### Econ 7217 Economic Analysis of Social Networks Peer (Spillover) Effects from Social Networks

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March 11, 2024

#### Studies on social interactions

There is a huge literature studying peer (spillover) effects in different contexts:

- primary school reading literacy progress (Ammermueller and Pischke, 2009); high school academic performance (Calvó-Armengol et al., 2009; Lin, 2010); college achievement (Carrell et al., 2009; Zimmerman, 2003; Sacerdote, 2001); academic cheating (Carrell et al., 2008);
- smoking (Powell et al., 2005; Nakajima, 2007; Fletcher, 2010a; Hsieh and Van Kippersluis, 2018) and substance use (Lundborg, 2006; Kawaguchi, 2004; Clark and Lohéac, 2007); crime and juvenile behavior (Glaeser et al., 1996; Gaviria and Raphael, 2001; Bayer et al., 2009);

References

#### Studies on social interactions

- school enrollment decision (Bobonis and Finan, 2009; Lalive and Cattaneo, 2009);
- occupation choice (Arcidiacono and Nicholson, 2005);
- productivity in workplace (Mas and Moretti, 2009; Guryan et al., 2009; Nair et al., 2010);
- scientific research (Waldinger, 2011);
- program participation (Dahl et al., 2014; Duflo and Saez, 2003; Bertrand et al., 2000);
- monetary shocks on real economy (Ozdagli and Weber, 2017);
- spatial dependence on FDI (Blonigen et al., 2007)

#### Linear-in-means model

- Finding correlation on individuals' economic activities is not difficult, but
  to argue that it results from peer effects is difficult. One must deal with
  several identification challenges, such as the reflection problem,
  self-selection, unobserved confounding effects, etc.
- The conventional model employed to study social interactions is the linear-in-means model (Manski, 1993).
- Group mean outcome,  $\mathbb{E}(Y_g)$ , and group mean characteristics,  $\mathbb{E}(X_g)$ , for group g are included to capture the endogenous effect  $(\lambda_0)$  and contextual effects  $(\beta_{20})$ , respectively:

$$y_{ig} = \lambda_0 \mathbb{E}(Y_g) + \beta_{10} x_{ig} + \beta_{20} \mathbb{E}(X_g) + \varepsilon_{ig}.$$
 (1)

• Assuming  $\mathbb{E}(\varepsilon_g) = 0$ , we can show that the two regressors  $\mathbb{E}(Y_g)$  and  $\mathbb{E}(X_g)$  are linearly dependent:

$$\mathbb{E}\left(Y_{g}\right) = \frac{\beta_{10} + \beta_{20}}{1 - \lambda_{0}} \mathbb{E}\left(X_{g}\right). \tag{2}$$

#### Linear-in-means model

The reduced form of the model is

$$y_{ig} = \beta_{10}x_{ig} + \left(\frac{\lambda_0\beta_{10} + \beta_{20}}{1 - \lambda_0}\right)\mathbb{E}\left(X_g\right) + \varepsilon_{ig}. \tag{3}$$

- The "reflection problem": only  $\beta_{10}$  and  $\frac{\lambda_0\beta_{10}+\beta_{20}}{1-\lambda_0}$  are identified from the reduced form. One cannot separately identify the endogenous effect coefficient  $\lambda_0$  and the contextual effects coefficient  $\beta_{20}$ .
- To circumvent the "reflection problem", empirical studies usually focus
  on either the endogenous effect or the contextual effect, assuming the
  other type of social effects is not present.
- The alternative way to solve the "reflection problem" is the exclusion of individual's own outcome/characteristics from the group mean as well as the variation of group size, which breaks down the linear relationship between the endogenous and contextual effects in Equation (2).
- One can also prevent the reflection problem by using nonlinear models, or panel data, etc.

#### Reflection Problem

• The model with both endogenous and contextual effects:

$$y_{ig} = \lambda_0 \overline{Y}_{-ig} + \beta_{10} x_{ig} + \beta_{20} \overline{X}_{-ig} + \varepsilon_{ig}, \quad g = 1, \cdots, G,$$
 (4)

where  $\overline{Y}_{-ig} = \left(\frac{1}{m_g-1}\sum_{j\neq i}^{m_g}y_{jg}\right)$  and  $\overline{X}_{-ig} = \left(\frac{1}{m_g-1}\sum_{j\neq i}^{m_g}x_{jg}\right)$  and  $m_g$  is the size of group g.

• Solving for  $\overline{Y}_{-ig}$  one can get a different version of Equation (2):

$$egin{aligned} \overline{Y}_{-i\mathrm{g}} &= rac{\lambda_0}{(m_\mathrm{g}-1) - \lambda_0 \, (m_\mathrm{g}-2)} y_{i\mathrm{g}} + rac{eta_{10} \, (m_\mathrm{g}-1) + eta_{20} \, (m_\mathrm{g}-2)}{(m_\mathrm{g}-1) - \lambda_0 \, (m_\mathrm{g}-2)} \overline{X}_{-i\mathrm{g}} \ &+ rac{eta_{20}}{(m_\mathrm{g}-1) - \lambda_0 \, (m_\mathrm{g}-2)} x_{i\mathrm{g}} + rac{(m_\mathrm{g}-1) \, \overline{arepsilon}_{-i\mathrm{g}}}{(m_\mathrm{g}-1) - \lambda_0 \, (m_\mathrm{g}-2)}, \end{aligned}$$

which is certainly not linear in  $\overline{X}_{-ig}$ .

References

#### Reflection Problem

The reduced form of the model becomes:

$$y_{ig} = \frac{\lambda_0 \beta_{20} + [(m_g - 1) - \lambda_0 (m_g - 2)] \beta_{10}}{(1 - \lambda_0) (m_g - 1 + \lambda_0)} x_{ig} + \frac{(m_g - 1) (\lambda_0 \beta_{10} + \beta_{20})}{(1 - \lambda_0) (m_g - 1 + \lambda_0)} \overline{X}_{-ig} + \frac{(m_g - 1)}{(m_g - 1 + \lambda_0)} \varepsilon_{ig} + \frac{\lambda_0 m_g}{(1 - \lambda_0) (m_g - 1 + \lambda_0)} \overline{\varepsilon}_g.$$
(5)

• As long as the group size,  $m_g$ , is different across groups, valuable information from the differences in the social interaction patterns among the groups resolves the "reflection problem".

#### Correlated Effects

- There is another endogeneity issue due to self-selection (sorting) into groups and the unobserved environmental factors (correlated effects) that confound with the endogenous and contextual peer effects.
- For example, rich families will move in good school districts that their children can go to these good schools.
- Standard solution in the literature is to include group fixed effects.
- A model with endogenous and contextual effects, as well as group fixed effects, is specified as follows:

$$y_{ig} = \lambda_0 \overline{Y}_{-ig} + \beta_{10} x_{ig} + \beta_{20} \overline{X}_{-ig} + \alpha_g + \epsilon_{ig}, \quad g = 1, \dots, G, \quad (6)$$

where  $\alpha_g$  denotes the fixed effect for group g.

#### Correlated Effects

• Based on Equation (6), Lee (2007) derives the between equation

$$\overline{Y}_{g} = \frac{(\beta_{10} + \beta_{20})}{(1 - \lambda_{0})} \overline{X}_{g} + \frac{1}{(1 - \lambda_{0})} \alpha_{g} + \frac{1}{(1 - \lambda_{0})} \overline{\epsilon}_{g}, \quad g = 1, \cdots, G, \quad (7)$$

and the within equation

$$y_{ig} - \overline{Y}_{g} = \frac{(m_{g} - 1) \left(\beta_{10} - \frac{\beta_{20}}{m_{g} - 1}\right)}{(m_{g} - 1 + \lambda_{0})} (x_{ig} - \overline{X}_{g}) + \frac{(m_{g} - 1)}{(m_{g} - 1 + \lambda_{0})} (\epsilon_{ig} - \overline{\epsilon}_{g}),$$
(8)

where  $\overline{Y}_g$ ,  $\overline{X}_g$ , and  $\overline{\epsilon}_g$  are computed from all  $m_g$  individuals in the  $g^{th}$  group.

#### Correlated Effects

- Because Equation (7) contains the unknown group fixed effect  $\alpha_g$ , there is no way to identify  $\lambda_0$ ,  $\beta_{10}$ , and  $\beta_{20}$  separately from  $\alpha_g$ . The possible identification only relies on Equation (8).
- If all group sizes are the same, i.e., m<sub>g</sub> = m for all g, identification fails because there are three structural form parameters but there is only one reduced-form equation. Thus, group size variation at least three different group sizes is again a necessary condition for identification.
- Nonetheless, it is important to note that the group size variation may only provide a tenuous source of identification. When the group size is large, the ratio  $\frac{m_g-1}{m_g-1+\lambda_0}$  is close to one and  $\lambda_0$  cannot be easily estimated from Equation (8).

#### SAR Model - Identification

Introduction

- Information on the social network of each individual in a group may be captured by a spatial weights matrix in a spatial autoregressive (SAR) model (Anselin, 1988; Kelejian and Prucha, 1998; Lee, 2004), which introduces additional non-linearity for identification of various social interaction effects beyond the variation of group sizes.
- The network interaction model with the endogenous and contextual peer effects, and the group fixed effects is specified as:

$$y_{ig} = \lambda_0 \sum_{j=1}^{m_g} \overline{w}_{ij,g} y_{jg} + \beta_{10} x_{ig} + \beta_{20} \sum_{j=1}^{m_g} \overline{w}_{ij,g} x_{jg} + \alpha_g + \epsilon_{ig}, \quad g = 1, \dots, G,$$

$$(9)$$

where  $\overline{w}_{ij,g} = \frac{w_{ij,g}}{\sum_i w_{ij,g}}$ ,  $w_{ij,g} = 1$  if individual j is i's friend;

#### SAR Model - Identification

Introduction

 To see where the identification comes from, consider a simplified model without group fixed effects and in the matrix form:

$$Y_g = \lambda_0 \overline{W}_g Y_g + X_g \beta_{10} + \overline{W}_g X_g \beta_{20} + \epsilon_g, \quad g = 1, \dots, G.$$
 (10)

- This model is identified if and only if some instruments can be found for the endogenous vector W<sub>g</sub> Y<sub>g</sub>.
- Bramoullé et al. (2009) and Calvó-Armengol et al. (2009) found useful IVs under the condition that the matrices,  $I_{m_g}$ ,  $\overline{W}_g$ ,  $\overline{W}_g^2$  are linearly independent, where  $I_{m_g}$  denotes the identity matrix of dimension  $m_g$ .
- This will be true as long as the network links are intransitive, i.e., some individuals are not friends with her friends' friends. Then the characteristics of peers of peers,  $\overline{W}_g^2 X_g$ , may serve as instruments for peers' outcomes,  $\overline{W}_g Y_g$ .

References

#### SAR Model - estimation with 2SLS

• From Equation (10), the reduced form is

$$Y_{g} = (I_{m_{g}} - \lambda_{0} \overline{W}_{g})^{-1} (\beta_{10} X_{g} + \beta_{20} \overline{W}_{g} X_{g} + \epsilon_{g})$$
$$= (I_{m_{g}} - \lambda_{0} \overline{W}_{g})^{-1} (H_{g} \beta_{0} + \epsilon_{g}), \tag{11}$$

where  $H_g = (X_g, \overline{W}_g X_g)$  and  $\beta_0 = (\beta_{10}, \beta_{20})'$ .

$$\mathbb{E}(\overline{W}_g Y_g | \overline{W}_g, X_g) = \overline{W}_g (I_{m_g} - \lambda_0 \overline{W}_g)^{-1} (H_g \beta_0). \tag{12}$$

• If  $|\lambda_0| < 1$ , the matrix  $(I_{m_g} - \lambda_0 \overline{W}_g)$  is nonsingular and one can write

$$\left(I_{m_g} - \lambda_0 \overline{W}_g\right)^{-1} = I_{m_g} + \lambda_0 \overline{W}_g + \lambda_0^2 \overline{W}_g^2 + \cdots$$
 (13)

$$\mathbb{E}(\overline{W}_{g}Y_{g}) = \overline{W}_{g}H_{g}\beta_{0} + \lambda_{0}\overline{W}_{g}^{2}H_{g}\beta_{0} + \lambda_{0}^{2}\overline{W}_{g}^{3}H_{g}\beta_{0} + \cdots$$

$$= (\overline{W}_{g}H_{g}, \overline{W}_{g}^{2}H_{g}, \overline{W}_{g}^{3}H_{g}, \cdots)(\beta'_{0}, \lambda_{0}\beta'_{0}, \lambda'_{0}^{2}\beta'_{0}, \cdots)' \qquad (14)$$

and thus  $(\overline{W}_g H_g, \overline{W}_g^2 H_g, \overline{W}_g^3 H_g, \cdots)$  can be used as IVs for  $\overline{W}_g Y_g$ .

#### SAR Model - estimation with 2SLS

• Define  $U_g = (H_g, \overline{W}_g H_g, \overline{W}_g^2 H_g, \cdots, \overline{W}_g^p H_g)$  as the IV matrix, then

$$\mathbb{E}(U_g'\epsilon_g)=0. \tag{15}$$

• Let  $\epsilon_g(\lambda_0, \delta_0) = Y_g - \lambda_0 \overline{W}_g Y_g - H_g \beta_0$ , the empirical counterpart of Equation (15) is

$$U_g'\epsilon_g(\lambda_0,\beta_0)=0. (16)$$

• One can further incorporate quadratic moment conditions in the form,  $\epsilon_g(\lambda_0,\beta_0)'A\epsilon_g(\lambda_0,\beta_0)$  with A denotes a constant square matrix in GMM to improve estimation efficiency (Liu and Lee, 2010) so that GMM can be asymptotically as efficient as MLE.

#### SAR Model - estimation with 2SLS

- Define  $Y=(Y_1',\cdots,Y_G')'$ ,  $H=(H_1',\cdots,H_G')'$ ,  $\epsilon=(\epsilon_1',\cdots,\epsilon_G')'$ ,  $W=D(\overline{W}_1,\cdots,\overline{W}_G)$ , where D denotes the block diagonal matrix, and Z=(WY,H) is the matrix of regressors.
- Use the instrument matrix  $U=(H,WH,W^2H)$ , the 2SLS estimator for  $\delta=(\lambda,\beta')'$  is

$$\hat{\delta}_{2sls} = \left( Z'PZ \right)^{-1} Z'PY, \tag{17}$$

where  $P = U(U'U)^-U'$  and  $A^-$  is the generalized inverse of a square matrix A.

$$\operatorname{var}(\hat{\delta}_{2sls}) = \hat{\sigma}^2 \left( Z' P Z \right)^{-1}. \tag{18}$$

#### SAR Model - estimation with 2SLS

 Consider a general form of the model with group fixed effect as in Equation (9):

$$Y_g = \lambda_0 \overline{W}_g Y_g + X_g \beta_{10} + \overline{W}_g X_g \beta_{20} + \ell_{m_g} \alpha_g + \epsilon_g, g = 1, \dots, G.$$
 (19)

 As shown in Lee et al. (2010) and Lin (2010), the group fixed effect can be eliminated by the de-group-mean transformation, i.e., by multiplying Equation (19) with the matrix

$$J_{m_g} = I_{m_g} - \frac{1}{m_g} \ell_{m_g} \ell'_{m_g}. \tag{20}$$

$$\hat{Y}_{g} = \lambda_{0} \overline{W}_{g} \hat{Y}_{g} + \hat{X}_{g} \beta_{10} + \overline{W}_{g} \hat{X}_{g} \beta_{20} + \hat{\epsilon}_{g}, \qquad (21)$$

where  $\hat{Y}_g = J_{m_g} Y_g, \hat{X}_g = J_{m_g} X_g$ , and  $\hat{\epsilon}_g = J_{m_g} \epsilon_g$ .

• This model is identified if and only if  $\mathbb{E}\left(\overline{W}_g\,\hat{Y}_g|X_g\right)$  is not perfectly collinear with the regressors  $\left(\hat{X}_g,\overline{W}_g\hat{X}_g\right)$  which is equivalent to the matrices,  $I_{m_g},\overline{W}_g,\overline{W}_g^2,\overline{W}_g^3$  are linearly independent.

#### SAR Model - estimation with MLE

• Assume  $\epsilon_g | W_g, X_g \sim N(0, \sigma^2 I_{m_g})$ , then from Equation(11) we have

$$Y_g \sim N(\mu_{Y_g}, \Sigma_{Y_g}), \tag{22}$$

where  $\mu_{Y_g} = (I_{m_g} - \lambda \overline{W}_g)^{-1} H_g \delta$  and  $\Sigma_{Y_g} = \sigma^2 (I_{m_g} - \lambda W_g)^{-1} (I_{m_g} - \lambda W_g')^{-1}.$ 

• Let  $\theta = (\lambda, \delta', \sigma^2)'$ , the log-likelihood is given by

$$\mathcal{L}(\theta) = -\frac{\sum_{g} m_{g}}{2} \ln(2\pi) - \frac{\sum_{g} m_{g}}{2} \ln \sigma^{2} + \sum_{g} \ln |(I_{m_{g}} - \lambda \overline{W}_{g})|$$
$$-\frac{1}{2\sigma^{2}} \sum_{g} \epsilon_{g}(\lambda, \delta)' \epsilon_{g}(\lambda, \delta). \tag{23}$$

- MLE is inconsistent when the error terms are heteroskedastic.
- Lin and Lee (2010) propose GMM estimation for SAR models with unknown heteroskedasticity.

# Social Interactions and Social Preference in Social Networks (Hsieh and Lin 2021)

- The experimental literature on social preferences has recently started to uncover the connection between peer effects and social preferences.
- As social interactions occur on a regular basis and within small groups, altruism is expected to play an important role since people may intrinsically care about the well-being of their social contacts and take into account their preferences when making decisions.
- In this paper, we provide the first empirical analysis on social interactions and social preferences in social networks, building a bridge between the two strands of rapidly growing yet unrelated literature. We investigate the model specification issues that emerge from extending the standard assumption of self-interest to a more evolutionary foundation in which individuals may be altruistic.

# Social Interactions and Social Preference in Social Networks (Hsieh and Lin. 2021)

Consider that individuals belong to groups,  $g=1,\cdots,G$ .

- $y_{i,g}$ : activity outcome of individual i in group g.
- $x_{i,g}$ : a  $k \times 1$  individual characteristics.
- $W_g$ : an adjacency matrix that summarizes the friendship links between  $m_g$  individuals in group g.  $w_{ij,g}=1$  if individual i chooses individual j as a friend and  $w_{ij,g}=0$  otherwise. We assume  $W_g$  is not symmetric.

$$y_{i,g} = \lambda \sum_{j=1}^{m_g} w_{ij,g} y_{j,g} + x_{i,g} \beta_1 + \sum_{j=1}^{m_g} w_{ij,g} x_{j,g} \beta_2 + \tau_g + \epsilon_{i,g}, \quad \text{for } i = 1, \dots, m_g.$$
(24)

We call Equation (24) or its vector form "conventional social interactions model",

$$Y_g = \lambda W_g Y_g + X_g \beta_1 + W_g X_g \beta_2 + \ell_g \tau_g + \epsilon_g.$$
 (25)

#### Social Interactions and Social Preference in Social Networks

 The quadratic specification of individual payoff function from Ballester et al. (2006) and Calvó-Armengol et al. (2009):

$$v_{i,g}(y_{i,g}, Y_{-i,g}, W_g) = \mu_{i,g} y_{i,g} - \frac{1}{2} y_{i,g}^2 + \lambda y_{i,g} \sum_{j=1}^{m_g} w_{ij,g} y_{j,g} + \eta \sum_{j=1}^{m_g} w_{ij,g} y_{j,g}.$$
(26)

- $\mu_{i,g}$  in the first term reflects individual heterogeneity.
- $y_{i,g} \sum_{j=1}^{m_g} w_{ij,g} y_{j,g}$  in the third term captures the complementary effect from peers' activities, which provides the source of peer influences.
- $\sum_{j=1}^{m_g} w_{ij,g} y_{j,g}$  in the fourth term captures the direct externality effect from peers' activity outcomes.

• If individuals directly choose  $y_{i,g}$  to maximize Eq. (26), then the first order condition gives

$$\mu_{i,g} - y_{i,g} + \lambda \sum_{j=1}^{m_g} w_{ij,g} y_{j,g} = 0,$$

which implies the optimal choice of  $y_{i,g}$  satisfies

$$y_{i,g} = \mu_{i,g} + \lambda \sum_{j=1}^{m_g} w_{ij,g} y_{j,g}.$$

- The unique Nash equilibrium vector of outcomes is given by  $Y_g = (I_{m_g} \lambda W_g)^{-1} \mu_g \text{ if } |\lambda| \text{ satisfies a bound constraint.}$
- By specifying  $\mu_{i,g} = (x_{i,g}\beta_1 + \sum_{j=1}^{m_g} w_{ij,g}x_{j,g}\beta_2 + \tau_g + \epsilon_{i,g})$ , the outcome  $Y_g$  can be modelled by the SAR in Equation (25).

- Now assume individuals are altruistic to others, which means individuals care about others' payoffs.
- ullet One simplest form of the utility function  $U_{i,g}$  which illustrates the above altruistic preference is a linear function of individual's own and others' payoffs

$$U_{i,g} = v_{i,g}(y_{i,g}, Y_{-i,g}, W_g) + \alpha_1 \sum_{j=1, j \neq i}^{m_g} v_{j,g}(y_{j,g}, Y_{-j,g}, W_g).$$
 (27)

- The coefficient  $\alpha_1$  reflects how much individuals care about others' payoffs, i.e., the altruism level.
- We assume  $\alpha_1$  to be bounded by [-1,1]. When  $\alpha_1$  is positive, individuals are altruistic; when  $\alpha_1$  equals to zero, individuals are selfish; and when  $\alpha_1$  is negative, individuals are spiteful.

- Based on Equation (27), the first order condition  $\frac{\partial U_{i,g}}{\partial y_{i,g}} = 0$  determines individual's choice of  $y_{i,g}$ .
- What we get is

$$\mu_{i,g} - y_{i,g} + \lambda \sum_{j=1}^{m_g} w_{ij,g} y_{j,g} + \alpha_1 (\lambda y_{j,g} w_{ji,g} + \eta w_{ji,g}) = 0.$$

The vector of Nash equilibrium strategy played by individuals is

$$Y_{g} = \lambda W_{g} Y_{g} + \lambda^{\mathrm{I}} W_{g}^{\mathrm{T}} Y_{g} + \eta^{\mathrm{I}} W_{g}^{\mathrm{T}} \ell_{g} + X_{g} \beta_{1} + W_{g} X_{g} \beta_{2} + \ell_{g} \tau_{g} + \epsilon_{g},$$
(28)

where  $\lambda^{\rm I}=\alpha_1\lambda$ ;  $\eta^{\rm I}=\alpha_1\eta$  and  $W^{\rm T}$  denotes the transpose of  $W_g$ . We refer Equation (28) as the "altruistic social interactions model."

- This extension justifies the peer effects from both outward and inward friendship links and why the in-degree centrality  $(W_g^T \ell_g)$  (or popularity) would matter for individual outcome.
- It also allows us to infer the degree of altruism toward others' payoffs and the direct externality effect from peers' activity outcome.
- ullet The estimate of  $\lambda$  in the conventional social interactions model would be
  - 1. (upward) biased when omitting the altruism term,  $W_g^{
    m T} Y_g$
  - 2. (upward or downward) biased when omitting the externality term,  $W_g^{\rm T}\ell_g$

• We can further enrich the utility specification of Equation (27) as follows:

$$U_{i,g} = v_{i,g}(y_{i,g}, Y_{-i,g}, W_g) + \sum_{j=1, j \neq i}^{m_g} (\alpha_1 + \alpha_2 w_{ij,g}) v_{j,g}(y_{j,g}, Y_{-j,g}, W_g),$$
(29)

to reflects the directed altruism in Leider et al. (2009) – the altruism level should be stronger among friends than among random strangers (heterogeneous altruism among pairs of individuals).

 Based on Equation (29), the vector of Nash equilibrium strategy can be modeled by the "directed altruistic social interactions model."

$$Y_{g} = \lambda W_{g} Y_{g} + \lambda^{\mathrm{I}} W_{g}^{\mathrm{T}} Y_{g} + \lambda^{\mathrm{R}} W_{g}^{\mathrm{R}} Y_{g} + \eta^{\mathrm{I}} W_{g}^{\mathrm{T}} \ell_{g} + \eta^{\mathrm{R}} W_{g}^{\mathrm{R}} \ell_{g}$$
$$+ X_{g} \beta_{1} + W_{g} X_{g} \beta_{2} + \ell_{g} \tau_{g} + \epsilon_{g},$$
(30)

where  $W_g^{\rm R}$  stands for the network of reciprocal links, i.e.,  $w_{ij,g}^{\rm R}=1$  if  $w_{ij,g}=w_{ji,g}=1$ .  $\lambda^{\rm I}=\alpha_1\lambda$ ,  $\eta^{\rm I}=\alpha_1\eta$ ,  $\lambda^{\rm R}=\alpha_2\lambda$ ,  $\eta^{\rm R}=\alpha_2\eta$ .

 It provides the microfoundations to explain the results of heterogeneous peer effects between chosen, unchosen, and mutual friends in Lin and Weinberg (2014).

- Our empirical study employs the Add Health data, which is a longitudinal study on a nationally representative sample in U.S. covering adolescents in grade 7 through 12 (average age from 12 to 17) from 132 schools.
- The Add Health data contains detailed information about respondents' demographic backgrounds, academic performance, and health related behaviors. Most uniquely, the Add Health asked each respondent to nominate their male and female friends so that researchers can use the information to construct students' friendship networks.

- We define groups at the school level and consider a sample of 24 schools with each size less than 300. There is a total of 2,926 students in this sample.
- We study four different activity outcomes
  - 1. academic achievement (measured by GPA)
  - 2. smoking (measured by number of smoking days per month)
  - extracurricular activities (measured by the number of school clubs attended)
  - misconducts (measured by frequency of doing dangerous activity, lying, and school skipping)
- We don't find significant estimates of altruism for club participation and misconduct.

| Variables                  | Min. | Max. | Mean     | S.D.    |
|----------------------------|------|------|----------|---------|
| GPA                        | 1    | 4    | 2.9020   | 0.7379  |
| Smoking                    | 0    | 30   | 4.4142   | 9.8641  |
| Club                       | 0    | 6    | 2.5772   | 1.8540  |
| Misconduct                 | 0    | 6    | 1.2230   | 1.0267  |
| Male                       | 0    | 1    | 0.4836   | 0.4998  |
| Age                        | 11   | 19   | 15.5533  | 1.2383  |
| White                      | 0    | 1    | 0.6141   | 0.4869  |
| Black                      | 0    | 1    | 0.2409   | 0.4277  |
| Asian                      | 0    | 1    | 0.0208   | 0.1429  |
| Hispanic                   | 0    | 1    | 0.0687   | 0.2530  |
| Other race                 | 0    | 1    | 0.0554   | 0.2287  |
| Both parents               | 0    | 1    | 0.7310   | 0.4435  |
| Less HS                    | 0    | 1    | 0.1063   | 0.3083  |
| HS                         | 0    | 1    | 0.3486   | 0.4766  |
| More HS                    | 0    | 1    | 0.4070   | 0.4914  |
| Edu missing                | 0    | 1    | 0.0660   | 0.2483  |
| Welfare                    | 0    | 1    | 0.0109   | 0.1040  |
| Job missing                | 0    | 1    | 0.0738   | 0.2615  |
| Professional               | 0    | 1    | 0.2642   | 0.4410  |
| Other job                  | 0    | 1    | 0.3452   | 0.4755  |
| Homemaker                  | 0    | 1    | 0.2338   | 0.4233  |
| group size                 | 15   | 245  | 171.9986 | 66.1802 |
| Number of groups (schools) |      |      | 24       |         |
| Observations               |      |      | 2,926    |         |

roduction Linear-in-means model SAR model Example I Example II Example III References

#### Social Interactions and Social Preference in Social Networks

### Table: Estimation Result: Conventional and Altruistic Social Interactions Models

|                                    | Conventional Model    |                       | Altruistic Model                               |   | Altruistic Model w/ direct externality                                   |  |
|------------------------------------|-----------------------|-----------------------|--|---|--|--|
|                                    | GPA                   | Smoking               | GPA  | Smoking                                     | GPA  | Smoking  |
| $\lambda$ $\lambda^{I}$ $\eta^{I}$ | 0.0700***<br>(0.0069) | 0.0924***<br>(0.0047) | 0.0610***<br>(0.0055)<br>0.0074***<br>(0.0015) | 0.0759***<br>(0.0135)<br>0.0184<br>(0.0127) | 0.0450***<br>(0.0058)<br>0.0302***<br>(0.0062)<br>-0.0701***<br>(0.0194) | 0.0592***<br>(0.0099)<br>0.0367***<br>(0.0097)<br>-0.1915***<br>(0.0707) |

## Table: Estimation Result: Directed Altruistic Social Interactions Models

|    | Directed Altruistic Model |                       | Directed Altruistic Model w/ externality |                                     |  |
|----|---------------------------|-----------------------|--|-------------------------------------|--|
|    | GPA                       | Smoking               | GPA                                      | Smoking                             |  |
| \  | 0.0648***<br>(0.0071)     | 0.0765***<br>(0.0116) | 0.0458***<br>(0.0075)                    | 0.0564***<br>(0.0110)               |  |
| 'I | 0.0087***<br>(0.0021)     | 0.0025<br>(0.0134)    | 0.0273***<br>(0.0093)                    | 0.0306***<br>(0.0119)               |  |
| R  | -0.0044<br>(0.0046)       | 0.0260*<br>(0.0144)   | 0.0012<br>(0.0118)                       | 0.0148<br>(0.0138)                  |  |
| I  |                           |                       | -0.0563**<br>(0.0287)                    | -0.3007* <sup>*</sup> *<br>(0.0945) |  |
| R  |                           |                       | -0.0239<br>(0.0388)                      | 0.3792<br>(0.2085)                  |  |

# Smoking Initiation – Peers and Personality (Hsieh and Van Kippersluis 2018)

- Smoking continues to be the leading preventable cause of death, killing nearly 6 million people each year (Mokdad et al., 2004; Danaei et al., 2009; OECD, 2013).
- The economics literature has traditionally focused on price, taxation, and addiction as determinants of smoking (Chaloupka and Warner, 2000; DeCicca et al., 2002).
- In recent years, considerably more attention is paid to social interactions in smoking and other unhealthy behaviors (Cawley and Ruhm, 2011; DeCicca et al., 2008).
- Social interactions and peer effects are not just often-cited determinants of smoking initiation, but – when present – additionally capable of generating social multiplier effects of policy interventions (Cutler and Glaeser, 2010; Fletcher, 2010b; Cawley and Ruhm, 2011).

#### Smoking Initiation – Peers and Personality

Most widely-accepted taxonomy of personality (also known as non-cognitive skills) is the so-called "Big Five" (acronym OCEAN, Digman, 1990; Matthews et al., 2003):

- Openness to experience ("the degree to which a person needs intellectual stimulation, change, and variety")
- Conscientiousness ("the degree to which a person is willing to comply with conventional rules, norms, and standards")
- Extraversion ("the degree to which a person needs attention and social interaction")
- Agreeableness ("the degree to which a person needs pleasant and harmonious relations with others")
- Emotional stability (or Neuroticism, "the degree to which an individual experiences the world as threatening and beyond his/her control")

#### Smoking Initiation – Peers and Personality

- When your behavior is correlated with the behaviors of your peers, this could occur for three different reasons:
  - Endogenous effect: individual behavior is truly affected by the peers' behaviors.
  - Contextual effect: individual behavior is affected by the (observed and unobserved) exogenous characteristics of the peers.
  - Correlated effect (a.k.a. selection, common environment): behaviors
    are similar due to (i) self-selection into the group, or (ii) share
    similar environments (e.g. rich neighborhood, good teacher quality).
- The reflection problem (Manski, 1993): the endogenous and contextual effects are not separately identified in a linear model when peers of individuals are perfectly identical, e.g., all school students are your peers.

#### Smoking Initiation - Peers and Personality

Incorporate personality effects into the SAR model:

$$\begin{split} y_{i,g} &= \lambda_{11} I(\mathbf{s}_{ir,g} < \overline{\mathbf{S}}_{r,g}) \sum_{j \neq i} w_{ij,g} I(\mathbf{s}_{jr,g} < \overline{\mathbf{S}}_{r,g}) y_{j,g} \\ &+ \lambda_{12} I(\mathbf{s}_{ir,g} < \overline{\mathbf{S}}_{r,g}) \sum_{j \neq i} w_{ij,g} I(\mathbf{s}_{jr,g} \geq \overline{\mathbf{S}}_{r,g}) y_{j,g} \\ &+ \lambda_{21} I(\mathbf{s}_{ir,g} \geq \overline{\mathbf{S}}_{r,g}) \sum_{j \neq i} w_{ij,g} I(\mathbf{s}_{jr,g} < \overline{\mathbf{S}}_{r,g}) y_{j,g} \\ &+ \lambda_{22} I(\mathbf{s}_{ir,g} \geq \overline{\mathbf{S}}_{r,g}) \sum_{j \neq i} w_{ij,g} I(\mathbf{s}_{jr,g} \geq \overline{\mathbf{S}}_{r,g}) y_{j,g} \\ &+ \chi_{i,g} \beta_{1} + \sum_{j \neq i} w_{ij,g} \chi_{i,g} \beta_{2} + \mathbf{s}_{i,g} \beta_{3} + \sum_{j \neq i} w_{ij,g} \mathbf{s}_{i,g} \beta_{4} + \alpha_{g} + \epsilon_{i,g}, \end{split}$$

where I(A) denotes an indicator function which equals one if A is satisfied and equals zero, otherwise.  $s_{ir,g}$  denote the  $r^{th}$  dimension of personality.  $\overline{S}_{r,g}$  denotes the average of the  $r^{th}$  personality measure in group g.

#### Smoking Initiation - Peers and Personality

The vector form of our SAR model specification:

$$\begin{aligned} Y_g &= \lambda_{11} W_{11,g} Y_g + \dots + \lambda_{22} W_{22,g} Y_g \\ &+ X_g \beta_1 + W_g X_g \beta_2 + S_g \beta_3 + W_g S_g \beta_4 + \ell_g \alpha_g + \epsilon_g, \end{aligned}$$

 $W_{\rm g}$  is now divided into 2  $\times$  2 blocks, where each block,  $W_{\rm g}^{pq}$ , p,q=1,2, represents the subnetwork between individuals in the personality subgroups 1 and 2.  $W_{pq,g}$  is a  $m_{\rm g} \times m_{\rm g}$  matrix with the corresponding  $(p,q)^{\rm th}$  block equal to  $W_{\rm g}^{pq}$  and 0 elsewhere.

Introduction Linear-in-means model SAR model Example II Example II References

### Smoking Initiation – Peers and Personality

- Add Health is a nationally representative survey of adolescents enrolled in grades 7-12 from 132 schools. Four waves of surveys were conducted from 1994 to 2008.
- In Wave I, 90,000 Students were interviewed and each respondent was asked to nominate up to five male and five female friends. We use such information to construct students' friendship networks.
- To study the relationship between personality and smoking, we use the Wave I in-home survey data, which contains more detailed questions on family background than the in-school survey data, and includes information on individual's personality characteristics.
- There are 20,745 students who participated in the Wave I in-home survey.
   We focus on small- and mid-size schools that have less than three hundred students.

### Smoking Initiation - Peers and Personality

Construct three out of the big five personality measures: emotional stability,

conscientiousness, and extraversion from the factor analysis.

| Item identifier | Description  | F      | actor loading | s      | Regression Coef. |        |        |
|-----------------|--|--------|---------------|--------|------------------|--------|--------|
|                 |  | ES     | С             | E      | ES               | С      | E      |
| H1PF30          | You have a lot of good qualities   | 0.6207 |               |        | 0.3164           |        |        |
| H1PF32          | You have a lot to be proud of  | 0.6602 |               |        | 0.3930           |        |        |
| H1PF33          | You like yourself just the way you are   | 0.4145 |               |        | 0.0150           |        |        |
| H1PF34          | You feel like you are doing everything just about right  | 0.3502 |               |        | -0.0371          |        |        |
| H1PF35          | You feel socially accepted   | 0.4191 |               |        | 0.0408           |        |        |
| H1PF36          | You feel wanted and loved  | 0.4903 |               |        | 0.1137           |        |        |
| H1PF18          | You get as many facts about the problem as possible when you have problems to be solved                          |        | 0.6300        |        |                  | 0.2778 |        |
| H1PF19          | You think of as many different ways to approach a problem as possible when you are attempting to find a solution |        | 0.6700        |        |                  | 0.3195 |        |
| H1PF20          | You generally use a systematic method for judging and comparing alternatives When making decisions               |        | 0.6245        |        |                  | 0.2741 |        |
| H1PF21          | You usually try to analyze what went right and what went wrong after carrying out a solution to a problem        |        | 0.5680        |        |                  | 0.2295 |        |
| S62B*           | I feel close to people at school   |        |               | 0.7014 |                  |        | 0.3543 |
| S62E*           | I feel like I am a part of this school   |        |               | 0.7175 |                  |        | 0.3786 |
| S62O*           | I feel socially accepted   |        |               | 0.6245 |                  |        | 0.2696 |

Note: These 13 items are selected by the Lexical approach and the exploratory factor analysis according to Young et al.(2011). We conduct the principle component analysis on these items and identify one main factor for each personality measure, which explains more than 90% of variation. We report the factor loadings for each item after rotation and the regression coefficients for predicting factor scores. ES: emotional stability; C:conscientiousness; E: extroversion. \* denotes that data source is Wave I in-school survey.

### Smoking Initiation – Peers and Personality

|                     | Whole Sample |       |        | Emotional Stability |       |       | Conscientiousness |       |       |       |        |       |
|---------------------|--------------|-------|--------|---------------------|-------|-------|-------------------|-------|-------|-------|--------|-------|
|                     |              |       |        |                     | high  |       | low               |       | high  |       | low    |       |
|                     | mean         | s.d.  | min    | max                 | mean  | s.d.  | mean              | s.d.  | mean  | s.d.  | mean   | s.d.  |
| smoke dummy         | 0.224        | 0.417 | 0.000  | 1.000               | 0.184 | 0.388 | 0.261             | 0.439 | 0.205 | 0.404 | 0.247  | 0.431 |
| smoke frequency     | 0.904        | 2.162 | 0.000  | 7.000               | 0.721 | 1.955 | 1.070             | 2.321 | 0.832 | 2.095 | 0.989  | 2.236 |
| drunk               | 0.311        | 0.463 | 0.000  | 1.000               | 0.272 | 0.445 | 0.346             | 0.476 | 0.296 | 0.457 | 0.327  | 0.469 |
| emotional stability | 0.015        | 0.715 | -4.033 | 1.021               | 0.636 | 0.285 | -0.547            | 0.485 | 0.146 | 0.670 | -0.140 | 0.73  |
| conscientiousness   | -0.032       | 0.831 | -3.790 | 1.565               | 0.188 | 0.877 | -0.232            | 0.733 | 0.536 | 0.499 | -0.701 | 0.61  |
| extraversion        | 0.009        | 0.840 | -2.385 | 1.260               | 0.193 | 0.806 | -0.157            | 0.835 | 0.082 | 0.838 | -0.077 | 0.83  |
| male                | 0.466        | 0.499 | 0.000  | 1.000               | 0.517 | 0.500 | 0.420             | 0.494 | 0.475 | 0.499 | 0.456  | 0.49  |
| white               | 0.541        | 0.498 | 0.000  | 1.000               | 0.538 | 0.499 | 0.544             | 0.498 | 0.530 | 0.499 | 0.554  | 0.49  |
| black               | 0.228        | 0.419 | 0.000  | 1.000               | 0.258 | 0.438 | 0.200             | 0.400 | 0.239 | 0.427 | 0.215  | 0.41  |
| asian               | 0.110        | 0.313 | 0.000  | 1.000               | 0.100 | 0.301 | 0.119             | 0.324 | 0.107 | 0.309 | 0.115  | 0.31  |
| hisp                | 0.064        | 0.244 | 0.000  | 1.000               | 0.048 | 0.214 | 0.078             | 0.267 | 0.068 | 0.253 | 0.058  | 0.23  |
| other race          | 0.057        | 0.232 | 0.000  | 1.000               | 0.055 | 0.229 | 0.059             | 0.235 | 0.056 | 0.230 | 0.059  | 0.23  |
| school taught       | 0.934        | 0.248 | 0.000  | 1.000               | 0.942 | 0.233 | 0.927             | 0.261 | 0.940 | 0.238 | 0.928  | 0.25  |
| smoke parent        | 0.643        | 0.479 | 0.000  | 1.000               | 0.632 | 0.482 | 0.652             | 0.476 | 0.634 | 0.482 | 0.654  | 0.47  |
| prof                | 0.275        | 0.447 | 0.000  | 1.000               | 0.299 | 0.458 | 0.253             | 0.435 | 0.278 | 0.448 | 0.272  | 0.44  |
| home                | 0.134        | 0.341 | 0.000  | 1.000               | 0.124 | 0.330 | 0.143             | 0.350 | 0.138 | 0.345 | 0.130  | 0.33  |
| nonprof             | 0.427        | 0.495 | 0.000  | 1.000               | 0.416 | 0.493 | 0.437             | 0.496 | 0.428 | 0.495 | 0.426  | 0.49  |
| low parent control  | 0.741        | 0.217 | 0.000  | 1.000               | 0.738 | 0.217 | 0.744             | 0.217 | 0.741 | 0.219 | 0.742  | 0.21  |
| maternal care       | 4.550        | 0.526 | 1.000  | 5.000               | 4.627 | 0.485 | 4.481             | 0.552 | 4.596 | 0.500 | 4.497  | 0.55  |
| sample size         |              | 97    | 28     |                     | 46    | 19    | 51                | 09    | 52    | 58    | 44     | 70    |

### Smoking Initiation – Peers and Personality

|   |                       | Smoke                  | Dummy                   |                         | Smoke Frequency       |                         |                         |                         |  |
|---|-----------------------|------------------------|-------------------------|-------------------------|-----------------------|-------------------------|-------------------------|-------------------------|--|
| Hom                                     |                       | geneous                | ES                      | СО                      | Homogeneous           |                         | ES                      | со                      |  |
| Endogenous effect                       | 0.0922***<br>(0.0074) | 0.0842***<br>(0.0077)  |                         |                         | 0.0947***<br>(0.0040) | 0.0911***<br>(0.0057)   |                         |                         |  |
| low-to-low                              | (0.0011)              | (0.0011)               | 0.1119***<br>(0.0127)   | 0.0914***<br>(0.0156)   | (0.0010)              | (0.0031)                | 0.1243***<br>(0.0129)   | 0.0965**<br>(0.0164)    |  |
| high-to-low                             |                       |                        | 0.0614***               | 0.0866***<br>(0.0175)   |                       |                         | 0.1257***<br>(0.0224)   | 0.1025**<br>(0.0205)    |  |
| low-to-high                             |                       |                        | 0.0802*** (0.0175)      | 0.0807***               |                       |                         | 0.0475***               | 0.0948**                |  |
| high-to-high                            |                       |                        | 0.0700***<br>(0.0171)   | 0.0802***               |                       |                         | 0.0610***               | 0.0907**                |  |
| Own effect                              |                       |                        | ` ,                     | ` ′                     |                       |                         | ()                      | ` ′                     |  |
| emotional stability                     |                       | -0.0268***<br>(0.0064) | -0.0256***<br>(0.0066)  | -0.0276***<br>(0.0063)  |                       | -0.0946***<br>(0.0327)  | -0.0580<br>(0.0341)     | -0.0945**<br>(0.0327)   |  |
| conscientiousness                       |                       | -0.0170***<br>(0.0051) | -0.0170***<br>(0.0051)  | -0.0161***<br>(0.0053)  |                       | -0.0477*<br>(0.0267)    | -0.0473*<br>(0.0267)    | -0.0451*<br>(0.0275)    |  |
| extraversion                            |                       | -0.0476***             | _0.0477 <sup>*</sup> ** | -0.0475 <sup>*</sup> ** |                       | _0.2775 <sup>*</sup> ** | _0.2792 <sup>*</sup> ** | _`0.2776 <sup>*</sup> * |  |
| Contextual effect<br>Group fixed effect | Yes<br>Yes            | Yes<br>Yes             | Yes<br>Yes              | Yes<br>Yes              | Yes<br>Yes            | Yes<br>Yes              | Yes<br>Yes              | Yes<br>Yes              |  |
| $\sigma_{\epsilon}^2$                   | 0.1577                | 0.1551                 | 0.1550                  | 0.1551                  | 4.2562                | 4.1819                  | 4.1750                  | 4.1817                  |  |

Note: We report the posterior mean of each parameter and the standard deviation in the parenthesis. The asterisks \*\*\*(\*\*\*) indicates that its 99% (99%, 90%), highest posterior density range does not cover zero. The MCMC sampling is running for 50,000 iterations with the first 5,000 iterations dropped for burn-in. ES: emotional stability; CO: conscientiousness. In the heterogeneous peer effect case, A-to-B denotes the peer effect that B receives from A.

### Smoking Initiation – Peers and Personality

|                           |                     | Smoke Dummy          |                      |                     | moke Frequency      |                       |
|---------------------------|---------------------|----------------------|----------------------|---------------------|---------------------|-----------------------|
|                           | Homogeneous         | ES                   | СО                   | Homogeneous         | ES                  | СО                    |
| Endogenous Effect         |                     |                      |                      |                     |                     |                       |
|                           | 0.0374***           |                      |                      | 0.0715***           |                     |                       |
|                           | (0.0098)            |                      |                      | (0.0091)            |                     |                       |
| low-to-low                |                     | 0.0668***            | 0.0442***            |                     | 0.0904***           | 0.0672***             |
|                           |                     | (0.0147)             | (0.0174)             |                     | (0.0129)            | (0.0164)              |
| high-to-low               |                     | 0.0247               | 0.0382**             |                     | 0.0854***           | 0.0636***             |
|                           |                     | (0.0191)             | (0.0181)<br>0.0357** |                     | (0.0210)            | (0.0182)              |
| low-to-high               |                     | 0.0316               |                      |                     | 0.0139<br>(0.0183)  | 0.0682***             |
| high-to-high              |                     | (0.0186)<br>0.0360** | (0.0180)<br>0.0322** |                     | 0.0304*             | (0.0196)<br>0.0588*** |
| Iligii-to-iligii          |                     | (0.0183)             | (0.0152)             |                     | (0.0186)            | (0.0137)              |
| Own and Contextual effect | Yes                 | Yes                  | Yes                  | Yes                 | Yes                 | Yes                   |
| Group fixed effect        | Yes                 | Yes                  | Yes                  | Yes                 | Yes                 | Yes                   |
| $\sigma_{\mu}^{2}$        | 0.1341              | 0.1344               | 0.1343               | 3.5772              | 3.6319              | 3.6609                |
| u u                       | 0.15.1              | 0.1511               | 0.1515               | 3.3772              | 3.0013              | 5.0005                |
| Link formation            |                     |                      |                      |                     |                     |                       |
| constant                  | 1.0340***           | 1.0395***            | 1.0333***            | 1.0131***           | 1.0280***           | 1.0370***             |
|                           | (0.0789)            | (0.0799)             | (0.0788)             | (0.0813)            | (0.0780)            | (0.0825)              |
| grade                     | 2.7500***           | 2.7533***            | 2.7553***            | 2.7405***           | 2.7457***           | 2.7509***             |
|                           | (0.0380)            | (0.0392)             | (0.0390)             | (0.0381)            | (0.0385)            | (0.0384)              |
| sex                       | 0.3511***           | 0.3498***            | 0.3506***            | 0.3516***           | 0.3508***           | 0.3533***             |
|                           | (0.0342)            | (0.0348)             | (0.0335)             | (0.0339)            | (0.0347)            | (0.0325)              |
| race                      | 1.1213***           | 1.1216***            | 1.1190***            | 1.1222***           | 1.1175***           | 1.1225***             |
|                           | (0.0415)            | (0.0413)             | (0.0403)             | (0.0394)            | (0.0406)            | (0.0414)              |
| emotional stability       | -0.0563*            | -0.0582*             | -0.0583*             | -0.0519*            | -0.0591*            | -0.0603*              |
|                           | (0.0291)            | (0.0291)             | (0.0301)             | (0.0290)            | (0.0294)            | (0.0294)              |
| conscientiousness         | -0.0410<br>(0.0255) | -0.0400<br>(0.0255)  | -0.0397<br>(0.0256)  | -0.0382<br>(0.0257) | -0.0380<br>(0.0254) | -0.0390<br>(0.0249)   |
| extraversion              | -0.2636***          | -0.2654***           | -0.2626***           | -0.2606***          | -0.2585***          | -0.2592***            |
| CALIBVEISION              | (0.0277)            | (0.0269)             | (0.0274)             | (0.0260)            | (0.0275)            | (0.0280)              |
|                           | (0.0211)            | (0.0209)             | (0.0214)             | (0.0200)            | (0.0213)            | (0.0200)              |

### Smoking Initiation – Peers and Personality

One may worry that our dichotomization of personality in strong/weak is arbitrary. We have additionally estimated a model with linear interaction terms between the peer effect and personality.

$$y_{i,g} = \lambda_1 \sum_{j \neq i} w_{ij,g} y_{j,g} s_{i,g} + \lambda_2 \sum_{j \neq i} w_{ij,g} y_{j,g} s_{j,g} + \lambda_3 \sum_{j \neq i} w_{ij,g} y_{j,g} s_{i,g} s_{j,g} + \cdots$$

|                           | Smok      | e Dummy  | Smoke      | Frequency |
|---------------------------|-----------|----------|------------|-----------|
|                           | ES        | СО       | ES         | СО        |
| Endogenous Effect         |           |          |            |           |
| $\lambda_1$               | -0.0168*  | -0.0099  | -0.0524*** | -0.0170   |
|                           | (0.0101)  | (0.0094) | (0.0114)   | (0.0101)  |
| $\lambda_2$               | -0.0261** | -0.0069  | -0.0204    | -0.0074   |
|                           | (0.0133)  | (0.0123) | (0.0135)   | (0.0116)  |
| $\lambda_3$               | 0.0255**  | 0.0147   | 0.0169     | 0.0281*** |
| -                         | (0.0129)  | (0.0105) | (0.0141)   | (0.0104)  |
| Own & Contextual effects  | Yes       | Yes      | Yes        | Yes       |
| Endogenous link formation | Yes       | Yes      | Yes        | Yes       |
| Group fixed effects       | Yes       | Yes      | Yes        | Yes       |
| $\sigma_u^2$              | 0.1298    | 0.1335   | 3.7602     | 3.5071    |

### Smoking Initiation - Peers and Personality

- The results indicate that individuals who are emotionally unstable face larger peer effects compared to individuals who are emotionally stable.
- For conscientiousness we do not find a similar pattern.
- Although it seems extremely difficult to manipulate the composition of peer groups on basis of personality, the results do suggest that interventions aimed at groups of emotionally unstable individuals have the largest scope in reducing the uptake of smoking and other unhealthy behaviors in adolescence.

# Gender and Racial Peer Effects with Endogenous Network Formation (Hsie

- Many existing studies focus only on the average magnitude of peer influences, without paying attention to the possible heterogeneous nature of peer effects along the dimensions of race and gender.
- To shed light on the debate on single-sex versus coeducational schooling, we need to know the mechanism of peer effects along the gender dimension.
- Another example is the debate on school segregation versus desegregation, which calls for the analysis on the mechanism of peer interactions within and across racial groups.

### Gender and Racial Peer Effects with Endogenous Network Formation

Table: Gender Peer Effects on GPA

|                     | Model (1) | Model (2) | Model (3) | Model (4) | Model (5) |
|---------------------|-----------|-----------|-----------|-----------|-----------|
| Endogenous effects: |           |           |           |           |           |
| $\lambda_{\it ff}$  | 0.140***  | 0.136***  | 0.136***  | 0.109***  | 0.102***  |
|                     | (0.024)   | (0.023)   | (0.024)   | (0.024)   | (0.022)   |
| $\lambda_{\it fm}$  | 0.025     | 0.025     | `0.019    | 0.013     | 0.002     |
|                     | (0.020)   | (0.020)   | (0.020)   | (0.020)   | (0.019)   |
| $\lambda_{mm}$      | 0.111***  | 0.109***  | 0.101***  | 0.077***  | 0.061**   |
|                     | (0.024)   | (0.025)   | (0.024)   | (0.025)   | (0.024)   |
| $\lambda_{mf}$      | 0.081***  | 0.078***  | 0.079***  | 0.067***  | 0.060***  |
|                     | (0.021)   | (0.020)   | (0.021)   | (0.020)   | (0.020)   |

# Gender and Racial Peer Effects with Endogenous Network Formation

#### Table: Gender Peer Effects on smoking

|                     | Model (1)              | Model (2)              | Model (3)              | Model (4)              | Model (5)              |
|---------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
| Endogenous effects: |                        |                        |                        |                        |                        |
| $\lambda_{ff}$      | 0.479***               | 0.476***               | 0.476***               | 0.477***               | 0.487***               |
|                     | (0.031)                | (0.031)                | (0.032)                | (0.031)                | (0.031)                |
| $\lambda_{fm}$      | `0.198 <sup>*</sup> ** | `0.198***              | `0.198***              | `0.198***              | `0.203 <sup>*</sup> ** |
|                     | (0.034)                | (0.034)                | (0.034)                | (0.034)                | (0.034)                |
| $\lambda_{mm}$      | 0.320***               | 0.322***               | 0.320***               | `0.318 <sup>*</sup> ** | `0.325 <sup>*</sup> ** |
|                     | (0.038)                | (0.038)                | (0.038)                | (0.038)                | (0.038)                |
| $\lambda_{mf}$      | 0.233***               | `0.232 <sup>*</sup> ** | `0.232 <sup>*</sup> ** | `0.231***              | 0.238***               |
| ****                | (0.037)                | (0.037)                | (0.037)                | (0.037)                | (0.037)                |

## Gender and Racial Peer Effects with Endogenous Network Formation

#### Table: Racial Peer Effects on GPA

|                     | Model (1)             | Model (2)             | Model (3)             | Model (4)             | Model (5)           |
|---------------------|-----------------------|-----------------------|-----------------------|-----------------------|---------------------|
| Endogenous effects: |                       |                       |                       |                       |                     |
| $\lambda_{ww}$      | 0.253***              | 0.255***              | 0.243***              | 0.194***              | 0.175***            |
|                     | (0.028)               | (0.029)               | (0.026)               | (0.028)               | (0.029)             |
| $\lambda_{wb}$      | -0.025                | -0.027                | -0.029                | -0.025                | -0.033              |
|                     | (0.026)               | (0.027)               | (0.027)               | (0.027)               | (0.027)             |
| $\lambda_{wo}$      | -0.036 <sup>*</sup> * | _0.036 <sup>*</sup> * | _0.034 <sup>*</sup> * | -0.033 <sup>*</sup> * | -0.029**            |
|                     | (0.017)               | (0.018)               | (0.018)               | (0.017)               | (0.017)             |
| $\lambda_{bb}$      | 0.112***              | 0.106***              | 0.105**               | 0.079*                | 0.058               |
|                     | (0.040)               | (0.040)               | (0.042)               | (0.042)               | (0.039)             |
| $\lambda_{bw}$      | 0.124***              | 0.118***              | 0.120***              | 0.098***              | 0.087**             |
|                     | (0.037)               | (0.037)               | (0.037)               | (0.036)               | (0.037)             |
| $\lambda_{bo}$      | 0.036                 | 0.039                 | 0.032                 | 0.013                 | 0.016               |
|                     | (0.033)               | (0.034)               | (0.033)               | (0.033)               | (0.033)             |
| $\lambda_{oo}$      | 0.022                 | 0.021                 | 0.019                 | 0.010                 | 0.006               |
|                     | (0.032)               | (0.030)               | (0.029)               | (0.029)               | (0.030)             |
| $\lambda_{ow}$      | 0.189***              | 0.189***              | 0.180***              | 0.139***              | 0.141***            |
|                     | (0.034)               | (0.036)               | (0.034)               | (0.035)               | (0.037)             |
| $\lambda_{ob}$      | $-0.014^{'}$          | $-0.014^{'}$          | $-0.024^{'}$          | _0.029 <sup>′</sup>   | _0.027 <sup>^</sup> |
|                     | (0.040)               | (0.040)               | (0.040)               | (0.041)               | (0.039)             |

# Gender and Racial Peer Effects with Endogenous Network Formation (

#### Table: Racial Peer Effects on smoking

|                     | Model (1)    | Model (2)             | Model (3)        | Model (4) | Model (5)    |
|---------------------|--------------|-----------------------|------------------|-----------|--------------|
| Endogenous effects: |              |                       |                  |           |              |
| $\lambda_{ww}$      | 0.507***     | 0.508***              | 0.513***         | 0.511***  | 0.520***     |
|                     | (0.029)      | (0.029)               | (0.028)          | (0.029)   | (0.029)      |
| $\lambda_{wb}$      | -0.019       | -0.017                | -0.024           | -0.028    | -0.012       |
|                     | (0.056)      | (0.056)               | (0.057)          | (0.056)   | (0.057)      |
| $\lambda_{wo}$      | 0.126***     | 0.124***              | 0.128***         | 0.127***  | 0.134***     |
|                     | (0.030)      | (0.030)               | (0.030)          | (0.030)   | (0.031)      |
| $\lambda_{bb}$      | 0.078        | 0.069                 | 0.083            | 0.097     | 0.055        |
|                     | (0.102)      | (0.102)               | (0.100)          | (0.100)   | (0.100)      |
| $\lambda_{bw}$      | 0.372***     | 0.364 <sup>*</sup> ** | 0.385***         | 0.382***  | 0.378***     |
|                     | (0.087)      | (0.085)               | (0.085)          | (0.085)   | (0.086)      |
| $\lambda_{bo}$      | 0.203        | 0.196                 | 0.206            | 0.176     | 0.160        |
|                     | (0.169)      | (0.171)               | (0.172)          | (0.172)   | (0.170)      |
| $\lambda_{oo}$      | 0.330***     | 0.328***              | 0.332***         | 0.321***  | 0.337***     |
|                     | (0.073)      | (0.072)               | (0.073)          | (0.072)   | (0.072)      |
| $\lambda_{ow}$      | 0.365***     | 0.360***              | 0.380***         | 0.370***  | 0.373***     |
|                     | (0.070)      | (0.069)               | (0.069)          | (0.072)   | (0.070)      |
| $\lambda_{ob}$      | $-0.185^{*}$ | $-0.177^{'}$          | $-0.173^{\circ}$ | -0.164    | $-0.175^{'}$ |
|                     | (0.110)      | (0.109)               | (0.108)          | (0.110)   | (0.111)      |

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