



SAFARI

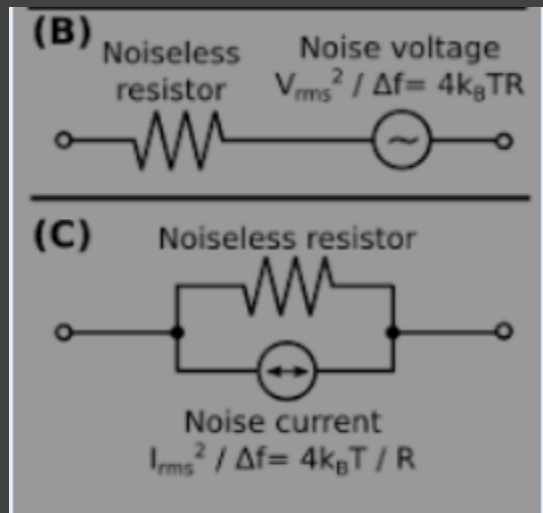
Development of the FDM Baseband Feedback

I. FEE Noise Model

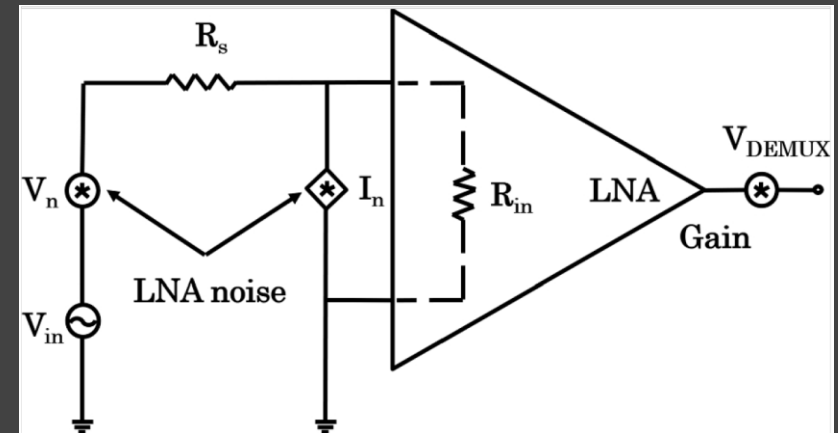
SRON

Amin Aminaiei, 28 September 2020

FEE Model



Johnson–Nyquist noise...
en.wikipedia.org

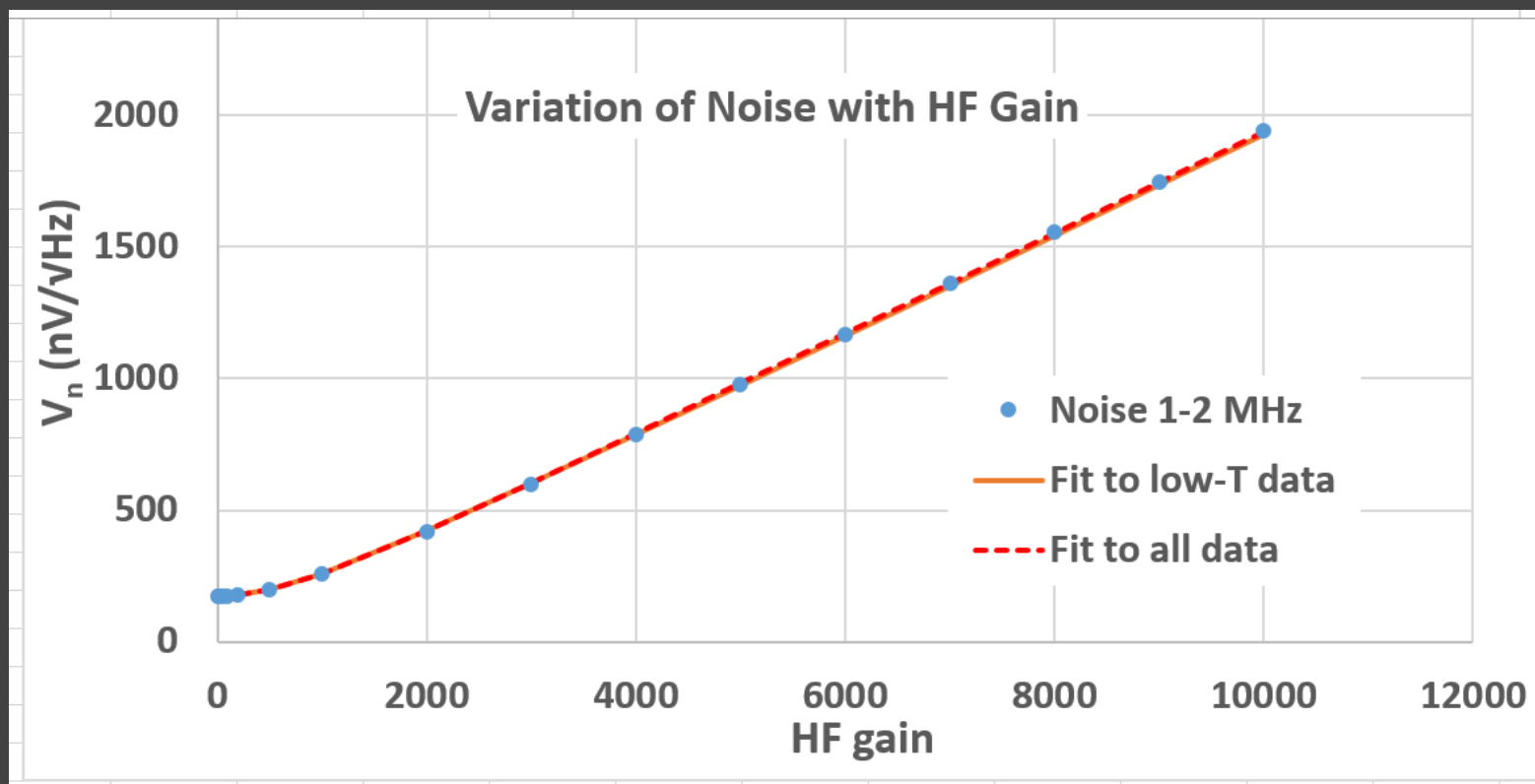


LNA: $V_n = 315 \text{ pV}/(\text{Hz})^{0.5}$
 $I_n = 5.4 \text{ pA}/(\text{Hz})^{0.5}$
 DEMUX $V_n = 173 \text{ nV}/(\text{Hz})^{0.5}$

Wang et al., 2020

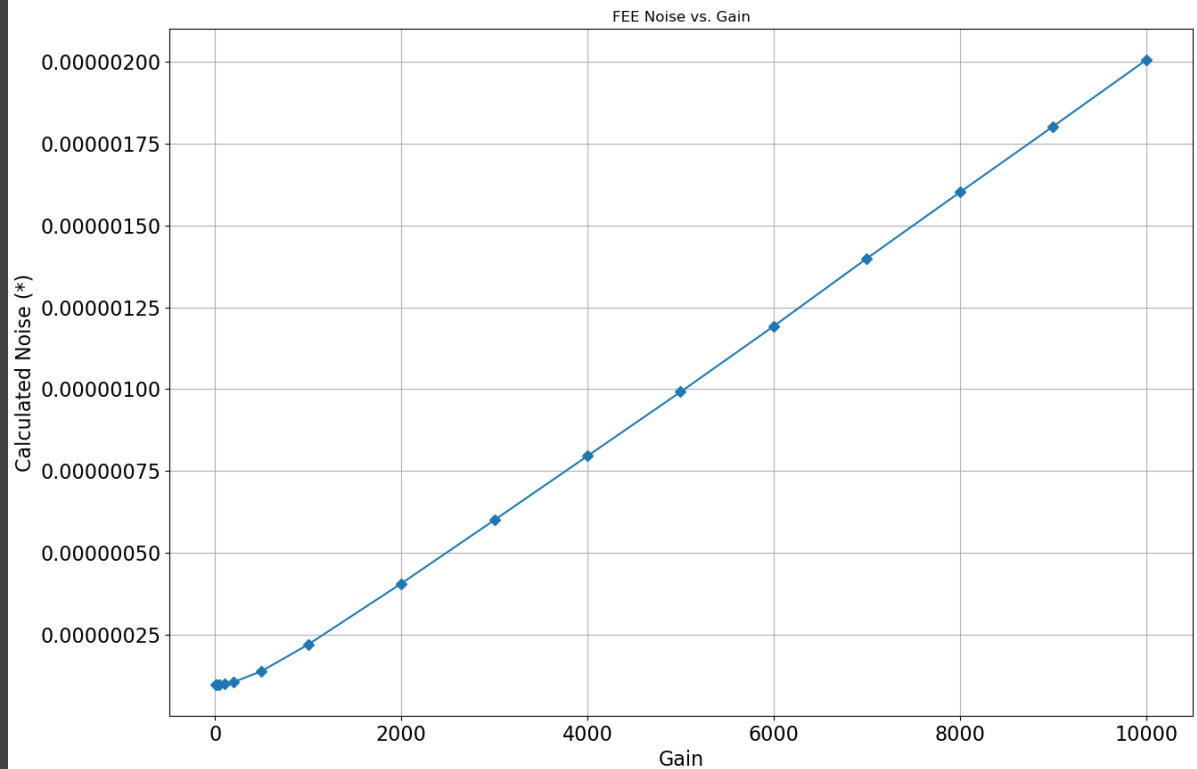
FEE7 Bandwidth is ~ 38.75 MHz, (Test Procedure FEE-7, SRON report, D. Boersma, 2014)
 Analysis is initially done in FDM range

Measured Noise of FEE versus Gain.



$R_{in} = 129 \text{ Ohm}$, $R_s = 91.6 \text{ Ohm}$, $T = 1.3 \text{ K to } 4 \text{ K}$

$T=1.3K-3.5K$
 $Gain=10,100,1000,10000$
 (Test Points for LT-Spice)
 $R_{in}=129 \text{ Ohm}$
 $R_s=91.6 \text{ Ohm}$
 $I_n=5.4pA/rt.(Hz)$
 $V_n=315pV/rt.(Hz)$
 $V_{n.Demux}=173nV/rt.(Hz)$
 $k_B=\text{Boltzmann constant}$
 $(1.38e-23)$



If $R_{lead} \sim 0$

$$V_{Model}^2 = V_{n.Demux}^2 + Gain^2 (I_n^2 \cdot R_s^2 + V_n^2 + 4 \cdot k_B \cdot T \cdot R_s) \cdot (R_{in}/(R_{in} + R_s))^2$$

$$V_{Model}^2 = V_{n.Demux}^2 \text{ (Noise DEMUX) +}$$

$$Gain^2 (I_n^2 \cdot R_s^2) \cdot (R_{in}/(R_{in} + R_s))^2 \text{ (FEE Current Noise) +}$$

$$Gain^2 (V_n^2) \cdot (R_{in}/(R_{in} + R_s))^2 \text{ (FEE Voltage Noise) +}$$

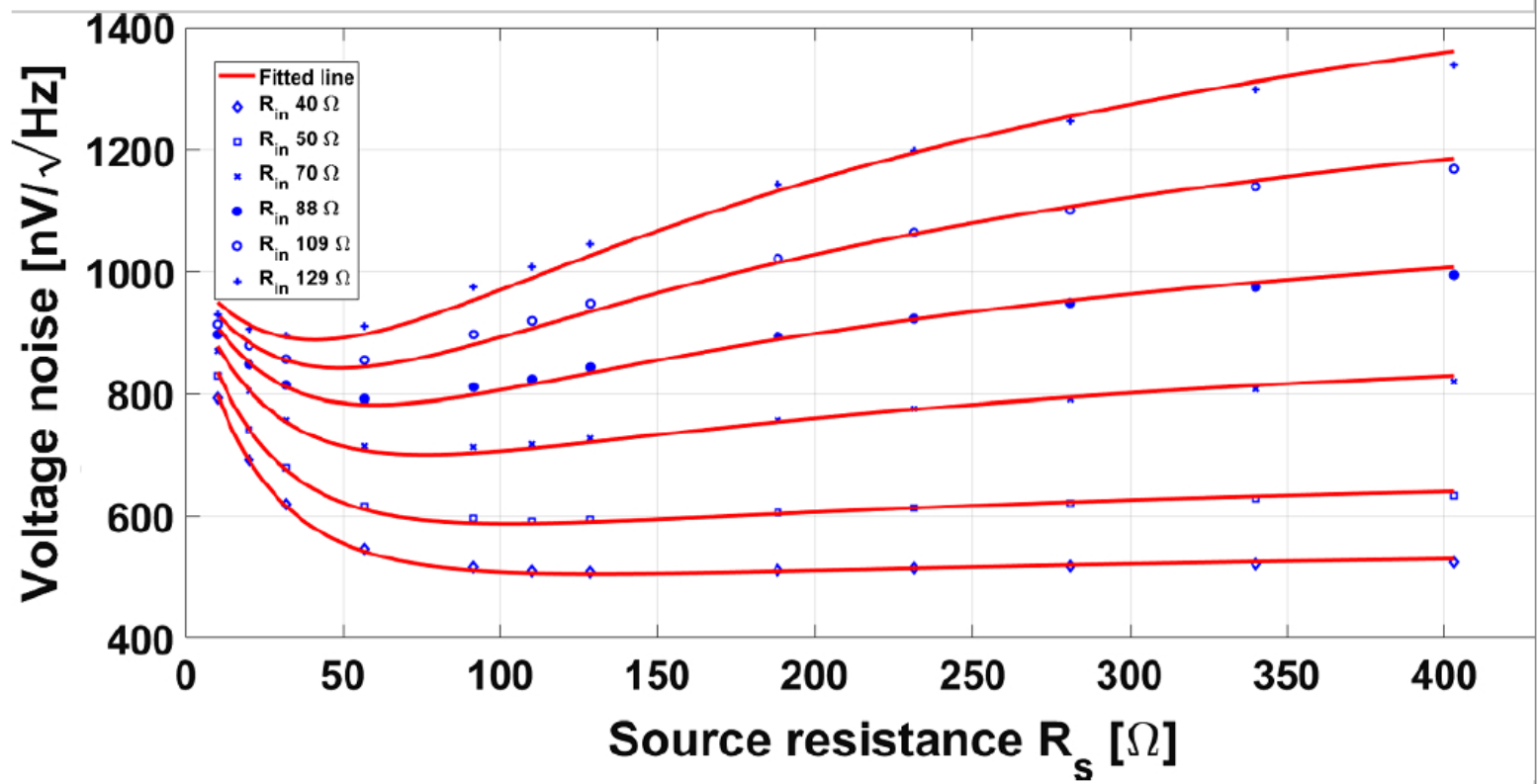
$$Gain^2 (4 \cdot k_B \cdot T \cdot R_s) \cdot (R_{in}/(R_{in} + R_s))^2 \text{ (Rs Noise)}$$

Noise vs. R_{in} , R_s

FEE which has 74-dB gain (5000) in the range 1–5 MHz and active input impedance

1/19/2020 e.Proofing

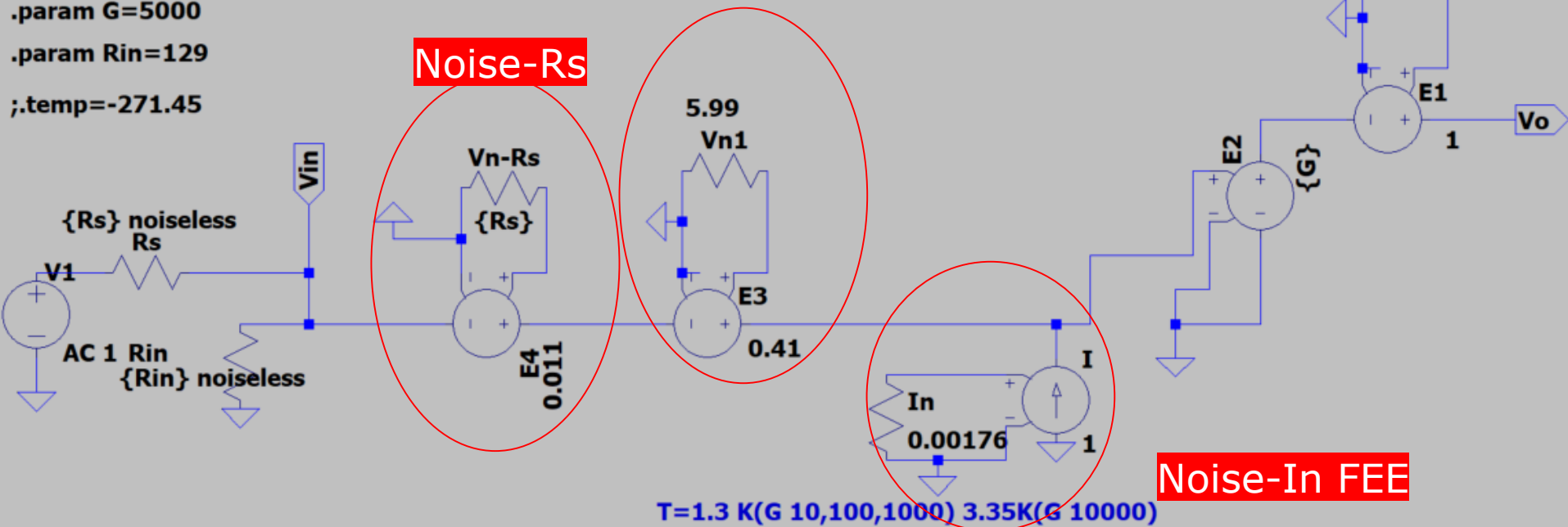
At 1.3 K, the output noise as a function of R_s with different R_{in} . The fitted current noise is $5.4 \pm 0.1 \text{ pA}/\sqrt{\text{Hz}}$, while the fitted voltage noise $315 \pm 10 \text{ pV}/\sqrt{\text{Hz}}$, both identical to the fitted parameters at 50 mK. (Color figure online)

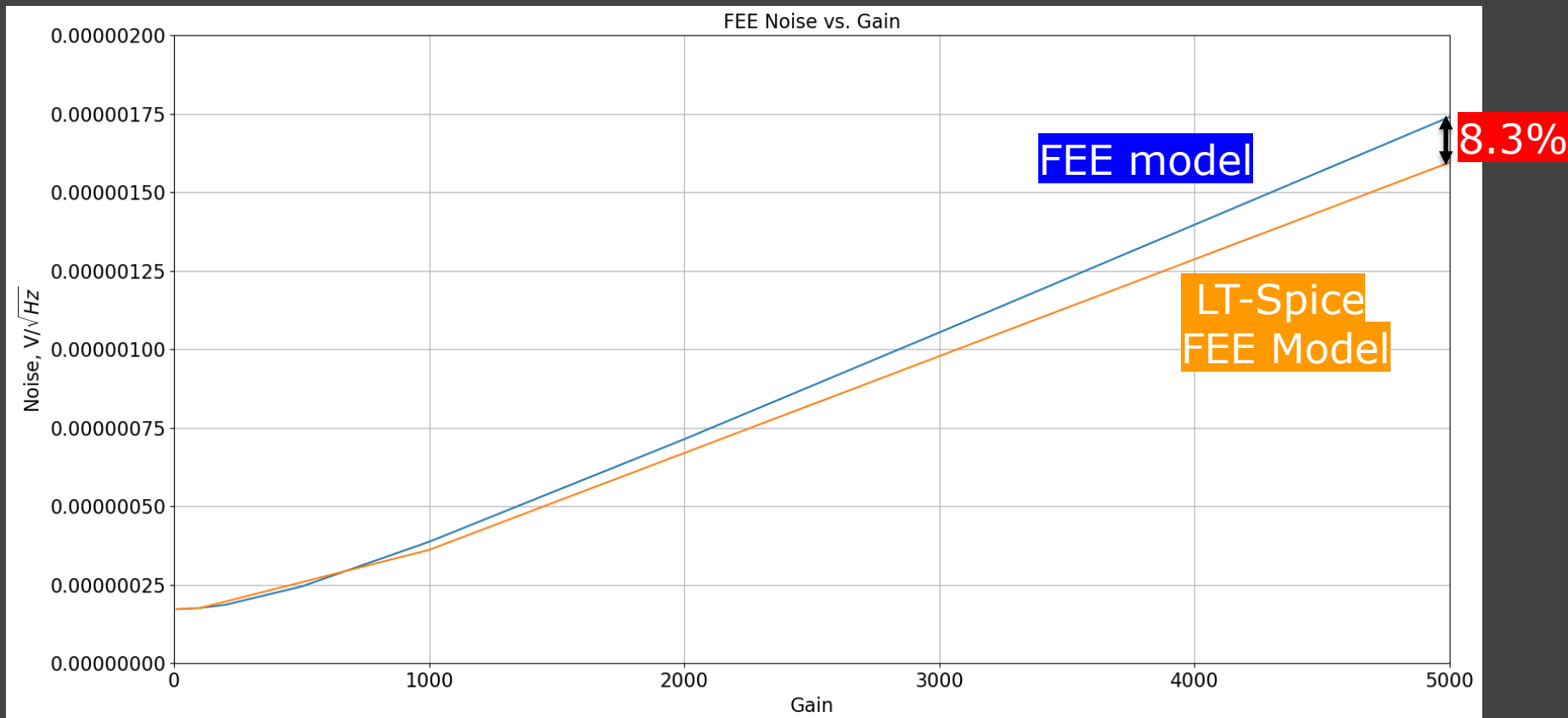


The best fits in Fig. 5 illustrate the identical (within the uncertainty) current noise and the voltage noise of the LNA as what we found from 50 mK data, confirming the model. Thus, we have now derived the noise data of our LNA.

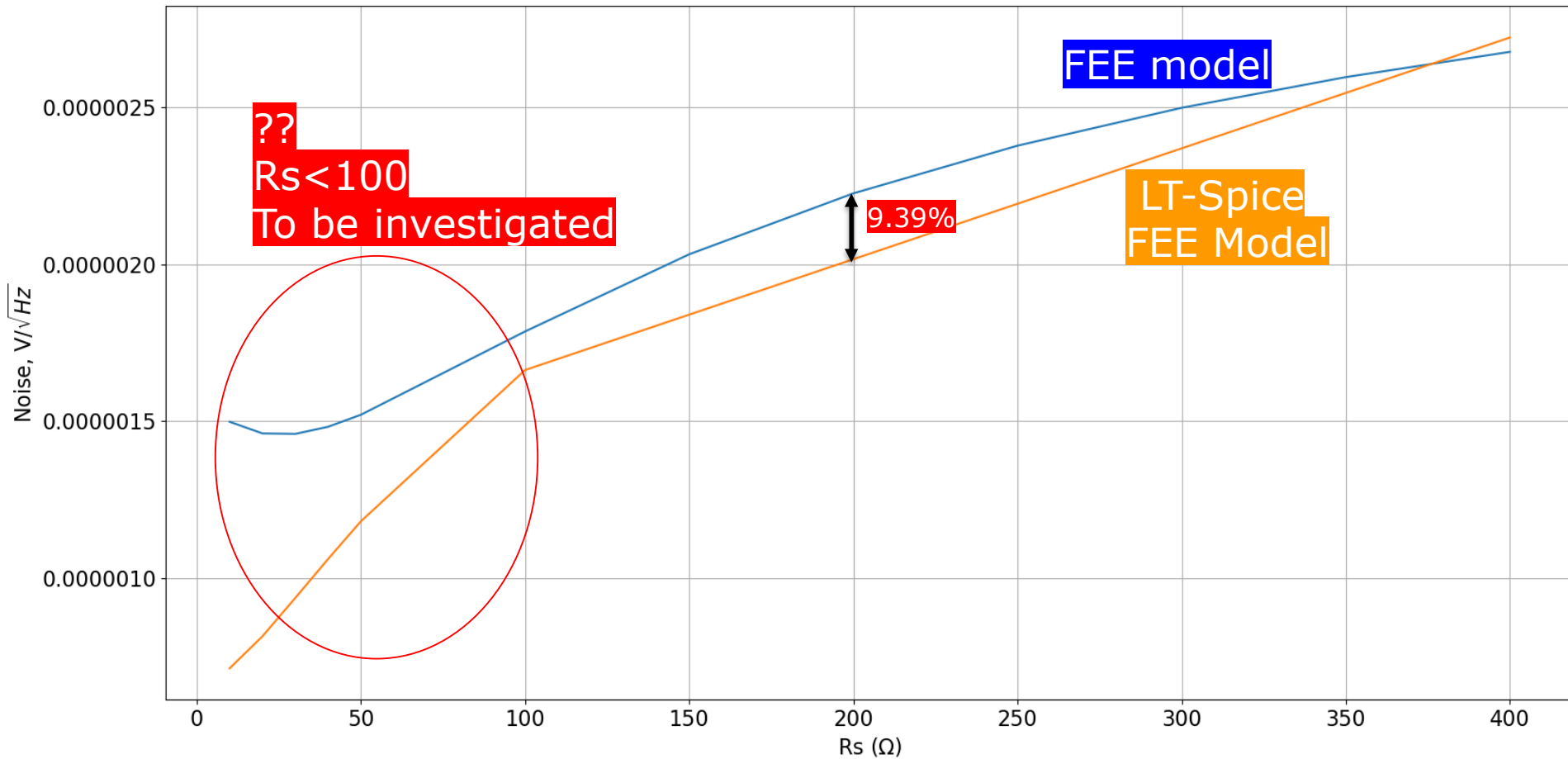
LT-Spice Model

```
.noise V(Vo) V1 oct 1000 1meg 4meg
.step param Rs list 10 50 100 400
.param G=5000
.param Rin=129
;.temp=-271.45
```

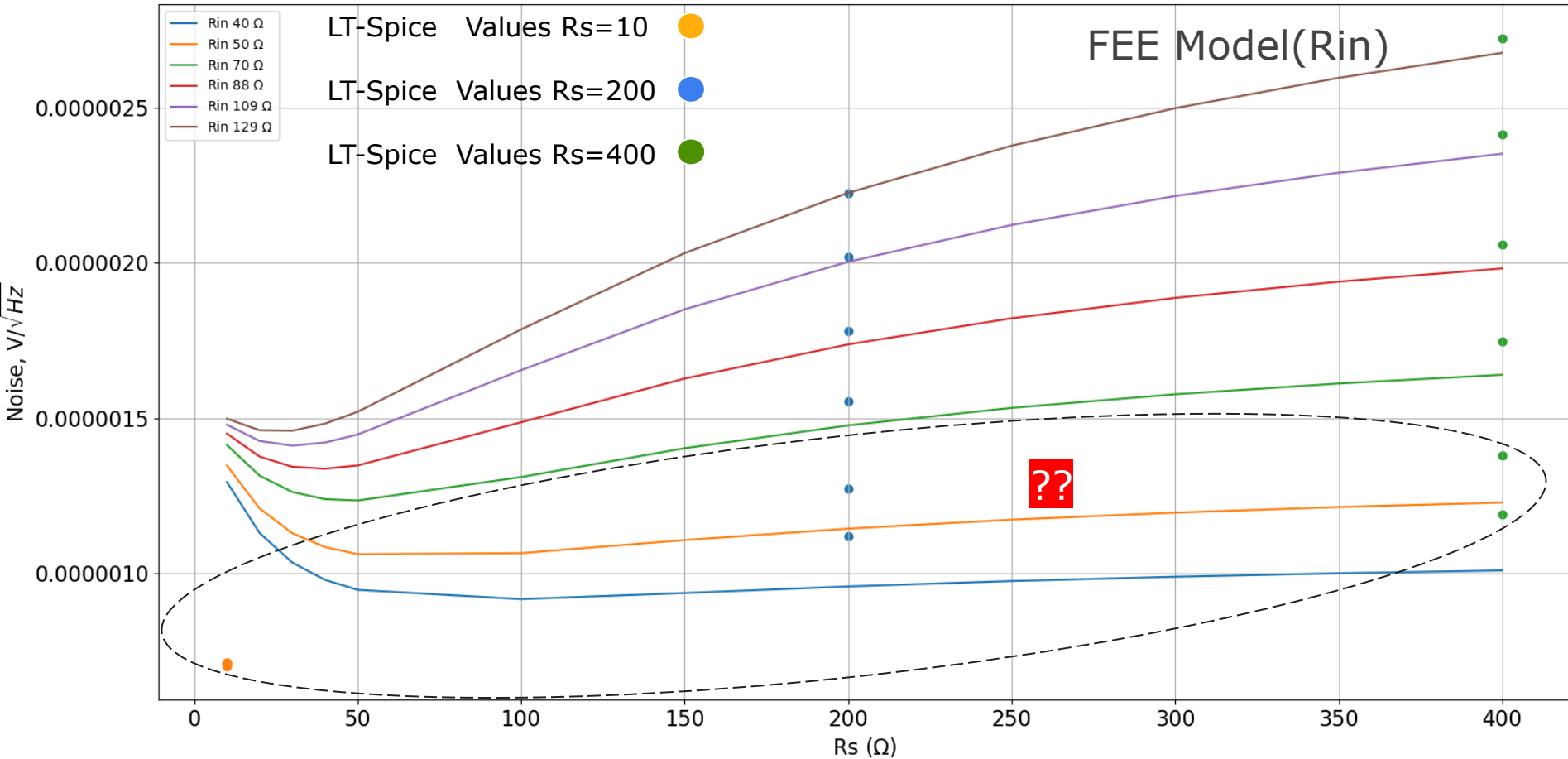




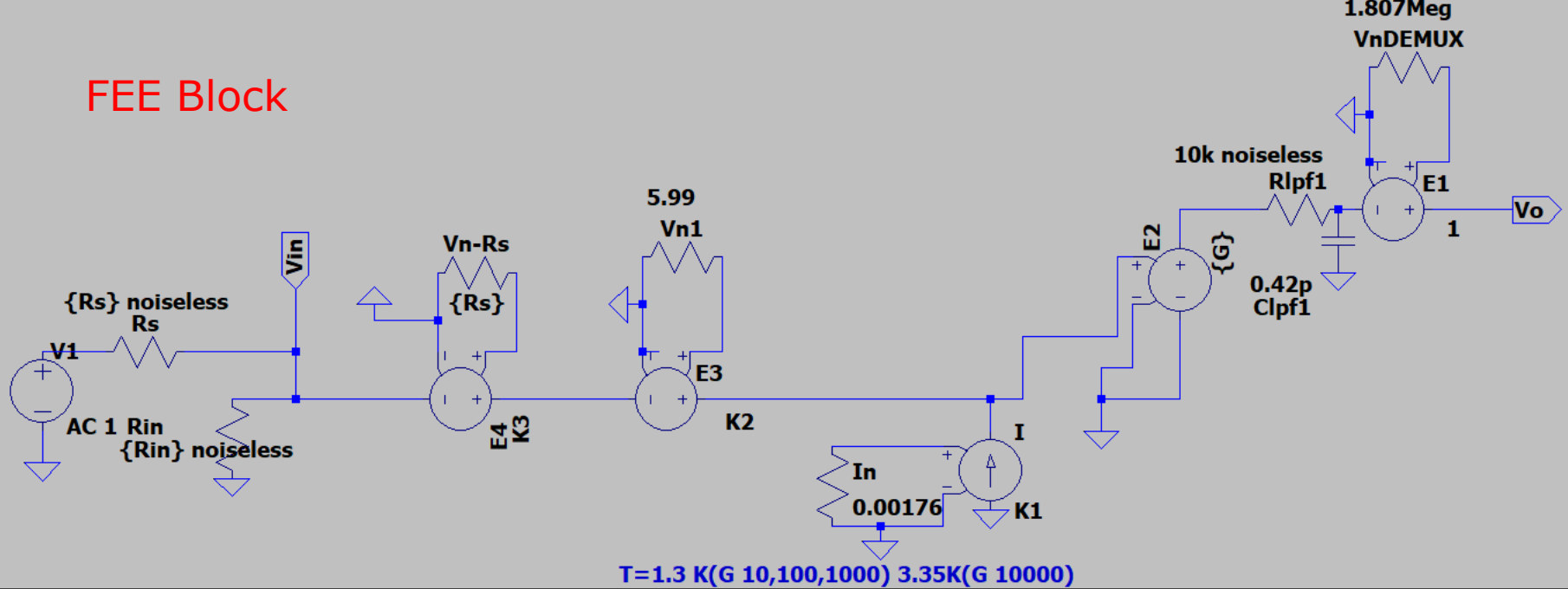
FEE Noise vs. Rs



FEE Noise vs. R_s , R_{in}



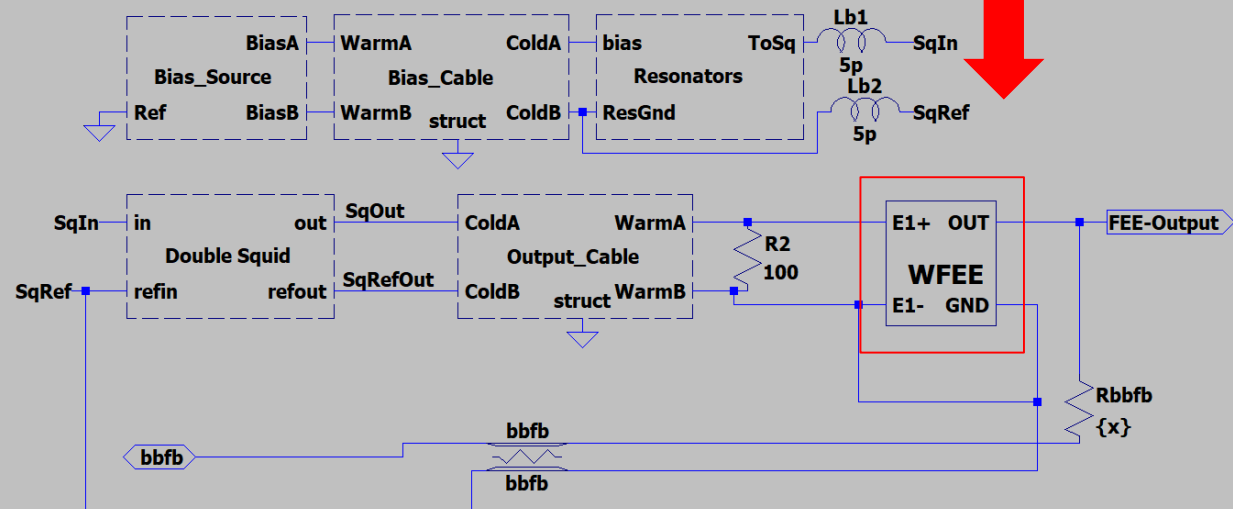
FEE Block



The LTSpice FEE Transformed Noise values ($V_n, I_n, V_{n_{RS}}$) is extracted from the

Noise Model written in Python to match the measurement.

FEE block also includes Vndemux, Gain, Bandwidth, R_s , R_{in} . To be used for FDM BBFB.



- Backup Slides

R_Lead

$$V_{\text{measured}}^2 = V_{\text{Demux}}^2 + \text{Gain}^2 (I_n^2 \cdot R_s^2 + V_n^2 + 4 \cdot k_B \cdot T \cdot (R_s - R_{\text{lead}}) + 4 \cdot k_B \cdot T_{\text{lead}} \cdot R_{\text{lead}}) \cdot (R_{\text{in}} / (R_{\text{in}} + R_s))^2$$

$R_{\text{lead}} = 0.5 \text{ Ohm}$
 $T_{\text{lead}} = 100 \text{ K}$

If $R_{\text{lead}} \sim 0$

(Test points)

$$V_{\text{measured}}^2 = V_{\text{Demux}}^2 + \text{Gain}^2 (I_n^2 \cdot R_s^2 + V_n^2 + 4 \cdot k_B \cdot T \cdot R_s) \cdot (R_{\text{in}} / (R_{\text{in}} + R_s))^2$$

$T = 1.3 \text{ K}$, $\text{Gain} = 5000$, $R_{\text{in}} = 88$, $R_s = 10\text{-}400 \text{ Ohm}$

$I_n = 5.4 \text{ pA}/\sqrt{\text{Hz}}$

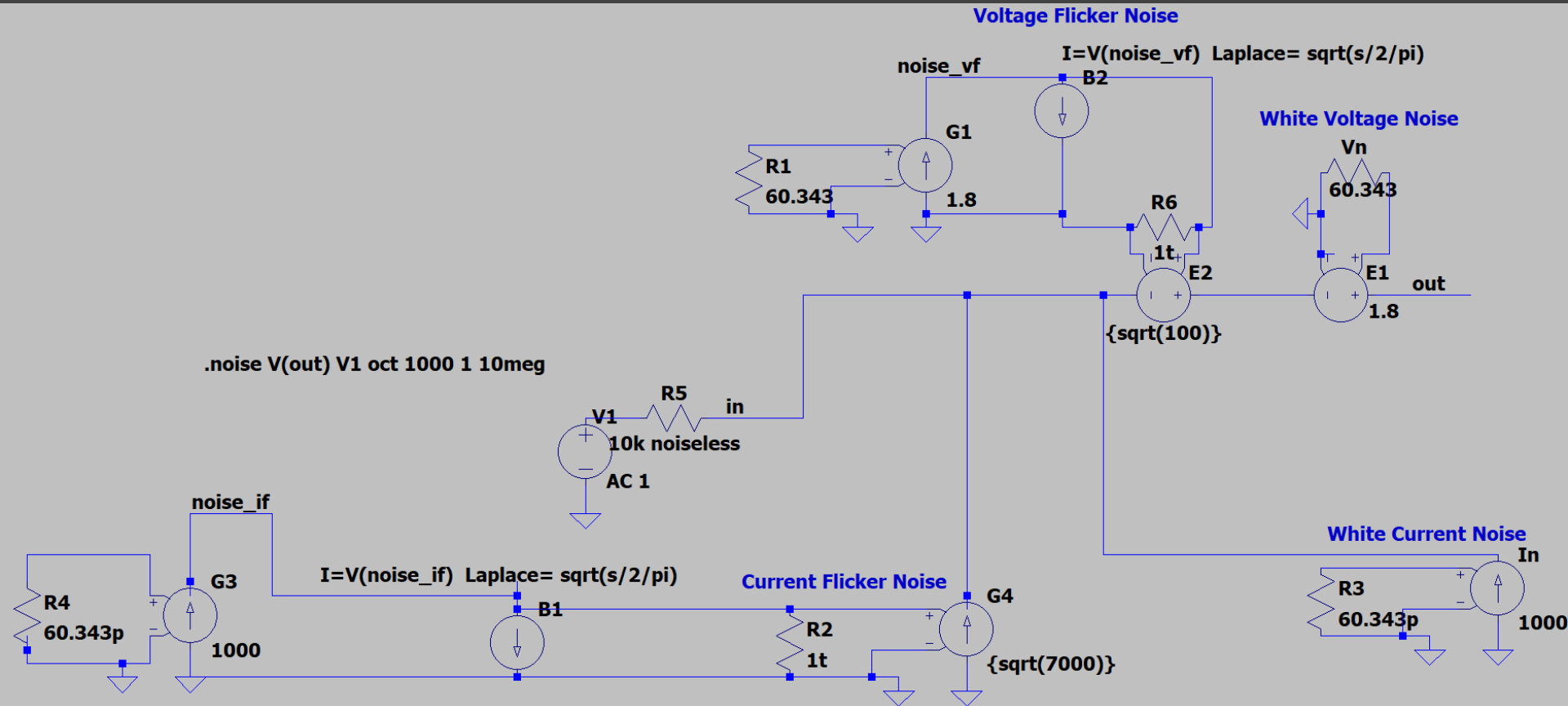
$V_n = 315 \text{ pV}/\sqrt{\text{Hz}}$

$V_{\text{demux}} = 173 \text{ nV}/\sqrt{\text{Hz}}$

k_B = Boltzmann constant

(1.38×10^{-23})

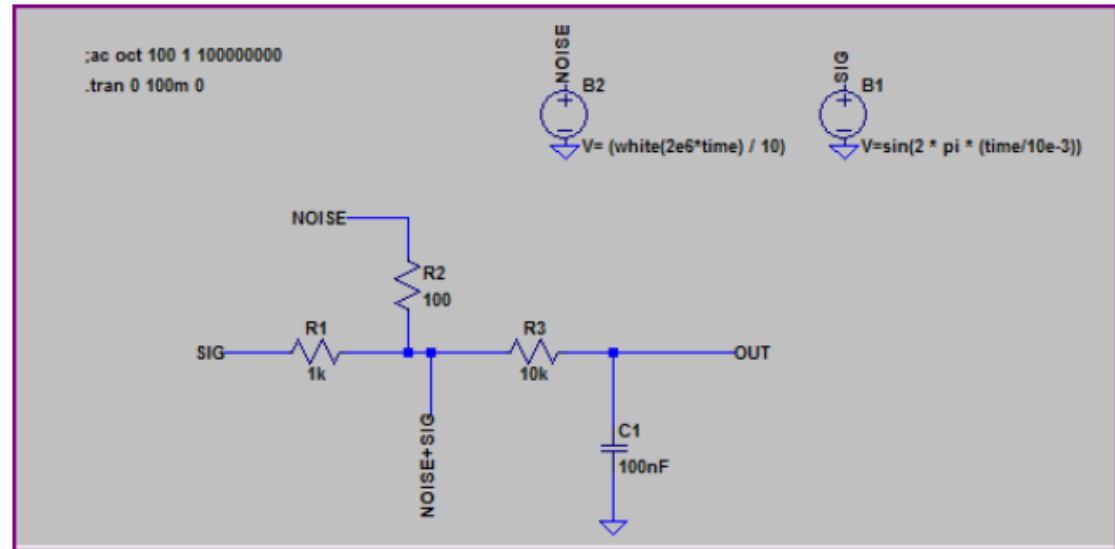
Flicker Noise, Thermal Noise Simulation for a commercial Amplifier



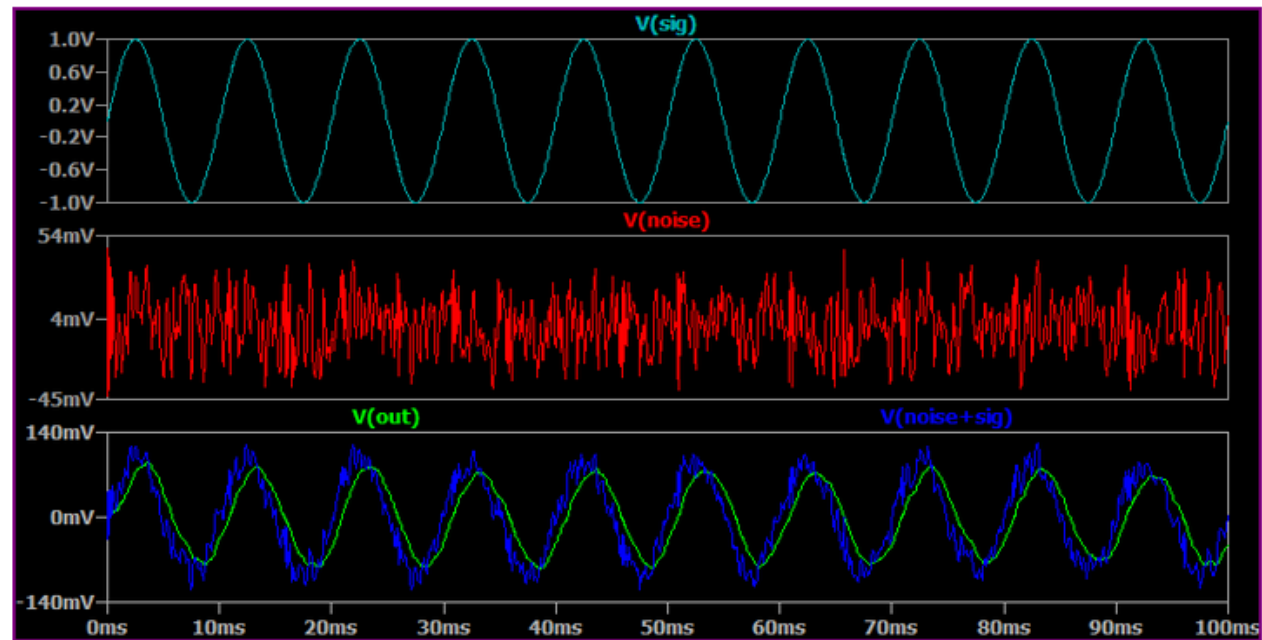
OPA838 input noise model

Reproduced from [2]

Transient Noise Analysis LT-Spice



Simulation:



References:

- [1]

Wang et al., 2020

- [2]

<https://axotron.se/blog/voltage-and-current-noise-sources-in-ltspice-noise-simulations/>

- [3]

<https://electronics.stackexchange.com/questions/55233/how-do-you-simulate-voltage-noise-with-ltspice>

- [4]

<https://www.allaboutcircuits.com/technical-articles/how-to-perform-transient-analysis-noise-simulation-LTspice/>