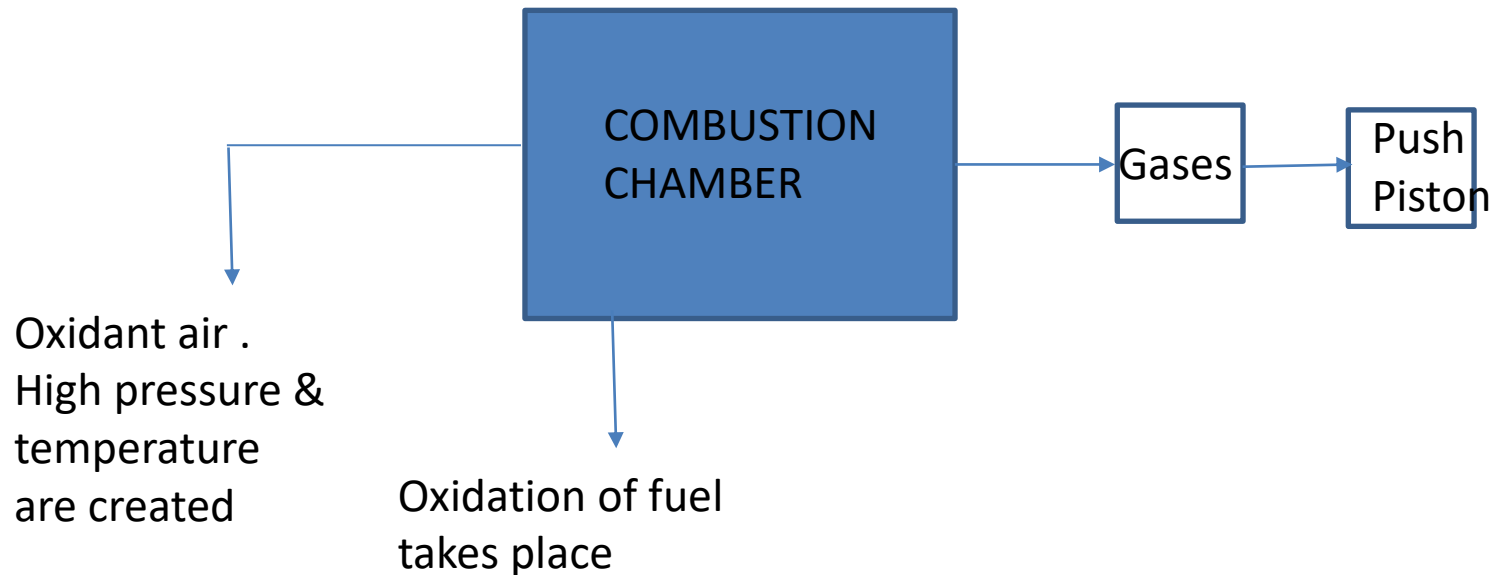


Run on two or  
more distinct  
power sources



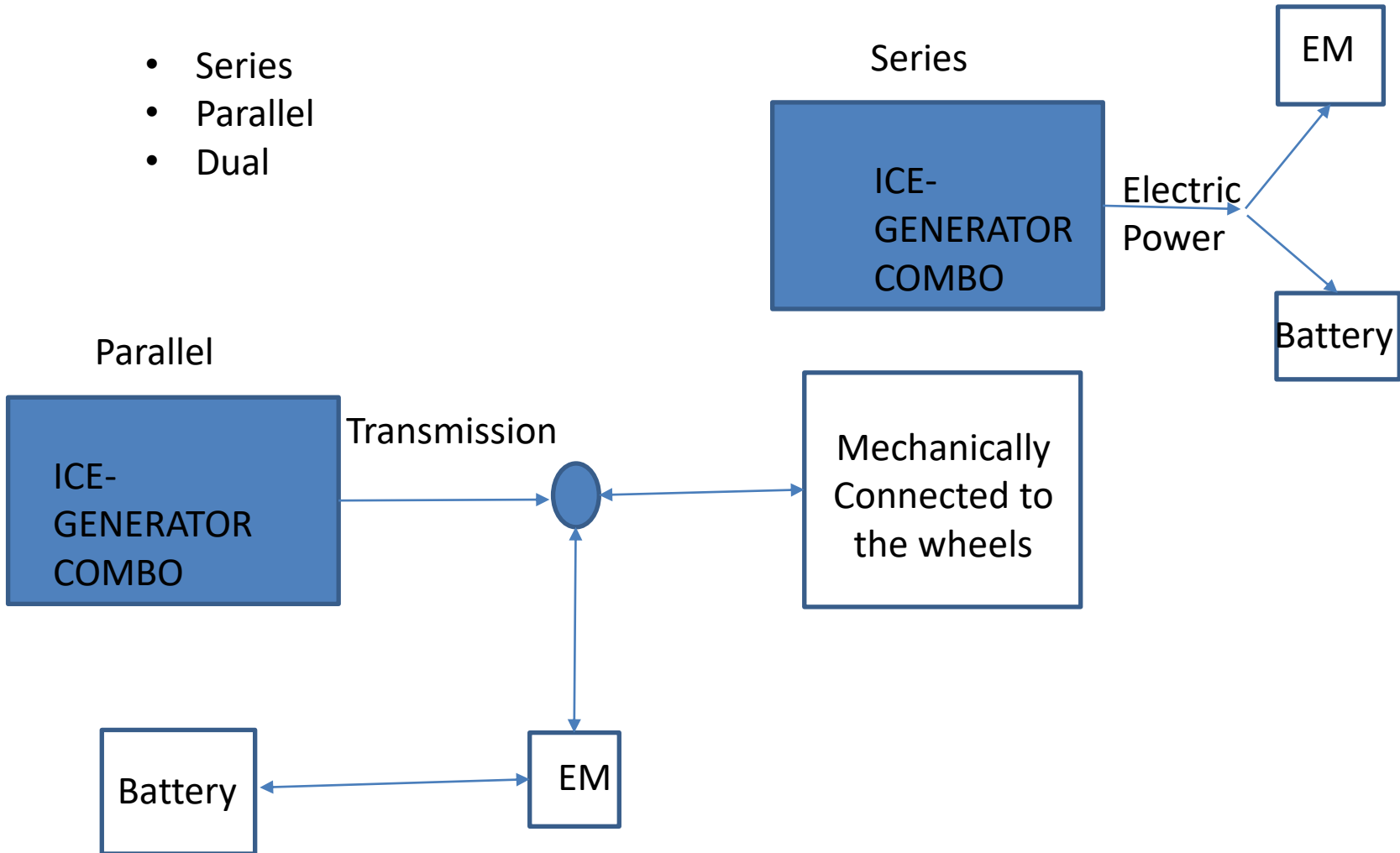
Run on one or  
more Electric  
Motor

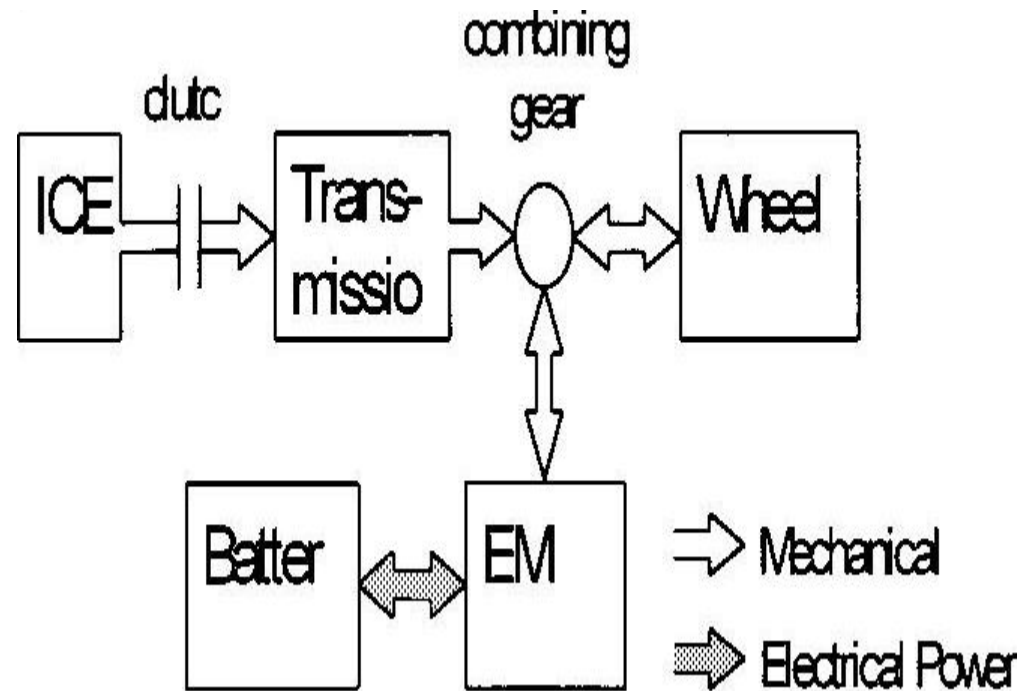
# INTERNAL COMBUSTION ENGINE



# Types of HEV

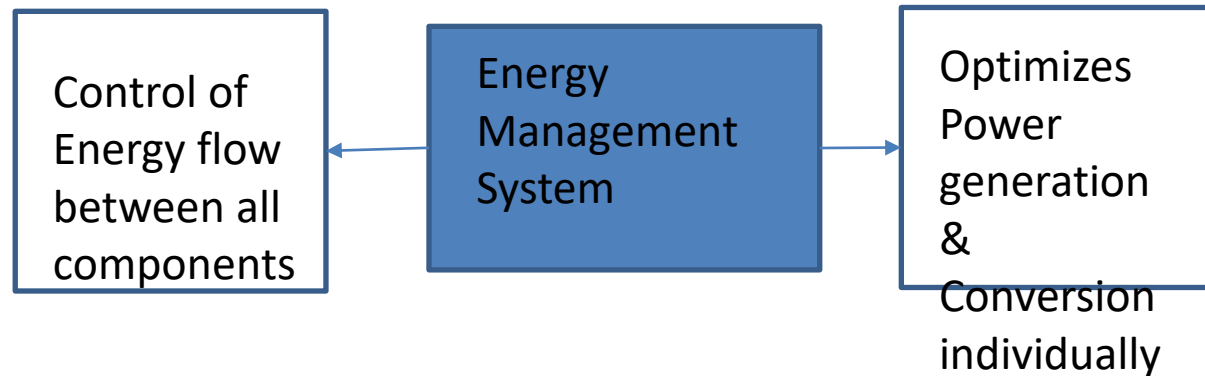
- Series
- Parallel
- Dual





- Power to wheel by ICE
- Power to wheel by EM
- Power to wheel by ICE & EM simultaneously
- Charge the battery, using part of ICE power to drive the EM as a generator (the other part of ICE power) is used to drive wheels
- Slow down the Vehicle by letting wheels drive the EM as a generator that provides power to the battery (regenerative braking)

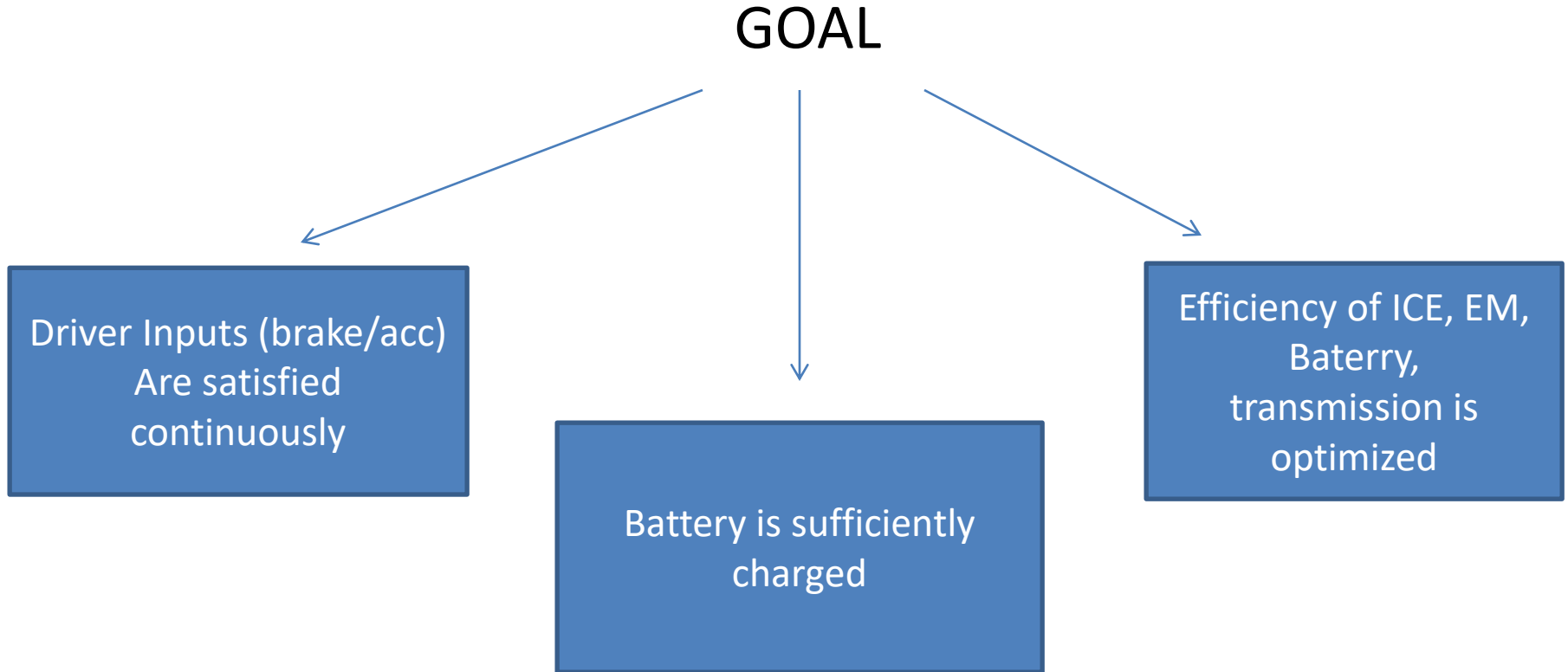
# Power Controller



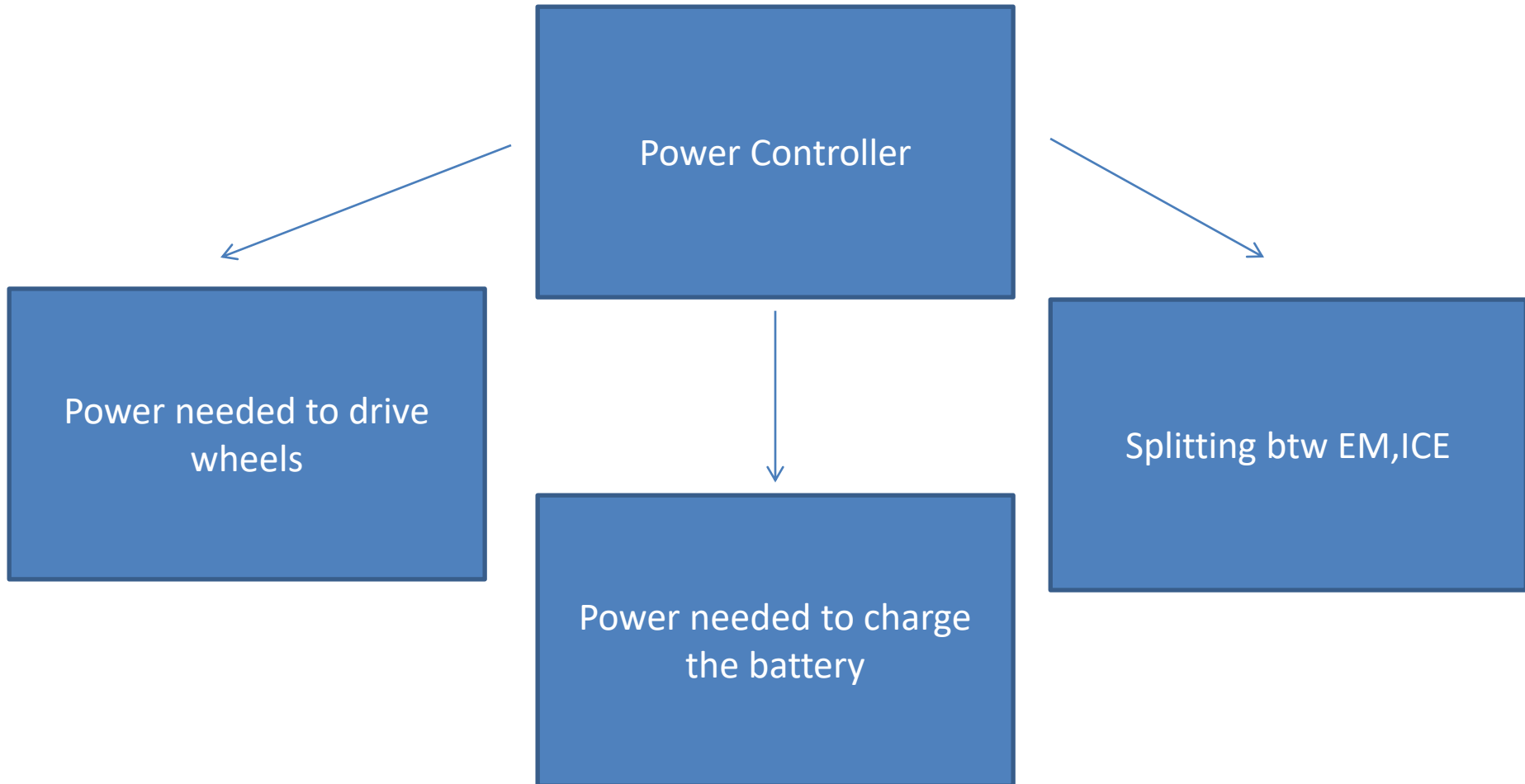
## Fuzzy logic

- Imprecise measurements
- Component Variability
- Rule based Energy management Strategy.

## SECTION-III:ENERGY MANAGEMENT STRATERGY

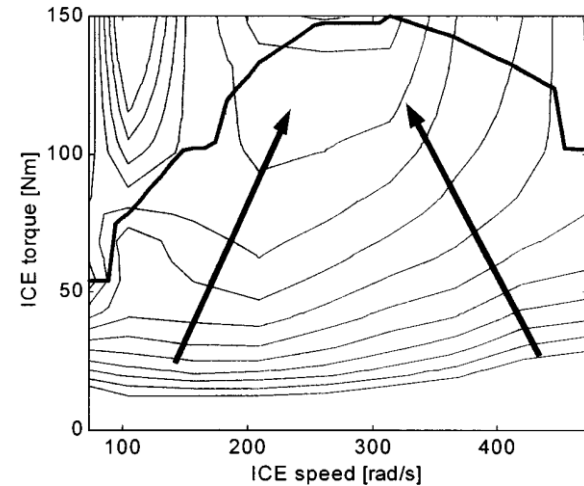


# Power Controller

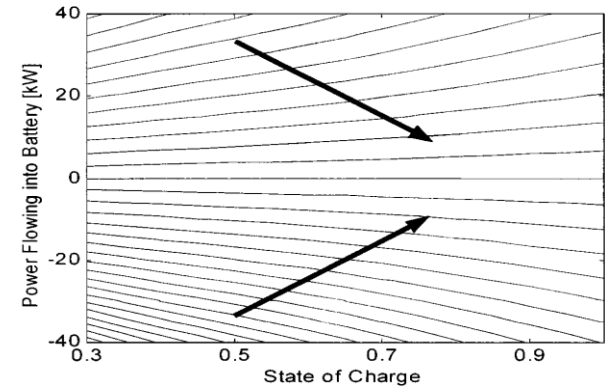




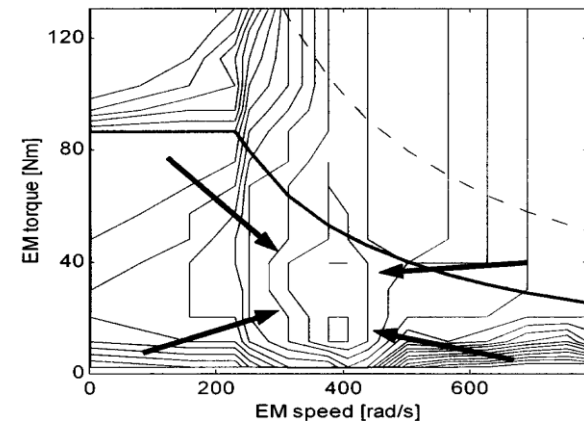
# A. Efficiency Maps



ICE Power should not be  
( $\leq 6\text{KW}$  or  $\geq 50\text{KW}$ )  
Torque: Throttle angle  
Speed: Shifting Gear

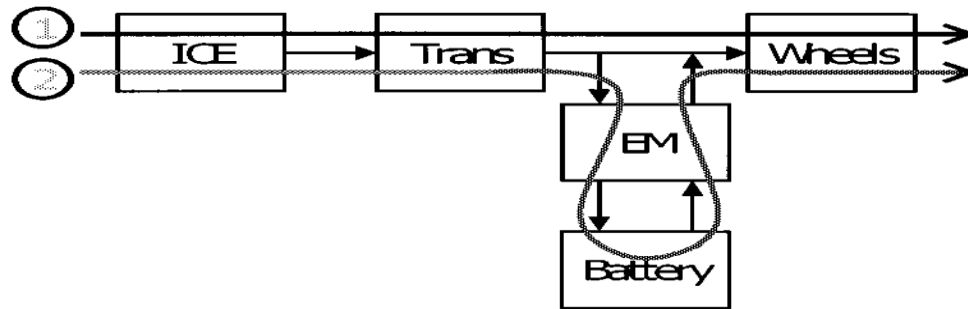


High SOC  
Low Power Level



EM speed can't be  
gear shifted so,  
Optimize power at  
given speed

## B. Power Split Strategy



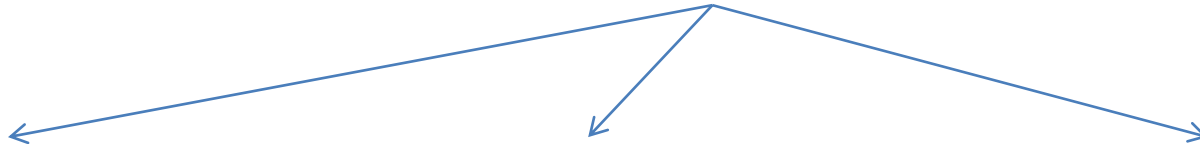
Losses associated with path-2

1. Efficiency of EM : 1<sup>st</sup> as generator ; 2<sup>nd</sup> motor
2. Efficiency of Battery: 1<sup>st</sup> to store; 2<sup>nd</sup> to release

After calculations



Advisable to use path 2 over path 1  
only when  
path 1 is 16% less efficient than path 2

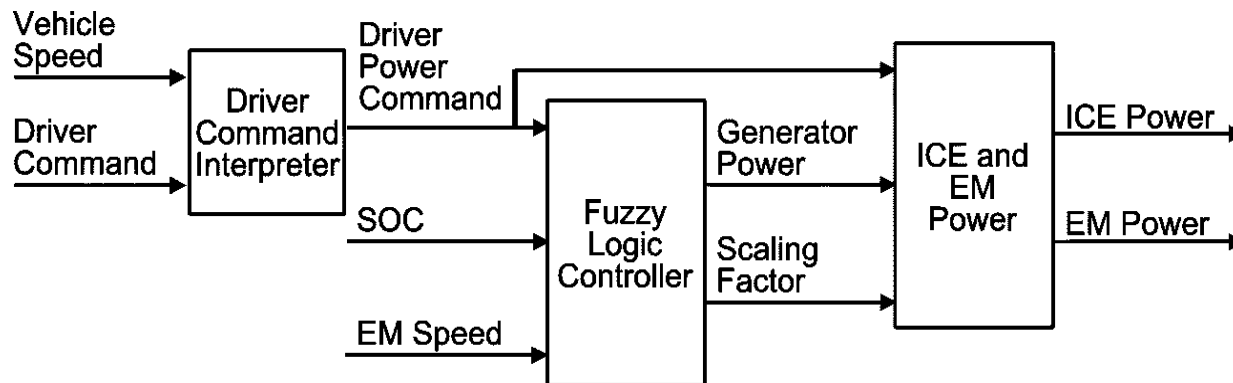
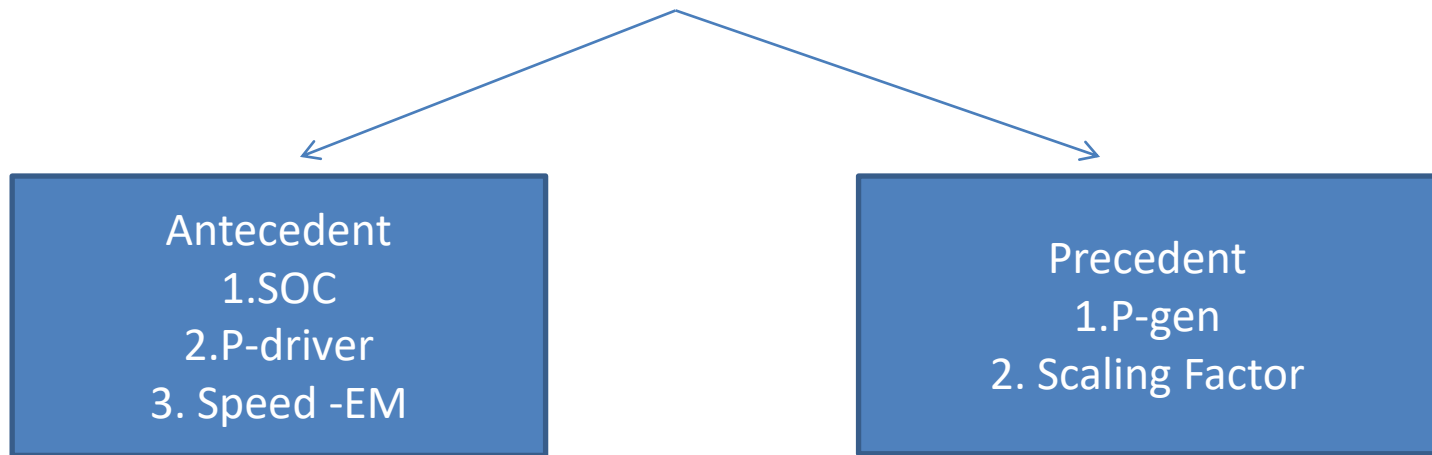


a) Power level < 6KW  
Only EM

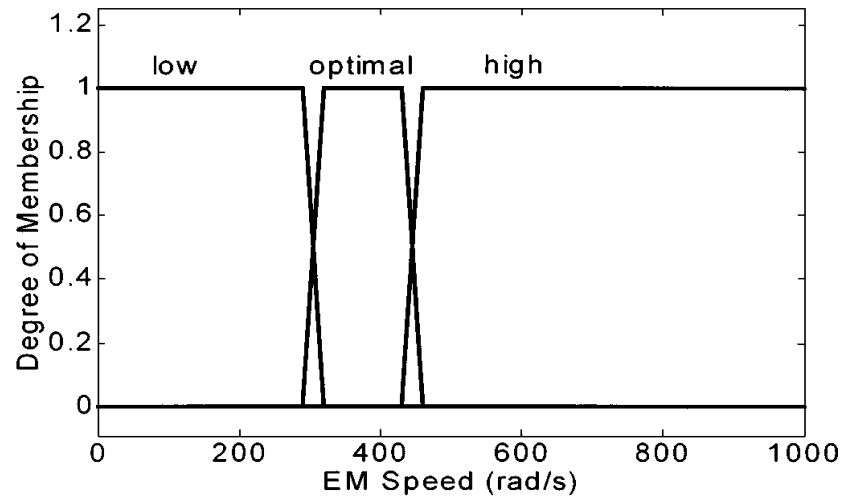
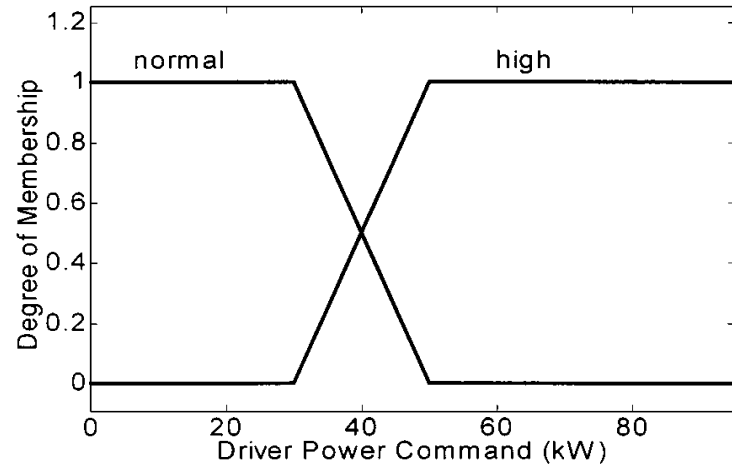
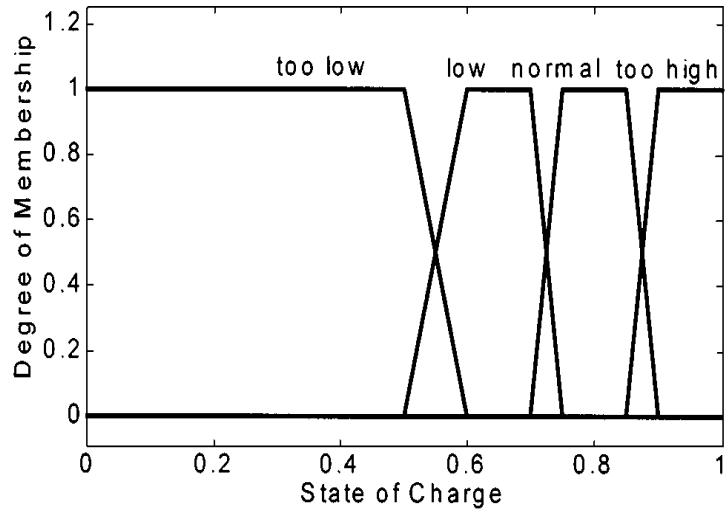
b) Power Level 6-50 KW  
Only ICE

c) Power level >50KW  
EM to complement  
ICE

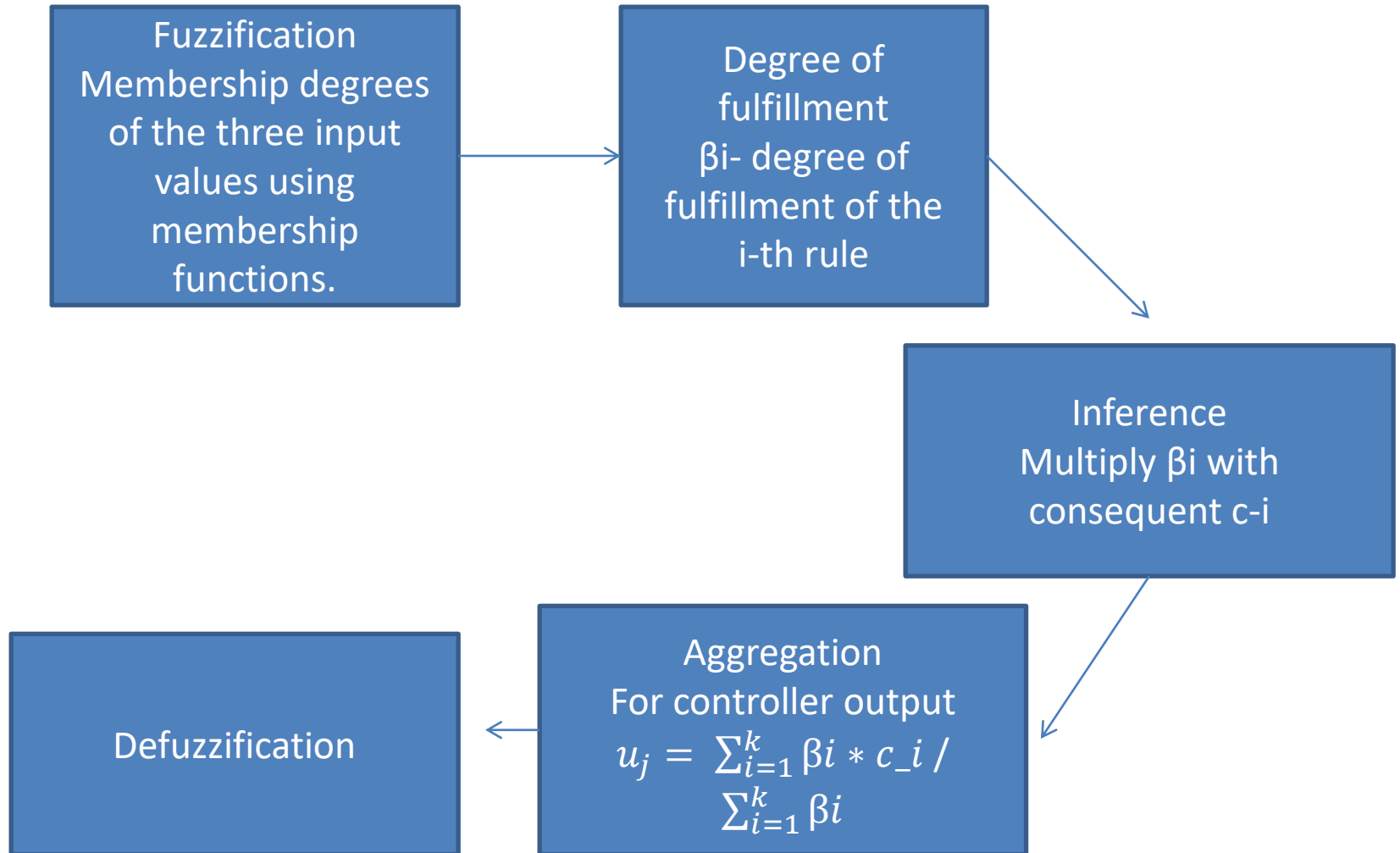
## Section IV: Fuzzy Logic Controller



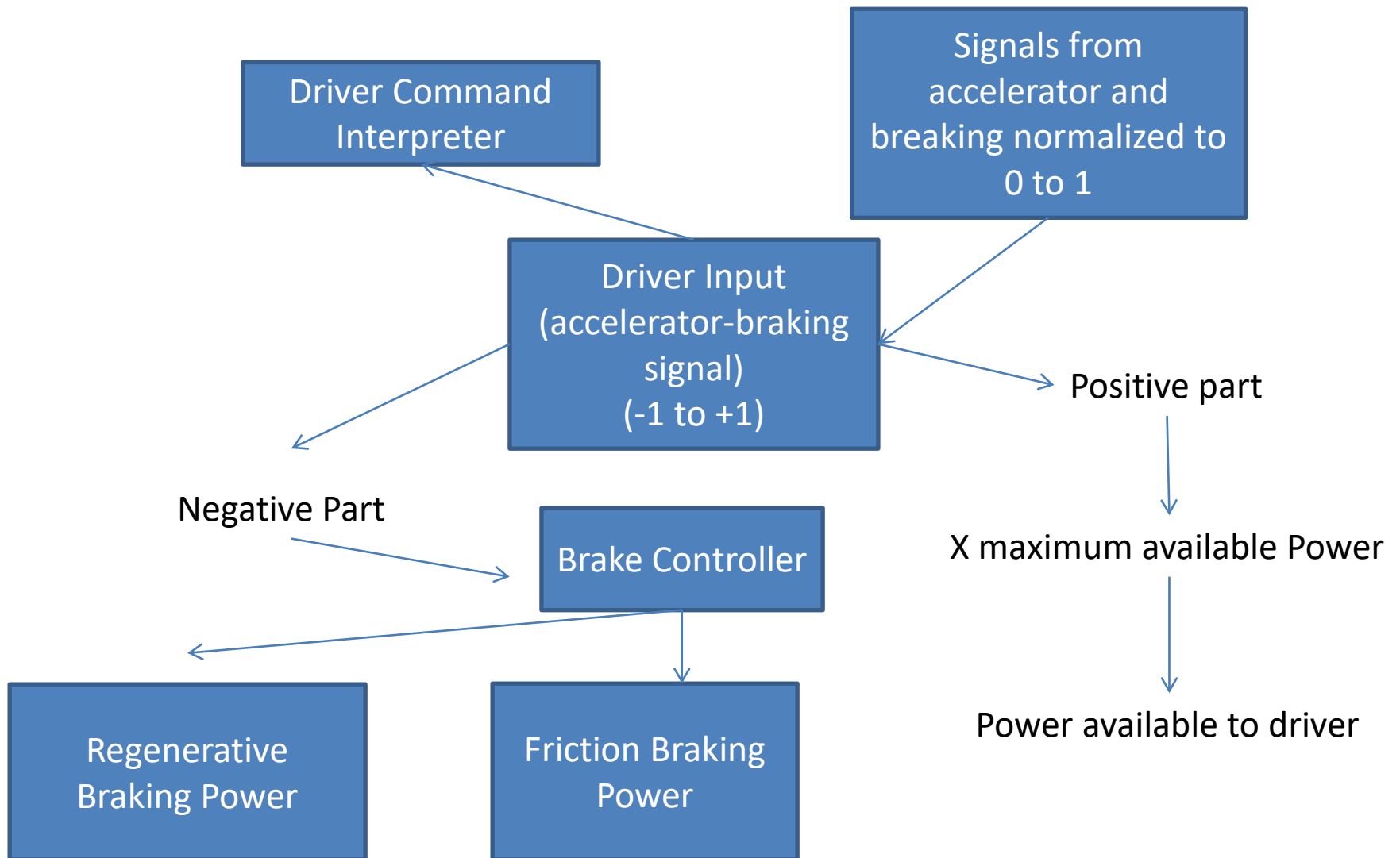
# Membership Functions



## STEPS

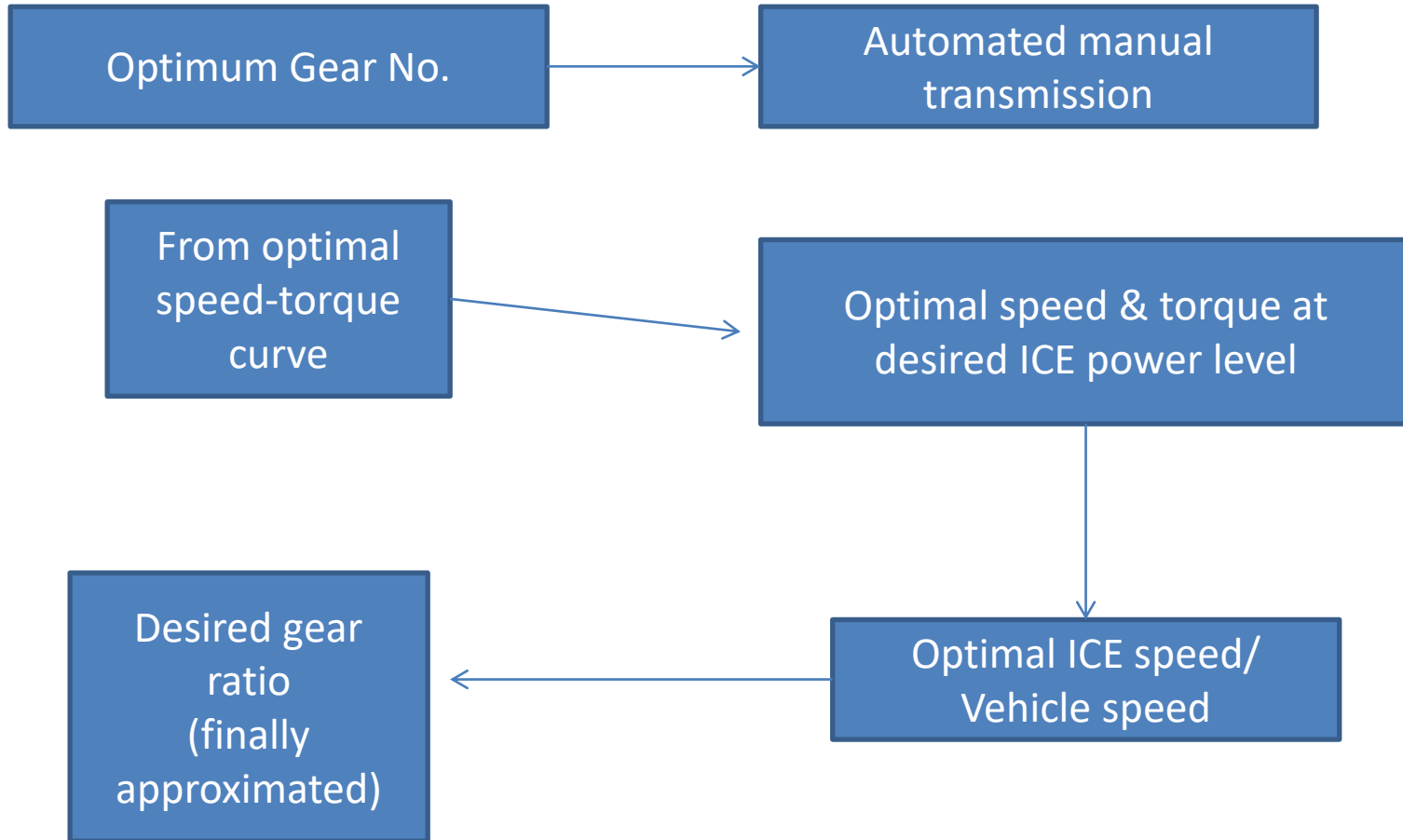


## B.Power Controller



Cannot exceed 65% of the total braking power

## C. Gear Shifting Control





Mathematical Model for

a) Vehicle speed

b) Power required

# Topics Covered

- 1) General description of vehicle movement
- 2) Vehicle resistance
- 3) Dynamic equation
- 4) Tire Ground Adhesion

# AIM

- Fundamental: Apply Newton's second law  
Acceleration of object  $\propto$  Net external force.
- Acceleration of the Vehicle depends on:
  - 1) Power delivered by the propulsion unit
  - 2) Road conditions
  - 3) Aerodynamics of the vehicle
  - 4) Composite mass of the vehicle

# General description of vehicle movement

- Forces acting are
  - 1) Tractive force ( $F_t$ ) - produced by the power plant of the vehicle.
- Resistive forces are
  - 1) Rolling resistance
  - 2) Aerodynamic drag
  - 3) Uphill resistance

$$\frac{dV}{dt} = \frac{\sum F_t - \sum F_{resistance}}{\delta M}$$

where

$V$  = vehicle speed

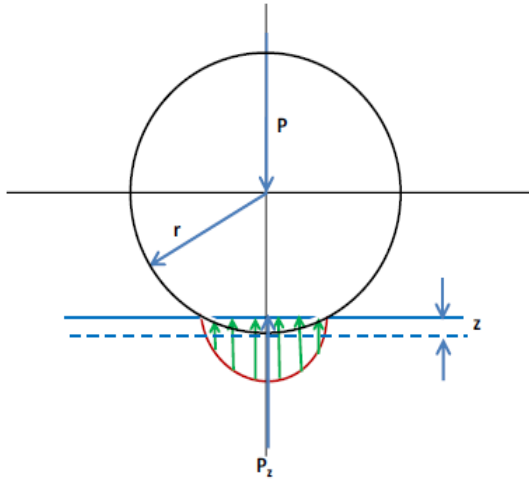
$\sum F_t$  = total tractive effort [ $Nm$ ]

$\sum F_{resistance}$  = total resistance [ $Nm$ ]

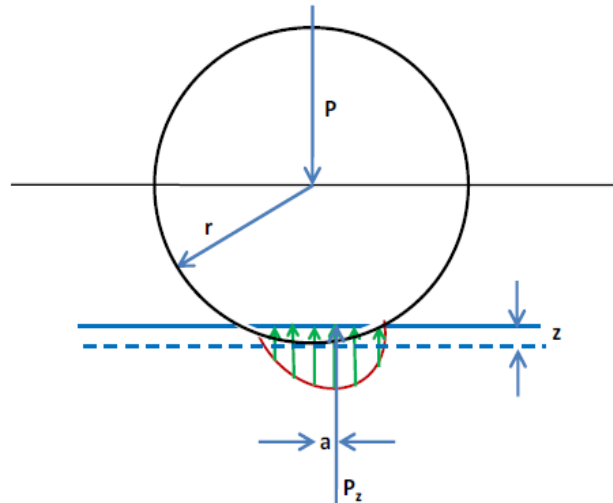
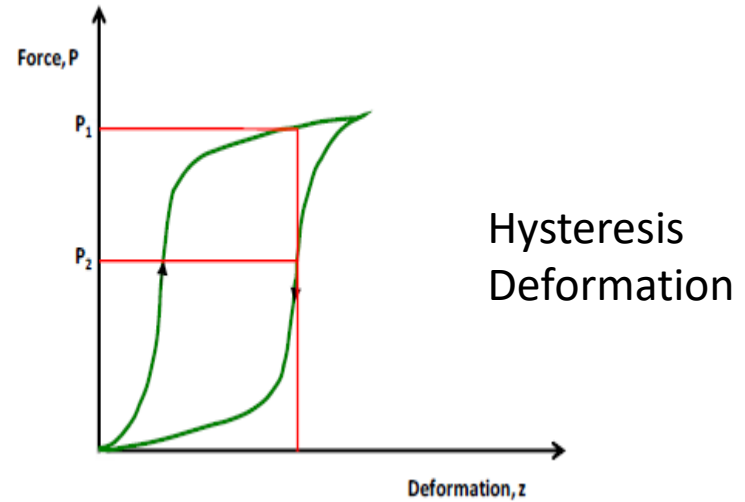
$M$  = total mass of the vehicle [ $kg$ ]

$\delta$  = mass factor for converting the rotational inertias of rotating components into translational mass

# Rolling Resistance



Stand-still



Loading & Unloading

- The moment produced by forward shift of the resultant ground reaction force is called rolling resistance moment

$$T_r = Pa = Mga$$

where

$T_r$  = rolling resistance [ $Nm$ ]

$P$  = Normal load acting on  
the centre of the rolling wheel [ $N$ ]

$M$  = mass of the vehicle [ $kg$ ]

$g$  = acceleration constant [ $m / s^2$ ]

$a$  = deformation of the tyre [ $m$ ]

- To keep the wheel rolling, a force  $F_r$ , acting on the center of the wheel is required to balance this rolling resistant moment.

$$F_r = \frac{T_r}{r_{dyn}} = \frac{Pa}{r_{dyn}} = Pf_r$$

where

$T_r$  = rolling resistance [ $Nm$ ]

$P$  = Normal load acting on the centre of the rolling wheel [ $N$ ]

$r_{dyn}$  = dynamic radius of the tyre [ $m$ ]

$f_r$  = rolling resistance coefficient



- Or equivalently expressing it as a horizontal force acting opposite to movement of wheel.

$$F_r = Pf_r$$

where

$P$  = Normal load acting on the centre of the rolling wheel [ $N$ ]

$f_r$  = rolling resistance coefficient

- Suppose we consider the vehicle is going Uphill.

$$F_r = Pf_r \cos(\alpha) = Mgf_r \cos(\alpha)$$

where

$P$  = Normal load acting on the centre of the rolling wheel [ $N$ ]

$f_r$  = rolling resistance coefficient

$\alpha$  = road angle [*radians*]

$F_r$  are given in table (1).

The rolling resistance coefficient,  $F_r$ , is a function of:  
a) Tire material ,b) Tire structure ,c) Tire temperature  
d) Tire inflation pressure etc.

The rolling resistance coefficient of a passenger car on a concrete road may be calculated as:

$$f_r = f_0 + f_s \left( \frac{V}{100} \right)^{2.5}$$

For most common range of inflation pressure, the following equation can be used for a passenger car on a concrete road

$$f_r = 0.01 \left( 1 + \frac{V}{160} \right)$$

where

$V$  = vehicle speed [km / h]

# Aerodynamic Drag

1) Shape drag

2) Skin effect

$$F_w = \frac{1}{2} \rho A_f C_D V^2$$

where

$\rho$  = density of air [ $kg / m^3$ ]

$A_f$  = vehicle frontal area [ $m^2$ ]

$V$  = vehicle speed [ $m / s$ ]

$C_D$  = drag coefficient

$C_D$  and  $A_f$  in table(2)

# Grading Resistance

- When a vehicle goes up or down a slope, its weight produces a component of force that is always directed downwards. This force component opposes the forward motion, i.e. the grade climbing.

$$F_g = Mg \sin(\alpha)$$

where

$M$  = mass of vehicle [kg]

$g$  = acceleration constant [ $m / s^2$ ]

$\alpha$  = road angle [radians]

- In some literature, the tire rolling resistance and the grading resistance taken together and is called **road resistance**. The road resistance is expressed as

$$F_{rd} = F_f + F_g = Mg(f_r \cos(\alpha) + \sin(\alpha))$$

# Acceleration resistance

$$F_a = \left( M + \frac{\sum J_{rot}}{r_{dyn}^2} \right) \frac{dV}{dt}$$

where

$M$  = mass of vehicle [kg]

$J_{rot}$  = inertia of rotational components [ $kg \times m^2$ ]

$V$  = speed of the vehicle [km / h]

$r_{dyn}$  = *dynamic radius of the tyre* [m]

- Or equivalently

$$F_a = \lambda M \frac{dV}{dt}$$

where

$\lambda$  = rotational inertia constant

$M$  = mass of the vehicle [ $kg$ ]

$V$  = speed of the vehicle [ $m / s$ ]



- Total driving resistance

$$F_{\text{resistance}} = F_r + F_w + F_g + F_a$$

- Substituting with the expressions

$$F_{\text{resistance}} = Mgf_r \cos(\alpha) + \frac{1}{2} \rho A_f C_D V^2 + Mg \sin(\alpha) + \lambda M \frac{dV}{dt}$$

- Power required (**P<sub>req</sub>**)

$$P_{\text{req}} = F_{\text{resistance}} V$$

# Dynamic equation

$$M \frac{dV}{dt} = (F_{\text{th}} + F_{\text{tr}}) - (F_{\text{rf}} + F_{\text{rr}} + F_{\text{w}} + F_{\text{g}} + F_{\text{a}})$$

# Adhesion, Dynamic wheel radius and slip

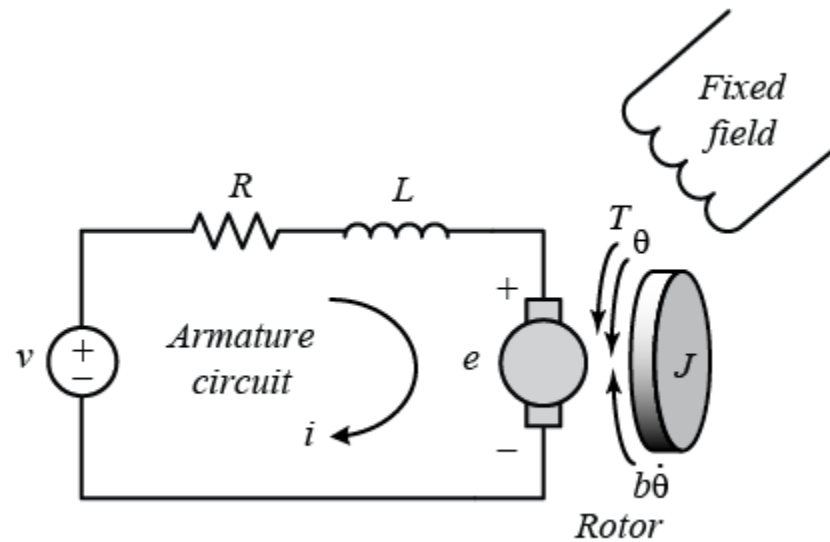
- Tractive effort of a vehicle > maximum tractive effort limit
- Results in “spinning of wheels”
- The slip between the tires and the surface can be described as:

$$\text{drive slip } S_T = \frac{\omega_R r_{dyn} - V}{\omega_R r_{dyn}}$$

- The dynamic wheel radius ( $r_{dyn}$ ) is calculated from the distance travelled per revolution of the wheel, rolling without slip.
- Dynamic wheel radius of common tire sizes in table(4).

# Mathematical Modeling of Electric Motor

# Basic Diagram



# Equations Involved

$$T = K_t i$$

$$e = K_e \dot{\theta}$$

$$J\ddot{\theta} + b\dot{\theta} = K i$$

$$L \frac{di}{dt} + Ri = V - K \dot{\theta}$$

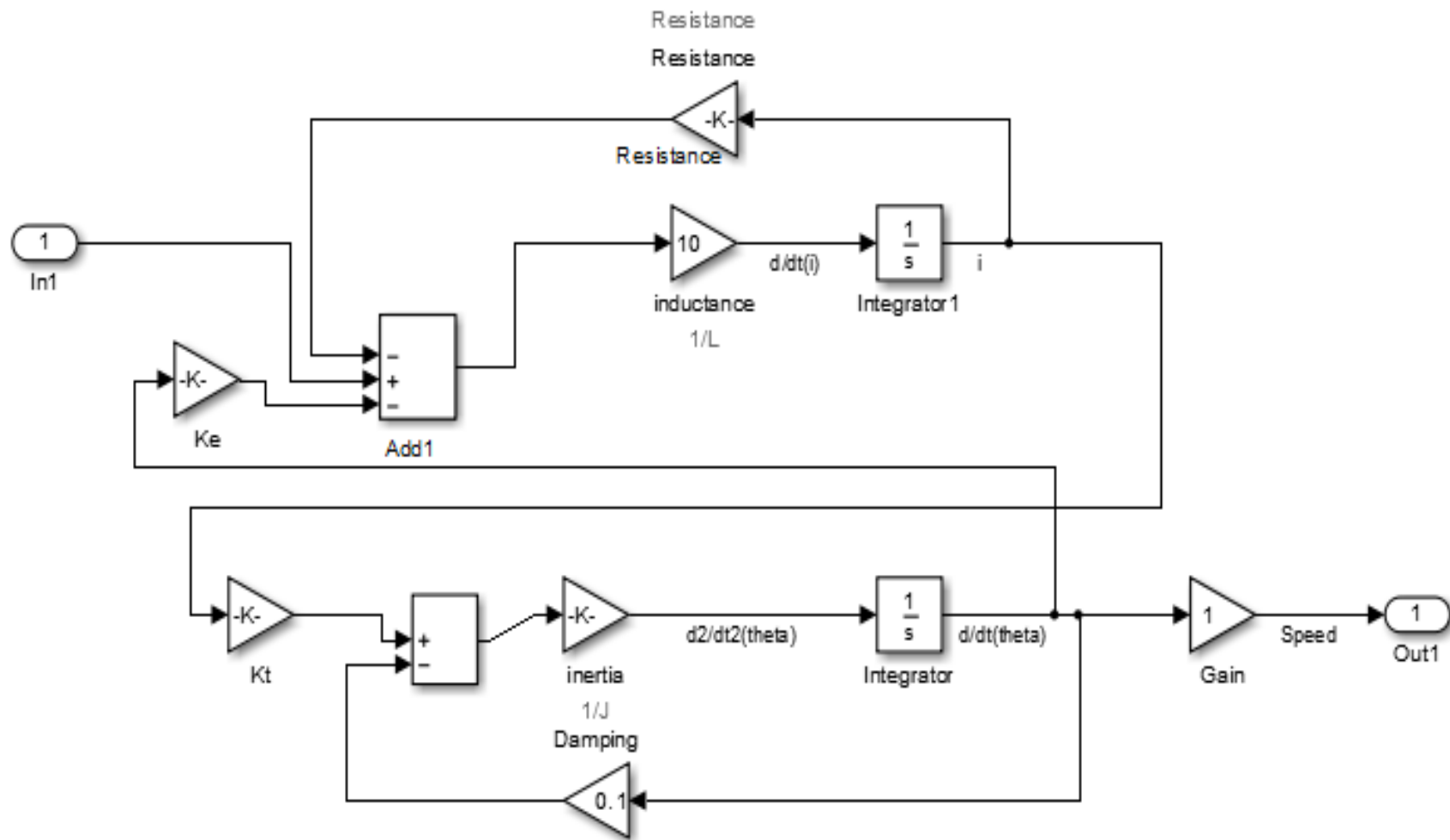
# Laplace Transform & Transfer Function

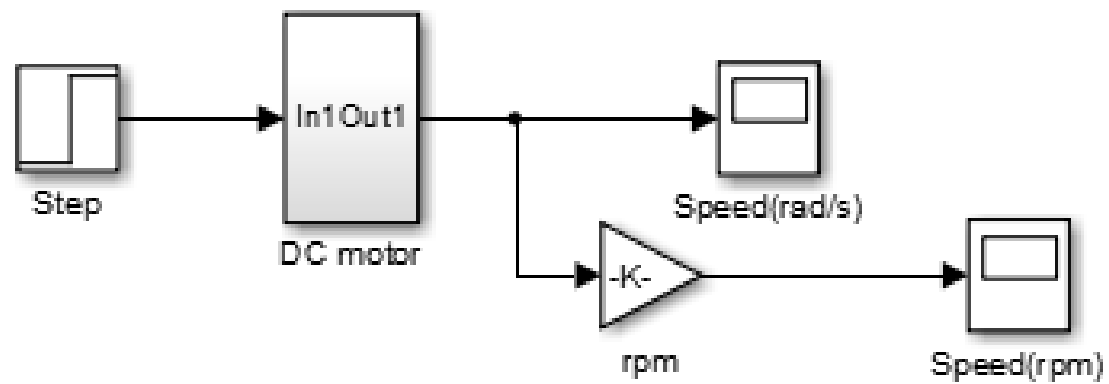
$$s(Js + b)\Theta(s) = KI(s)$$

$$(Ls + R)I(s) = V(s) - Ks\Theta(s)$$

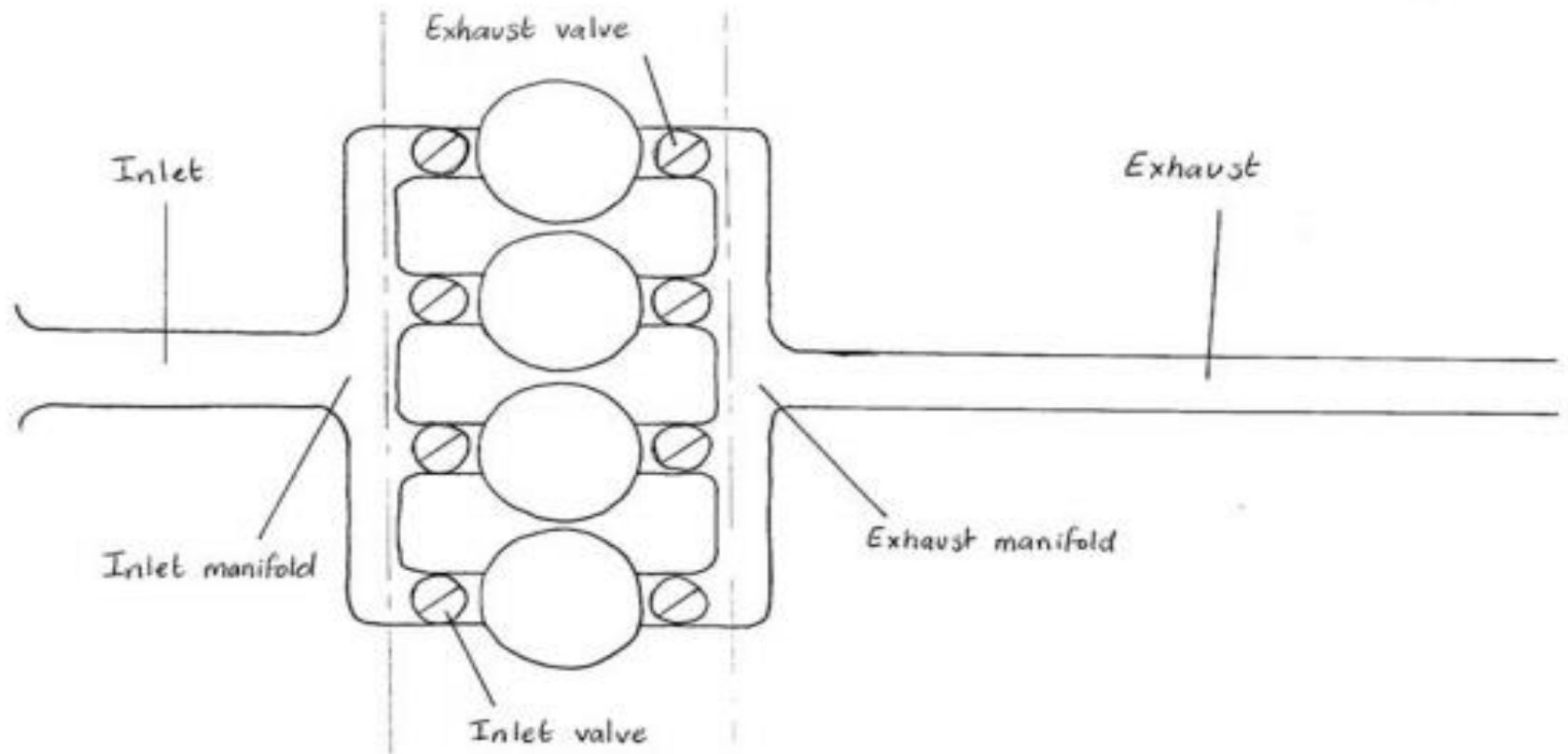
$$P(s) = \frac{\dot{\Theta}(s)}{V(s)} = \frac{K}{(Js + b)(Ls + R) + K^2} \quad \left[ \frac{\text{rad/sec}}{V} \right]$$







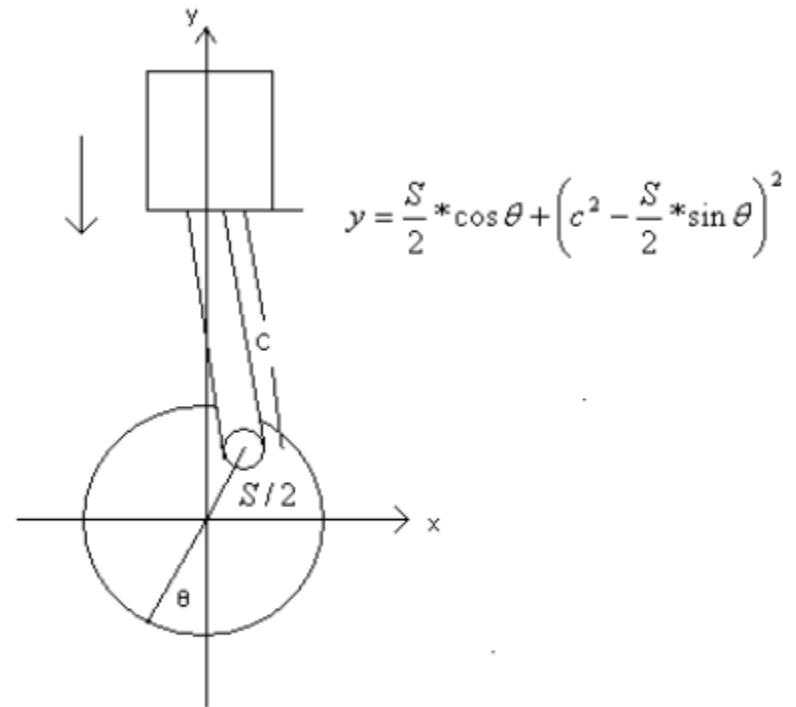
One dimensional modeling  
of an internal combustion engine.



**Fig 1. Model of the engine**

# Sub-models

- 1. Piston Velocity



**Fig. 2 Side view of piston**

$$\dot{y}(\theta) = \frac{S}{2} * \sin \theta \left[ -1 - \frac{S * \cos \theta}{2 * \sqrt{L_c^2 - \frac{S^2 * \sin^2 \theta}{4}}} \right] \dot{\theta}$$

$$v_{p\_max} \Rightarrow \theta = \frac{\pi}{2} \Rightarrow |v_{p\_max}| = \frac{S}{2} * \dot{\theta}$$

$$\dot{\theta} = \frac{rpm * \pi}{30} \Rightarrow v_{p\_max} = \frac{S * \pi * rpm}{60}$$

# Incompressible flow

$$u_{ip\_max} * A_{ip} = v_{p\_max} * A_p$$

$$u_{ip\_max} = v_{p\_max} * \left( \frac{B}{d_{ip}} \right)^2$$

$$rpm = \frac{M * a * 60}{S * \pi} * \left( \frac{d_{ip}}{B} \right)^2$$

$$rpm = 752$$

# Compressible flow

$$P * V = m * R * T$$

$$V_c = \frac{\pi * B^2 * S}{4}$$

$$m_{in} = \frac{P_{atm} * \pi * B^2 * S}{4 * R * T_{atm}} = 5.99 * 10^{-4} \text{ kg}$$



$$t_{open} = (180^0) = \left( \frac{rpm}{60} \right)^{-1} * 0.5 = \frac{30}{rpm} \text{sec}$$

$$\dot{m}_{in} = \frac{5.99 * 10^{-4} * rpm}{30} = 2.00 * 10^{-5} * rpm \text{ kg} * s^{-1}$$

$$\begin{aligned} \dot{m}_{in} &= \rho * u_{ip} * A_{ip} = \rho * M * a * A_{ip} = \rho * M * \sqrt{\gamma * R * T} * A_{ip} = \\ &= \frac{\rho}{\rho_0} * \rho_0 * M * \sqrt{\gamma * R} * \sqrt{\frac{T}{T_0}} * \sqrt{T_0} * A_{ip} \end{aligned}$$

$$\therefore \dot{m}_{in} = \rho_0 * \sqrt{\gamma * R * T_0} * A_{ip} * \frac{\rho}{\rho_0} * \left( \frac{T}{T_0} \right)^{\frac{1}{2}} * M$$

$$\frac{\rho}{\rho_0}=\left[1+\frac{1}{2}(\gamma-1)M^2\right]^{\frac{-1}{\gamma-1}} \& \frac{T}{T_0}=\left[1+\frac{1}{2}(\gamma-1)M^2\right]^{-1}$$

$$\dot{m}_in=\rho_0*\sqrt{\gamma*R*T_0}*A_{ip}*\left[1+\frac{1}{2}(\gamma-1)M^2\right]^{\frac{-1}{\gamma-1}-\frac{1}{2}}$$

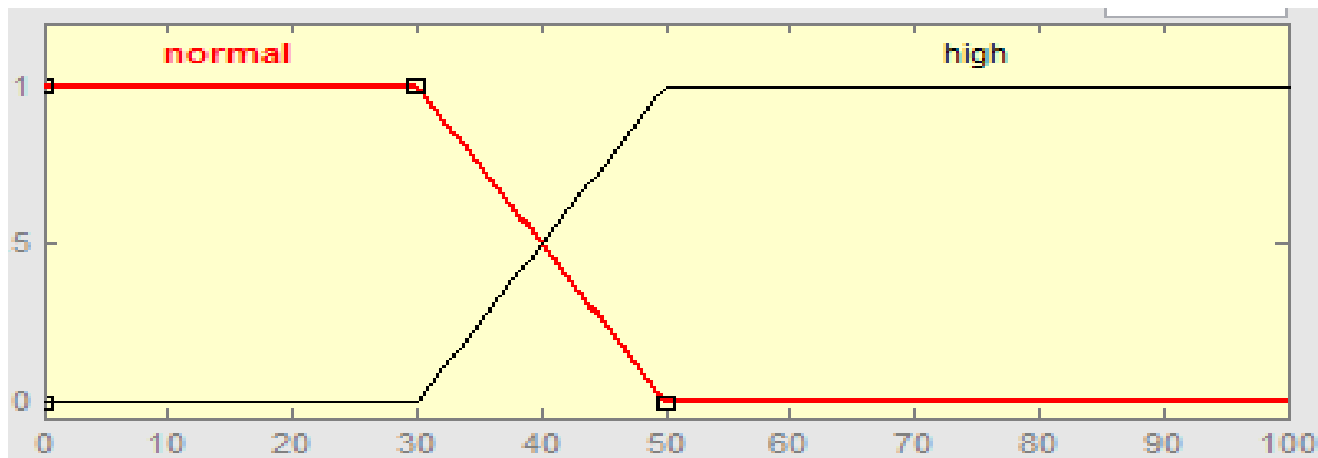
$$8.484*10^{-5}*rpm=M*[1+0.2M^2]^{-3}$$

# Exhaust flow

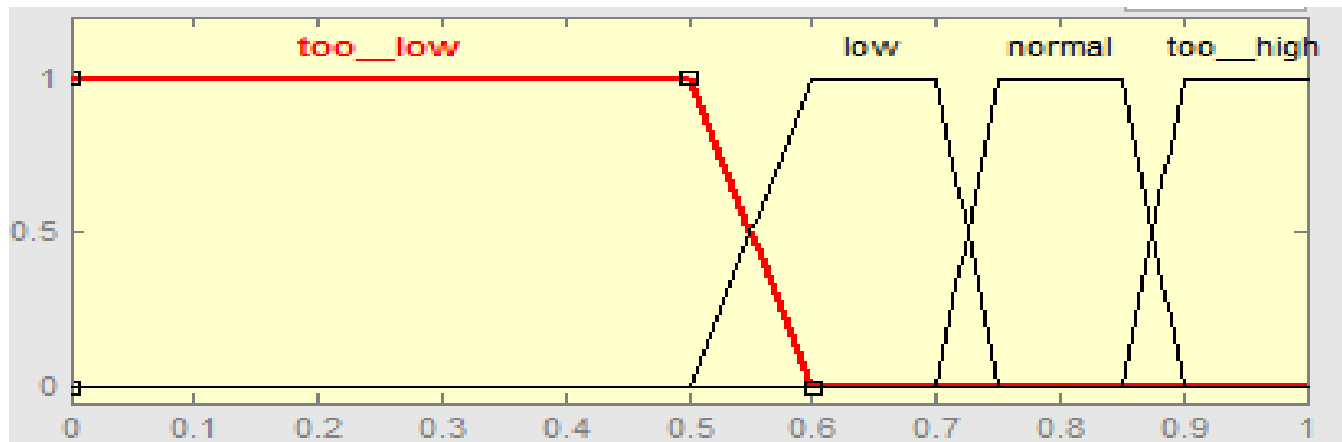
$$1.1701 \times 10^{-5} * rpm = M * \left[ 1 + 0.2M^2 \right]^{-3}$$

# Fuzzy Logic Controller

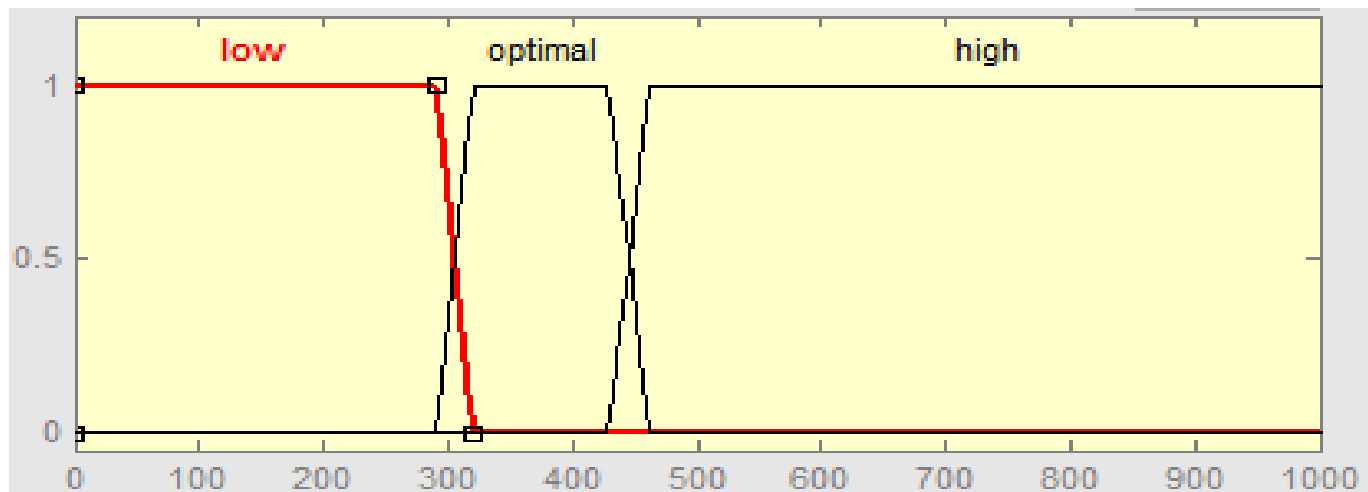
- Inputs:-



1) Driver Power Command (kW)



2)State of Charge (SOC)



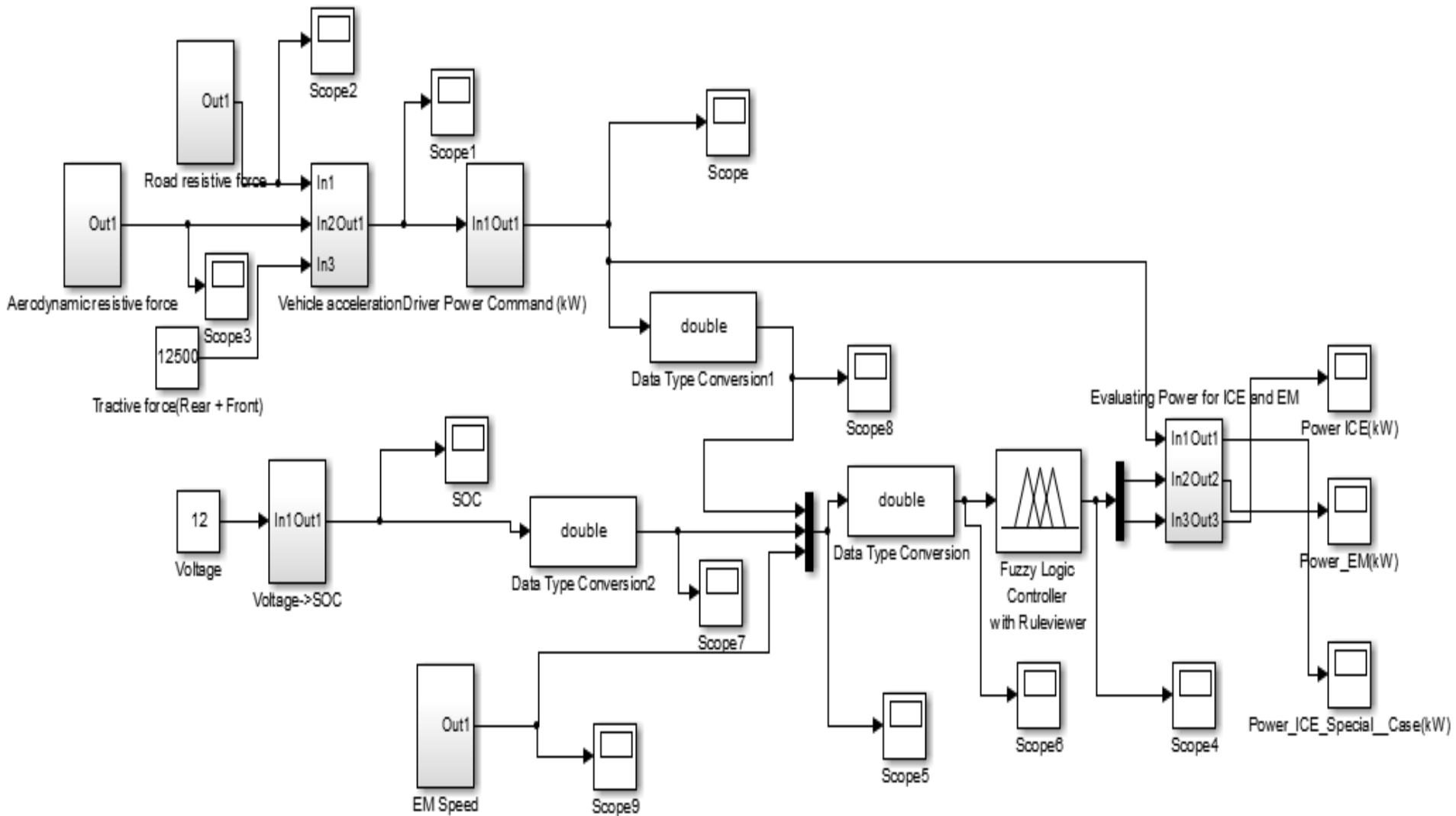
3)EM Speed

# Rule Base

## RULE BASE OF THE FUZZY LOGIC CONTROLLER

- 
- 1    **If SOC is too high then  $P_{\text{gen}}$  is 0 kW**
  - 2    **If SOC is normal and  $P_{\text{driver}}$  is normal and  $\omega_{\text{EM}}$  is optimal then  $P_{\text{gen}}$  is 10 kW**
  - 3    **If SOC is normal and  $\omega_{\text{EM}}$  is not optimal then  $P_{\text{gen}}$  is 0 kW**
  - 4    **If SOC is low and  $P_{\text{driver}}$  is normal and  $\omega_{\text{EM}}$  is low then  $P_{\text{gen}}$  is 5 kW**
  - 5    **If SOC is low and  $P_{\text{driver}}$  is normal and  $\omega_{\text{EM}}$  is not low then  $P_{\text{gen}}$  is 15 kW**
  - 6    **If SOC is too low then  $P_{\text{gen}}$  is  $P_{\text{gen,max}}$**
  - 7    **If SOC is too low then scale factor is 0**
  - 8    **If SOC is not too low and  $P_{\text{driver}}$  is high then  $P_{\text{gen}}$  is 0 kW**
  - 9    **If SOC is not too low then scale factor is 1**
-

# Simulink Model



# Example

- Inputs:-
  - 1) Tractive Force (rear + front) = 12500W
  - 2) Voltage (Battery)=12V
- Outputs:-
  - 1) Power \_ ICE = 20.2417 kW
  - 2) Power \_ EM = -7.5 kW