

# AVL Trees

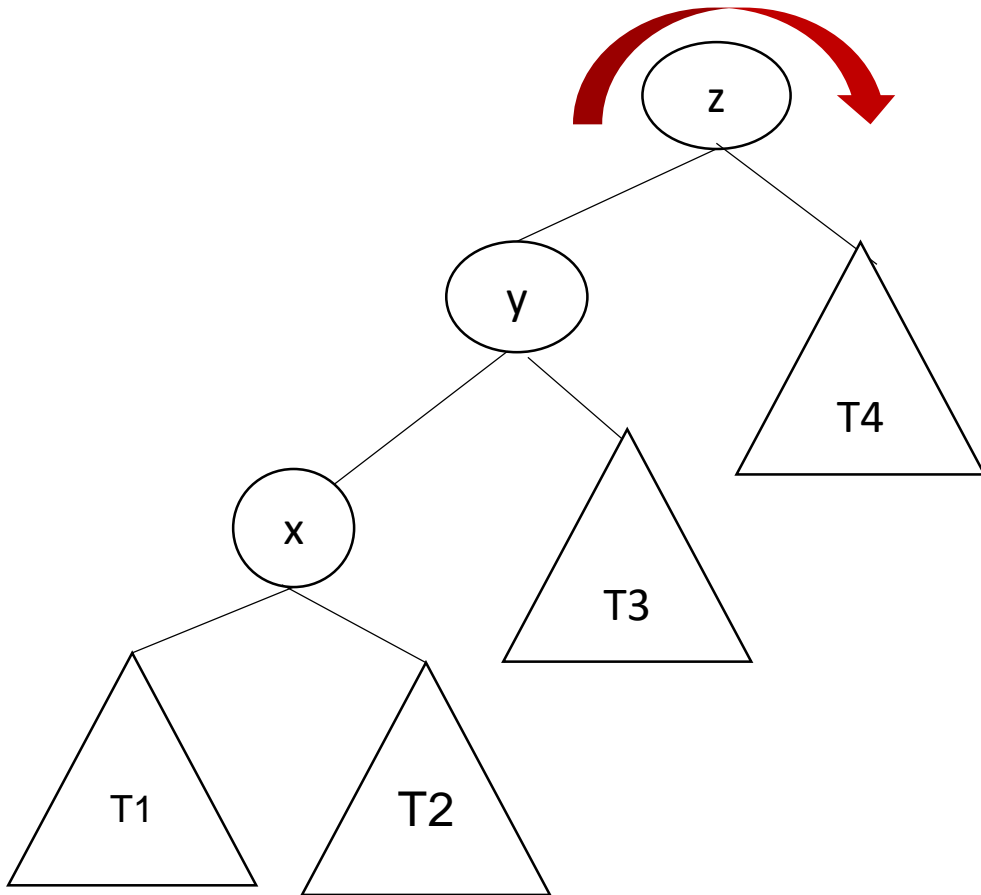
( Adelson, Velskii and Landis)

# Rotations

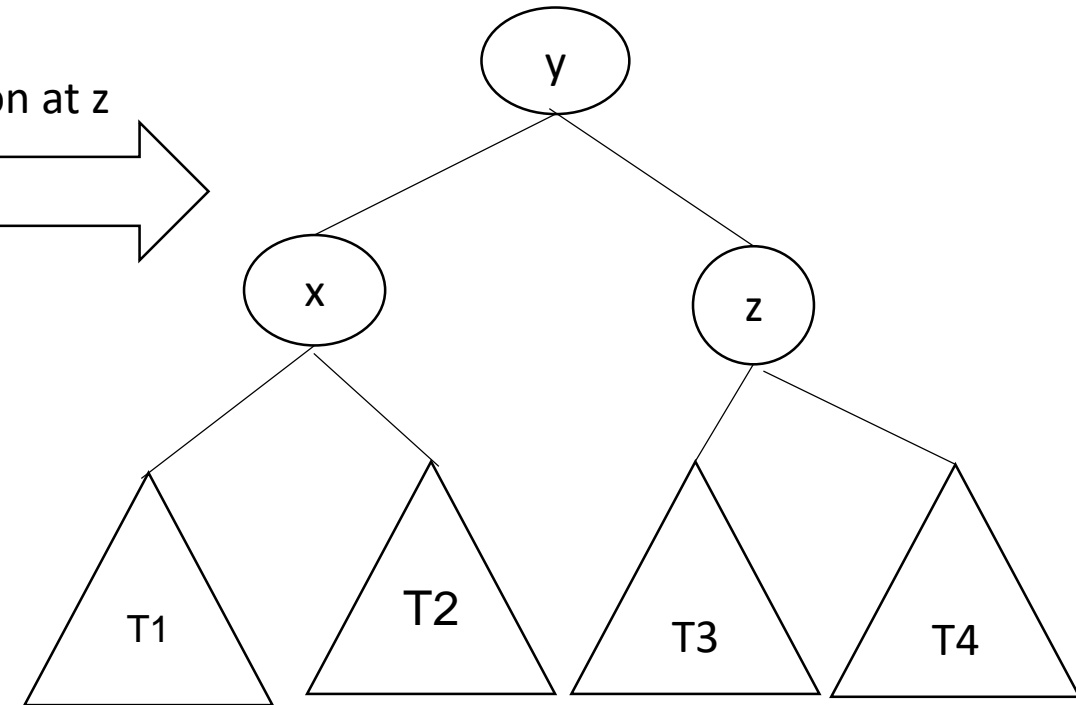
- Rotations – Single and Double
- Single Rotation – Left , Right
- Double – Left Right , Right Left

# Right Rotation

- Required when the inserted node is in Left-Left- Branch of unbalanced node (z)

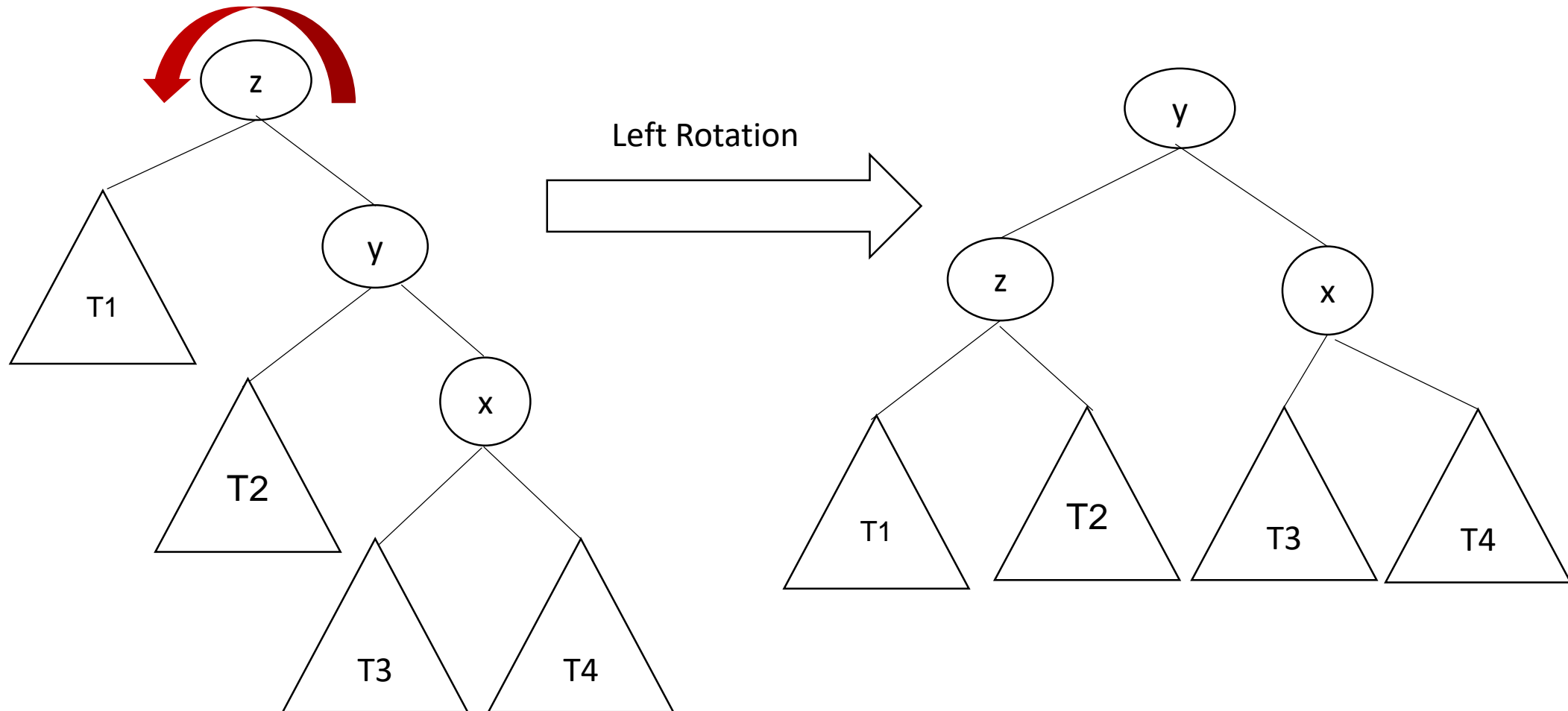


Right Rotation at z



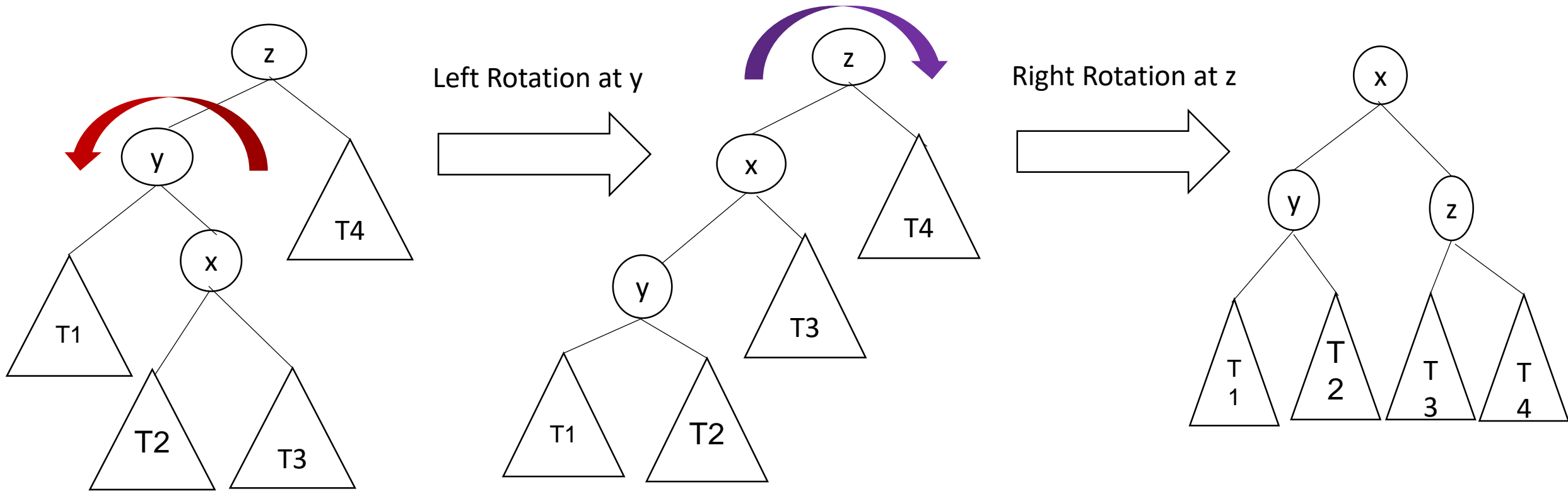
# Left Rotation

- Required when the inserted node is in Right-Right- Branch of unbalanced node (z)



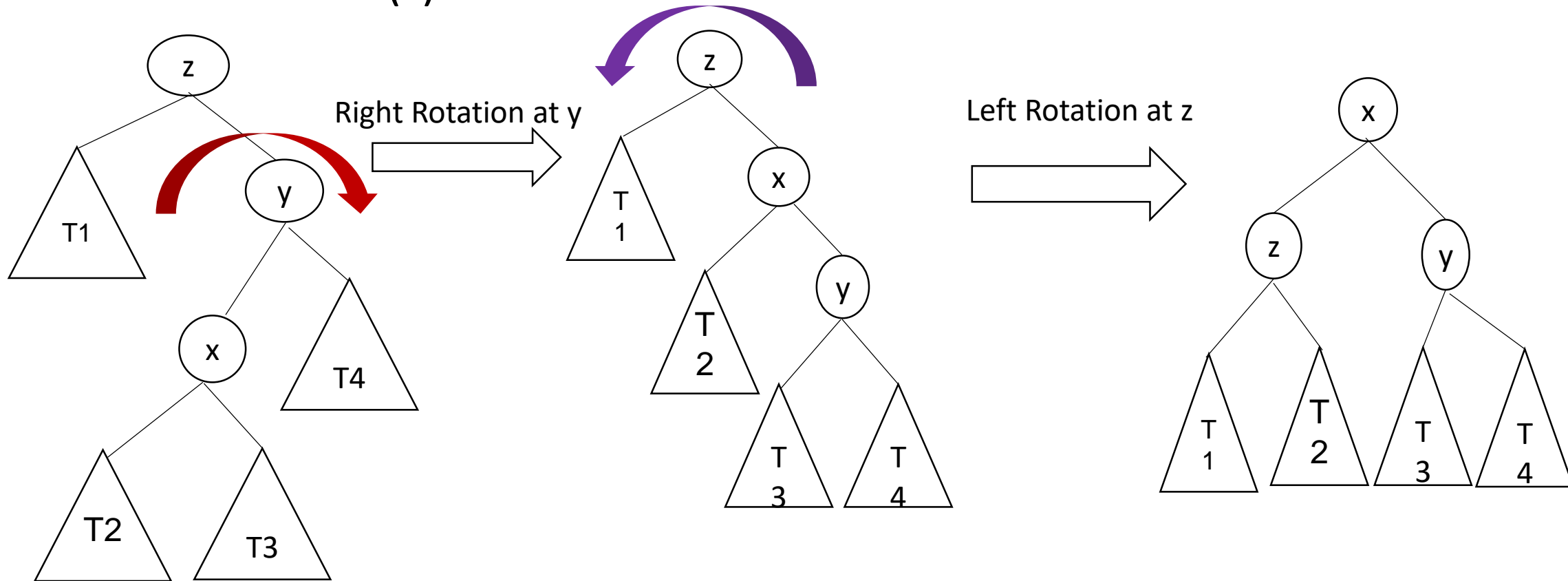
# Left Right Rotation

- Required when the inserted node is in Left-Right- Branch of unbalanced node (z)



# Right Left Rotation

- Required when the inserted node is in Right – Left Branch of unbalanced node (z)



# Insertion

1. Let  $w$  be the inserted node
2. Starting from  $w$ , travel up and find the first unbalanced node  $z$
3. Let  $y$  be the child of  $z$  and  $x$  be the grandchild of  $x$  – in the path from  $w$  to  $z$
4. Rebalance using any one of the rotations

# Deletion

1. Perform BST delete for  $w$  (node deleted)
2. Starting from  $w$ , travel up and find the first unbalanced node  $z$
3. Let  $y$  be the larger height child of  $z$  and  
     $x$  be the larger height child of  $y$
4. Rebalance using appropriate rotation as in insertion
5. After rotation at  $z$ , may have to perform rotation at ancestors of  $z$ 
  - must continue to trace the path until we reach the root