

# Parametric Cubic Intersection

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Given two parametric curves:

$$x_1(t_1) = a_{x1} t_1^3 + b_{x1} t_1^2 + c_{x1} t_1 + d_{x1}$$

$$y_1(t_1) = a_{y1} t_1^3 + b_{y1} t_1^2 + c_{y1} t_1 + d_{y1}$$

$$x_2(t_2) = a_{x2} t_2^3 + b_{x2} t_2^2 + c_{x2} t_2 + d_{x2}$$

$$y_2(t_2) = a_{y2} t_2^3 + b_{y2} t_2^2 + c_{y2} t_2 + d_{y2}$$

This document outlines the derivation of the closed form polynomial that identifies where these two curves intersect.

The goal is to identify points that these curves have in common. So we need to identify where the coordinate  $(x_1, y_1)$  equals  $(x_2, y_2)$ . Algebraically this means we're looking at the following system (where  $x_1 = x_2$  and  $y_1 = y_2$ ):

$$a_{x1} t_1^3 + b_{x1} t_1^2 + c_{x1} t_1 + d_{x1} = a_{x2} t_2^3 + b_{x2} t_2^2 + c_{x2} t_2 + d_{x2}$$

$$a_{y1} t_1^3 + b_{y1} t_1^2 + c_{y1} t_1 + d_{y1} = a_{y2} t_2^3 + b_{y2} t_2^2 + c_{y2} t_2 + d_{y2}$$

# 1 Cubic Formula

There are multiple ways to solve a cubic equation. This section derives the cubic formula we will use using the Tschirnhaus Transformation and Vieta's Substitution. Our initial equation is:

$$x^3 + bx^2 + cx + d = 0$$

## 1.1 Apply Tschirnhaus Transformation:

Apply the Tschirnhaus Transformation:  $z = x + \frac{b}{3}$

$x^3 + bx^2 + cx + d = 0$	(Given.)
$(z - \frac{b}{3})^3 + b(z - \frac{b}{3})^2 + c(z - \frac{b}{3}) + d = 0$	Substitute $x = z - \frac{b}{3}$ .
$(z^3 - 3z^2\frac{b}{3} + 3z\frac{b^2}{9} - \frac{b^3}{27}) + b(z^2 - 2z\frac{b}{3} + \frac{b^2}{9}) + c(z - \frac{b}{3}) + d = 0$	Expand powers.
$(z^3 - z^2b + z\frac{b^2}{3} - \frac{b^3}{27}) + (z^2b - 2z\frac{b^2}{3} + \frac{b^3}{9}) + (zc - c\frac{b}{3}) + d = 0$	Distribute coefficients.
$z^3 + z^2(-b + b) + z(\frac{b^2}{3} - 2\frac{b^2}{3} + c) + (\frac{-b^3}{27} + \frac{b^3}{9} - c\frac{b}{3} + d) = 0$	Factor $z$ terms.
$z^3 + z(\frac{-b^2}{3} + c) + (\frac{2b^3}{27} - \frac{bc}{3} + d) = 0$	Simplify.

Now we have a depressed cubic (that is: there is no term  $z^2$ ). Let's introduce a couple of new variables to clean up the equation:

$$C = \frac{-b^2}{3} + c$$

$$D = \frac{2b^3}{27} - \frac{bc}{3} + d$$

$$z^3 + Cz + D = 0$$

## 1.2 Use Vieta's substitution:

Use Vieta's substitution:  $z = w - \frac{C}{3w}$

Towards the end of this derivation we introduce  $j$  and  $k$ , which will prove helpful later on.

$z^3 + C z + D = 0$	(Given.)
$(w - \frac{C}{3w})^3 + C (w - \frac{C}{3w}) + D = 0$	Substitute $z = w - \frac{C}{3w}$ .
$(w^3 - 3 w^2 \frac{C}{3w} + 3 w \frac{C^2}{9w^2} - \frac{C^3}{27w^3}) + C (w - \frac{C}{3w}) + D = 0$	Expand powers.
$w^3 - w C + \frac{C^2}{3w} - \frac{C^3}{27w^3} + w C - \frac{C^2}{3w} + D = 0$	Remove parentheses.
$w^3 + D - \frac{C^3}{27w^3} = 0$	Simplify.
$w^6 + D w^3 - \frac{C^3}{27} = 0$	Multiply by $w^3$
$w^3 = \frac{-D \pm \sqrt{D^2 + 4C^3/27}}{2}$	Apply the quadratic formula.
$w^3 = \frac{-D}{2} \pm \sqrt{\frac{D^2}{4} + \frac{C^3}{27}}$	Simplify.
$j = \pm \sqrt{\frac{D^2}{4} + \frac{C^3}{27}}$	Define $j$ .
$k = \frac{-D}{2} + j$	Define $k$ .
$w^3 = k$	Substitute $k$ .
$w = k^{1/3}$	Solve for $w$ .

State  $x$  in terms of  $w$ :

$z = w - \frac{C}{3w}$	(Given.)
$z = x + \frac{b}{3}$	(Given.)
$x + \frac{b}{3} = w - \frac{C}{3w}$	Transitive property.
$x = w - \frac{C}{3w} - \frac{b}{3}$	Subtract $\frac{b}{3}$ .

## 2 Fractional Cubic Root Elimination

This section addresses an obstacle that will appear shortly. Here we eliminate the fractional roots in this equation:

$$c_1 k^{1/3} + c_2 k^{2/3} = z$$

(I'm not sure if this transformation has a more official name, but I'll refer to it here simply as "Fractional Cubic Root Elimination".)

$c_1 k^{1/3} + c_2 k^{2/3} + c_3 = 0$	(Given.)
$c_1 k^{1/3} (1 + \frac{c_2}{c_1} k^{1/3}) = -c_3$	Factor the left-hand side by $c_1 k^{1/3}$ .
$1 + \frac{c_2}{c_1} k^{1/3} = \frac{-c_3}{c_1 k^{1/3}}$	Divide both sides by $c_1 k^{1/3}$ .
$1 + 3 \frac{c_2}{c_1} k^{1/3} + 3 \frac{c_2^2}{c_1^2} k^{2/3} + \frac{c_2^3}{c_1^3} k = \frac{(-c_3)^3}{c_1^3 k}$	Cube both sides of the equation.
$c_1^3 k + 3 c_1^2 c_2 k^{4/3} + 3 c_1 c_2^2 k^{5/3} + c_2^3 k^2 = -c_3^3$	Multiply both sides by $c_1^3 k$ .
$3 c_1^2 c_2 k^{4/3} + 3 c_1 c_2^2 k^{5/3} = -c_3^3 - c_1^3 k - c_2^3 k^2$	Isolate fractional exponents.
$c_1 k^{1/3} + c_2 k^{2/3} = \frac{-c_3^3 - c_1^3 k - c_2^3 k^2}{3 c_1 c_2 k}$	Divide by $3 c_1 c_2 k$ .

The left-hand side of the last equation resembles to the left-hand of the first equation, so it follows that:

$$\frac{-c_3^3 - c_1^3 k - c_2^3 k^2}{3 c_1 c_2 k} = -c_3$$

So when we encounter the first equation, we can replace it with this equivalent equation:

$$-c_3^3 - c_1^3 k - c_2^3 k^2 + 3 c_1 c_2 c_3 k = 0$$

### 3 Derivation

The previous two sections outlined formulas/transformations that will be used to address the original problem. This section details the actual derivation. The end goal is a single polynomial expression that identifies where two curves intersect, and the beginning equations are:

$$\begin{aligned} a_{x1} t_1^3 + b_{x1} t_1^2 + c_{x1} t_1 + d_{x1} &= a_{x2} t_2^3 + b_{x2} t_2^2 + c_{x2} t_2 + d_{x2} \\ a_{y1} t_1^3 + b_{y1} t_1^2 + c_{y1} t_1 + d_{y1} &= a_{y2} t_2^3 + b_{y2} t_2^2 + c_{y2} t_2 + d_{y2} \end{aligned}$$

Starting with:

$$a_{x1} t_1^3 + b_{x1} t_1^2 + c_{x1} t_1 + (d_{x1} - a_{x2} t_2^3 - b_{x2} t_2^2 - c_{x2} t_2 - d_{x2}) = 0$$

Introduce a few variables to simplify this equation:

$$\begin{aligned} a &= \frac{b_{x1}}{a_{x1}} \\ b &= \frac{c_{x1}}{a_{x1}} \\ c &= \frac{d_{x1}}{a_{x1}} + \frac{-a_{x2} t_2^3}{a_{x1}} + \frac{-b_{x2} t_2^2}{a_{x1}} + \frac{-c_{x2} t_2}{a_{x1}} + \frac{-d_{x2}}{a_{x1}} \\ t_1^3 + a t_1^2 + b t_1 + c &= 0 \end{aligned}$$

Apply a Tschirnhaus transform by substituting  $t_1 = z + \frac{-a}{3}$ :

$$z^3 + z \left( \frac{-a^2}{3} + b \right) + \left( \frac{2a^3}{27} + c + \frac{-ab}{3} \right) = 0$$

Introduce a few more variables to simplify this equation:

$$\begin{aligned} p &= \left( \frac{-a^2}{3} + b \right) \\ q &= \left( \frac{2a^3}{27} + c + \frac{-ab}{3} \right) = 0 \\ z^3 + p z + q &= 0 \end{aligned}$$

Apply Vieta's Substitution,  $z = m + \frac{-p}{3m}$ :

$$m^3 + q + \frac{-p^3}{27} m^{-3} = 0$$

Define  $m = k^{1/3}$ :

$$k + q + \frac{-p^3}{27} k^{-1} = 0$$

Multiply by  $k$  to produce a simple quadratic equation:

$$k^2 + q k + \frac{-p^3}{27}$$

We can apply the quadratic formula to this equation to solve for  $k$ :

$$v = \frac{q^2}{4} + \frac{p^3}{27}$$

$$k = \frac{-q}{2} + v^{1/2}$$

Combine the definitions used for the Tschirnhaus transform, the Vieta substitution, and  $m$  to redefine  $t_1$ :

$$t_1 = k^{1/3} + \frac{-a}{3} + \frac{-p}{3} k^{-1/3} = 0$$

Now reconsider the  $y$ -equation:

$$a_{y1} t_1^3 + b_{y1} t_1^2 + c_{y1} t_1 + (d_{y1} - a_{y2} t_2^3 - b_{y2} t_2^2 - c_{y2} t_2 - d_{y2}) = 0$$

Substitute in our new definition of  $t_1$ :

$$\begin{aligned} & -a_{y2} t_2^3 + -b_{y2} t_2^2 + -c_{y2} t_2 + (d_{y1} - d_{y2} + \frac{-a^3 a_{y1}}{27} + a_{y1} k + \frac{a^2 b_{y1}}{9} + \frac{-2 b_{y1} p}{3} + b_{y1} k^{2/3} + \\ & \frac{-a c_{y1}}{3} + c_{y1} k^{1/3} + \frac{2 a a_{y1} p}{3} - a a_{y1} k^{2/3} + \frac{a^2 a_{y1} k^{1/3}}{3} - a_{y1} k^{1/3} p + \frac{a_{y1} p^2}{3 k^{1/3}} + \frac{-a_{y1} p^3}{27 k} + \frac{-2 a b_{y1} k^{1/3}}{3} + \\ & \frac{b_{y1} p^2}{9 k^{2/3}} + \frac{-c_{y1} p}{3 k^{1/3}} + \frac{-a a_{y1} p^2}{9 k^{2/3}} + \frac{-a^2 a_{y1} p}{9 k^{1/3}} + \frac{2 a b_{y1} p}{9 k^{1/3}}) = 0 \end{aligned}$$

However  $k$  is expressed as a cubic root, so we have to apply a fractional cubic root elimination. This means everything has to be cubed.

Then there is also a square root inside  $k$ , so we have to tease that out: so we'll have to square everything to resolve  $v$ .

We'll also have to apply all the substitutions we previously made to simplify this equation. The end result is an equation that is 42055-many terms long, so the next section is devoted simply to stating the  $c$  coefficients in this equation:

$$c_{18} t_2^{18} + c_{17} t_2^{17} + c_{16} t_2^{16} + c_{15} t_2^{15} + c_{14} t_2^{14} + c_{13} t_2^{13} + \dots + c_3 t_2^3 + c_2 t_2^2 + c_1 t_2 + c_0 = 0$$

In this equation all the  $c$  terms are expressed in terms of the constants ( $a_{x1}$ ,  $b_{x1}$ ,  $c_{x1}$  etc.) used to define the two cubic parametric curves, so the only remaining variable is  $t_2$ .

## 4 Coefficient Definitions

This section states the definition of coefficients in this equation:

$$c_{18} t_2^{18} + c_{17} t_2^{17} + c_{16} t_2^{16} + c_{15} t_2^{15} + c_{14} t_2^{14} + c_{13} t_2^{13} + \dots + c_3 t_2^3 + c_2 t_2^2 + c_1 t_2 + c_0 = 0$$

$$\begin{aligned} c_0 = & (a_{x1} d_{y1} - a_{y1} d_{x1})^6 - 6(a_{x1} d_{y1} - a_{y1} d_{x1})^5 (a_{x1} d_{y2} - a_{y1} d_{x2}) + (a_{x1} d_{y2} - a_{y1} d_{x2})^6 + \\ & (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^4 + (a_{x1} c_{y1} - \\ & a_{y1} c_{x1})^4 (c_{x1} d_{y2} - c_{y1} d_{x2})^2 + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})^4 - 2(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (c_{x1} d_{y1} - \\ & c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\ & 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^3 - 6(a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^5 + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 15(a_{x1} d_{y1} - a_{y1} d_{x1})^4 (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^2 + 15(a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^4 - 20(a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^3 + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\ & b_{y1} c_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2})^2 + 7(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + \\ & 2(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 1(a_{x1} d_{y1} - a_{y1} d_{x1})^4 (b_{x1} c_{y1} - \\ & b_{y1} c_{x1})^2 + 3(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (d_{x1} d_{y2} - d_{x2} d_{y1})^2 + 7(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2})^2 + 2(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - \\ & 1(a_{x1} d_{y2} - a_{y1} d_{x2})^4 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 2(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (c_{x1} d_{y2} - \\ & c_{y1} d_{x2}) - 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - \\ & 8(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12(a_{x1} c_{y1} - \\ & a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 2(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\ & a_{y1} d_{x1})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) + 2(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) + \\ & 2(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 8(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\ & a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 2(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} d_{y2} - \\ & b_{y1} d_{x2})^2 + 2(a_{x1} d_{y2} - a_{y1} d_{x2})^5 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 2(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} d_{y1} - \\ & b_{y1} d_{x1})^2 + 6(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^4 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 2(a_{x1} d_{y1} - a_{y1} d_{x1})^5 (b_{x1} c_{y1} - \\ & b_{y1} c_{x1}) + 10(a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^4 (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - \\ & a_{y1} d_{x1})^4 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 20(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^4 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\ & 4(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - \\ & 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (d_{x1} d_{y2} - d_{x2} d_{y1}) + 6(a_{x1} b_{y1} - \\ & a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 10(a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^4 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (d_{x1} d_{y2} - \\ & d_{x2} d_{y1}) - 30(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^4 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\ & b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^3 (d_{x1} d_{y2} - d_{x2} d_{y1}) - 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) (d_{x1} d_{y2} - \\ & d_{x2} d_{y1}) - 20(a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 2(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\ & b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 60(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 2(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (c_{x1} d_{y1} - \\ & c_{y1} d_{x1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - \end{aligned}$$





$$\begin{aligned}
& c_{y1} d_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) - 10 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (c_{x1} d_{y1} - c_{y1} d_{x1})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) + \\
& 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (c_{x1} d_{y1} - c_{y1} d_{x1})^3 + 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (d_{x1} d_{y2} - d_{x2} d_{y1})^2 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 42 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2})
\end{aligned}$$

$$\begin{aligned}
c_1 = & 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^3 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^3 - \\
& 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 6 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^5 + 30 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^4 (a_{x1} d_{y2} - a_{y1} d_{x2}) - 60 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + 60 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^3 - \\
& 30 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^4 + 6 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^5 - 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^4 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 32 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 8 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 144 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 96 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} -
\end{aligned}$$



$$\begin{aligned}
& c_{y1} d_{x2})^2 - 2(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 16(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})(d_{x1} d_{y2} - d_{x2} d_{y1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})(c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})(c_{x2} d_{y2} - c_{y2} d_{x2})(d_{x1} d_{y2} - d_{x2} d_{y1}) + \\
& 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})(c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 6(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 36(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})(b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 4(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2}) + \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2})^2 + \\
& 12(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} d_{y1} - b_{y1} d_{x1})(c_{y2} d_{x1} - c_{x2} d_{y1}) - 10(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})(b_{x1} c_{y1} - b_{y1} c_{x1})(c_{y2} d_{x1} - c_{x2} d_{y1}) + 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1})(c_{x1} d_{y1} - c_{y1} d_{x1}) - 8(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})(b_{x1} c_{y1} - b_{y1} c_{x1})(c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})(c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})(c_{x1} c_{y2} - c_{x2} c_{y1})(c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} c_{y1} - b_{y1} c_{x1})(d_{x1} d_{y2} - d_{x2} d_{y1}) + 8(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1})(c_{x1} d_{y1} - c_{y1} d_{x1})(c_{y2} d_{x1} - c_{x2} d_{y1}) + 8(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})^3 + 18(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1})(c_{x1} c_{y2} - \\
& c_{x2} c_{y1})(d_{x1} d_{y2} - d_{x2} d_{y1}) - 54(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})(b_{x1} d_{y1} - b_{y1} d_{x1})(b_{x1} d_{y2} - \\
& b_{y1} d_{x2})(c_{x1} c_{y2} - c_{x2} c_{y1}) - 16(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1})(c_{y2} d_{x1} - c_{x2} d_{y1})(d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})(b_{x1} c_{y1} - b_{y1} c_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2})(c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})(b_{x1} c_{y1} - b_{y1} c_{x1})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2}) - 6(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} d_{y2} - b_{y1} d_{x2})(c_{x2} d_{y2} - c_{y2} d_{x2}) - 4(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2})(c_{x1} c_{y2} - c_{x2} c_{y1}) + 10(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})(b_{x1} c_{y2} - b_{y1} c_{x2})(c_{x1} d_{y2} - c_{y1} d_{x2}) - 8(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2})(c_{x1} d_{y2} - \\
& c_{y1} d_{x2})(d_{x1} d_{y2} - d_{x2} d_{y1}) - 28(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2})(c_{x1} c_{y2} - c_{x2} c_{y1})(d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2})(c_{x1} d_{y2} - c_{y1} d_{x2})(c_{y2} d_{x1} - c_{x2} d_{y1}) + \\
& 30(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 24(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 8(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2})(c_{x1} d_{y2} - c_{y1} d_{x2})(c_{x2} d_{y2} - c_{y2} d_{x2}) - 8(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2})^3 + 8(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})(b_{x1} c_{y2} - b_{y1} c_{x2}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 12(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} c_{y1} - b_{y1} c_{x1})^2 + \\
& 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y2} - b_{y1} d_{x2}) + 12(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y2} - a_{y1} d_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 42(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{x1} d_{y1} - a_{y1} d_{x1})(c_{x1} d_{y1} - c_{y1} d_{x1})(c_{x2} d_{y2} - c_{y2} d_{x2}) + 36(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (c_{x2} d_{y2} - c_{y2} d_{x2})(d_{x1} d_{y2} - d_{x2} d_{y1}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - \\
& a_{y1} d_{x1})(b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 12(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x1} d_{y1} - a_{y1} d_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 -
\end{aligned}$$

$$\begin{aligned}
& 8(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^3(b_{x1}c_{y1} - b_{y1}c_{x1})(b_{x1}c_{y2} - b_{y1}c_{x2}) + 12(a_{x1}c_{y1} - a_{y1}c_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^2(b_{x1}c_{y2} - b_{y1}c_{x2})(b_{x1}d_{y2} - b_{y1}d_{x2}) - 6(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})(c_{x1}d_{y2} - c_{y1}d_{x2})(c_{x2}d_{y2} - c_{y2}d_{x2}) + 8(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y1} - a_{y1}d_{x1})^3(c_{x2}d_{y2} - c_{y2}d_{x2}) - 16(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y1} - a_{y1}d_{x1})^3(a_{x1}d_{y2} - a_{y1}d_{x2})(b_{x1}c_{y2} - b_{y1}c_{x2}) - 24(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})(b_{x1}d_{y1} - b_{y1}d_{x1}) - 48(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})(c_{x1}d_{y1} - c_{y1}d_{x1}) - 12(a_{x1}c_{y1} - a_{y1}c_{x1})^3(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})(d_{x1}d_{y2} - d_{x2}d_{y1}) + 18(a_{x1}c_{y1} - a_{y1}c_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(c_{x1}d_{y2} - c_{y1}d_{x2}) - 24(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y2} - a_{y1}d_{x2})^3(b_{x1}d_{y1} - b_{y1}d_{x1}) + 24(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y1} - a_{y1}d_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^2(c_{x2}d_{y2} - c_{y2}d_{x2}) - 16(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^3(b_{x1}c_{y1} - b_{y1}c_{x1}) - 12(a_{x1}c_{y1} - a_{y1}c_{x1})^3(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y2} - a_{y1}d_{x2})^2(c_{x1}d_{y1} - c_{y1}d_{x1}) - 4(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})^2(b_{x1}c_{y2} - b_{y1}c_{x2})(d_{x1}d_{y2} - d_{x2}d_{y1}) - 8(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})(b_{x1}c_{y2} - b_{y1}c_{x2})(b_{x1}d_{y2} - b_{y1}d_{x2})(c_{x1}d_{y1} - c_{y1}d_{x1}) + 36(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^2(b_{x1}c_{y2} - b_{y1}c_{x2}) - 72(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})(b_{x1}d_{y2} - b_{y1}d_{x2}) + 72(a_{x1}c_{y1} - a_{y1}c_{x1})(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^2(b_{x1}d_{y1} - b_{y1}d_{x1})
\end{aligned}$$

$$\begin{aligned}
c_2 = & 3(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})^2(c_{x1}d_{y1} - c_{y1}d_{x1})^2 + 6(a_{x1}c_{y1} - a_{y1}c_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})^2(b_{x1}d_{y1} - b_{y1}d_{x1})^2 + 21(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}d_{y1} - a_{y1}d_{x1})^2(c_{x1}c_{y2} - c_{x2}c_{y1})^2 + 9(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})^2(c_{x1}d_{y2} - c_{y1}d_{x2})^2 + 21(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^2(c_{x1}c_{y2} - c_{x2}c_{y1})^2 - 12(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}c_{y1} - a_{y1}c_{x1})^2(c_{x2}d_{y2} - c_{y2}d_{x2})^2 + 12(a_{x1}b_{y1} - a_{y1}b_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})^2(c_{x1}d_{y2} - c_{y1}d_{x2})^2 - 6(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^2(b_{x1}c_{y1} - b_{y1}c_{x1})^2 + 6(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y2} - b_{y1}c_{x2})^2(b_{x1}d_{y1} - b_{y1}d_{x1})^2 + 6(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y2} - b_{y1}c_{x2})^2(b_{x1}d_{y2} - b_{y1}d_{x2})^2 + (a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})^2(c_{x1}c_{y2} - c_{x2}c_{y1})^2 + 15(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y1} - a_{y1}d_{x1})^4 + 90(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^2 + 15(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^4 + (a_{x1}c_{y1} - a_{y1}c_{x1})^4(c_{x1}c_{y2} - c_{x2}c_{y1})^2 - 6(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^5 + 30(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^4(a_{x1}d_{y2} - a_{y1}d_{x2}) - 60(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^3(a_{x1}d_{y2} - a_{y1}d_{x2})^2 - 60(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y1} - a_{y1}d_{x1})^3(a_{x1}d_{y2} - a_{y1}d_{x2}) + 60(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})^2(a_{x1}d_{y2} - a_{y1}d_{x2})^3 - 30(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y1} - a_{y1}d_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^4 - 60(a_{x1}c_{y2} - a_{y1}c_{x2})^2(a_{x1}d_{y1} - a_{y1}d_{x1})(a_{x1}d_{y2} - a_{y1}d_{x2})^3 + 6(a_{x1}b_{y2} - a_{y1}b_{x2})(a_{x1}d_{y2} - a_{y1}d_{x2})^5 - 2(a_{x1}c_{y1} - a_{y1}c_{x1})^4(b_{y2}c_{x1} - b_{x2}c_{y1})(c_{x1}d_{y1} - c_{y1}d_{x1}) - 4(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}b_{y2} - b_{x2}b_{y1})(b_{x1}d_{y1} - b_{y1}d_{x1})^3 + 12(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}b_{y2} - b_{x2}b_{y1})(b_{x1}d_{y1} - b_{y1}d_{x1})^2(b_{x1}d_{y2} - b_{y1}d_{x2}) - 12(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}b_{y2} - b_{x2}b_{y1})(b_{x1}d_{y1} - b_{y1}d_{x1})(b_{x1}d_{y2} - b_{y1}d_{x2})^2 - 12(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y2} - b_{y1}c_{x2})^2(b_{x1}d_{y1} - b_{y1}d_{x1})(b_{x1}d_{y2} - b_{y1}d_{x2}) + 2(a_{x1}c_{y1} - a_{y1}c_{x1})^4(b_{y2}c_{x1} - b_{x2}c_{y1})(c_{x1}d_{y2} - c_{y1}d_{x2}) + 4(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}b_{y2} - b_{x2}b_{y1})(b_{x1}d_{y2} - b_{y1}d_{x2})^3 + 12(a_{x1}c_{y1} - a_{y1}c_{x1})^2(a_{x1}c_{y2} - a_{y1}c_{x2})(a_{x1}d_{y2} - a_{y1}d_{x2})(b_{x1}c_{y2} - b_{y1}c_{x2})(b_{x1}d_{y2} - b_{y1}d_{x2}) + 4(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y1} - a_{y1}c_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})(b_{y2}c_{x1} - b_{x2}c_{y1})(c_{x1}d_{y1} - c_{y1}d_{x1}) - 4(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y1} - a_{y1}c_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})(b_{y2}c_{x1} - b_{x2}c_{y1})(c_{x1}d_{y2} - c_{y1}d_{x2}) - 2(a_{x1}b_{y1} - a_{y1}b_{x1})(a_{x1}c_{y1} - a_{y1}c_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})(c_{x1}c_{y2} - c_{x2}c_{y1})^2 - 2(a_{x1}b_{y1} - a_{y1}b_{x1})^2(b_{x1}c_{y1} - b_{y1}c_{x1})^2(b_{y2}c_{x1} - b_{x2}c_{y1})
\end{aligned}$$



$$\begin{aligned}
& a_{y1} b_{x1} (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 84 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 40 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 20 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 60 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 60 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2})^2 - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 64 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 60 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 10 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^4 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 8 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 42 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x2} d_{y2} - b_{y2} d_{x2}) - 6 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x2} d_{y2} - b_{y2} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 72 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 24 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) - \\
& 18 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 48 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{y2} d_{x1} - b_{x2} d_{y1}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) + 18 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) -
\end{aligned}$$

$$\begin{aligned}
& 72(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{x2}d_{y2}- \\
& c_{y2}d_{x2})-18(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(c_{x1}d_{y1}-c_{y1}d_{x1})- \\
& 24(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^3(b_{x1}c_{y2}-b_{y1}c_{x2})-4(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})^2(d_{x1}d_{y2}-d_{x2}d_{y1})+36(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}d_{y2}-b_{y1}d_{x2})-8(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y1}- \\
& b_{y1}c_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}d_{y1}-c_{y1}d_{x1})+8(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{y2}d_{x1}- \\
& b_{x2}d_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})+8(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})^3+8(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{x1}d_{y2}-b_{y1}d_{x2})(b_{x2}d_{y2}-b_{y2}d_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})- \\
& 8(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})^3+6(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^3(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})+4(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{y2}c_{x1}- \\
& b_{x2}c_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})^2-4(a_{x1}c_{y1}-a_{y1}c_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})^2+ \\
& 4(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}c_{y1}-b_{y1}c_{x1})^3+6(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})+8(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(b_{x1}c_{y2}- \\
& b_{y1}c_{x2})^2-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+ \\
& 6(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}d_{y1}-b_{y1}d_{x1})^2-8(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^3(b_{x1}c_{y2}-b_{y1}c_{x2})^2-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})(b_{y2}d_{x1}-b_{x2}d_{y1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{x2}d_{y2}- \\
& c_{y2}d_{x2})+4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})-6(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})(b_{x2}d_{y2}-b_{y2}d_{x2})-28(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})(b_{y2}c_{x1}-b_{x2}c_{y1})(d_{x1}d_{y2}-d_{x2}d_{y1})+24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})(b_{x2}d_{y2}-b_{y2}d_{x2})-30(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})^2(b_{y2}c_{x1}- \\
& b_{x2}c_{y1})+4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})+16(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})(d_{x1}d_{y2}-d_{x2}d_{y1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}d_{y1}-b_{y1}d_{x1})(d_{x1}d_{y2}-d_{x2}d_{y1})+24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})(d_{x1}d_{y2}-d_{x2}d_{y1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(b_{x2}d_{y2}-b_{y2}d_{x2})(d_{x1}d_{y2}-d_{x2}d_{y1})-24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}b_{y2}- \\
& b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})(b_{x2}d_{y2}-b_{y2}d_{x2})-24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}c_{y1}- \\
& b_{y1}c_{x1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})-6(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y2}- \\
& a_{y1}d_{x2})^2(b_{x1}d_{y1}-b_{y1}d_{x1})^2-4(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{x1}d_{y2}-b_{y1}d_{x2})(b_{y2}c_{x1}-b_{x2}c_{y1})(d_{x1}d_{y2}- \\
& d_{x2}d_{y1})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})^2(b_{y2}c_{x1}- \\
& b_{x2}c_{y1})-24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})-8(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})(d_{x1}d_{y2}-d_{x2}d_{y1})-12(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+24(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})-18(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})^2+24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})+12(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^3(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})^2+6(a_{x1}c_{y1}-a_{y1}c_{x1})^4(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{y2}d_{x1}- \\
& b_{x2}d_{y1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}-
\end{aligned}$$



$$\begin{aligned}
& b_{y1} d_{x1}) - 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 4(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 18(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 8(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2})^2 - \\
& 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12(a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 4(a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 8(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1})^2 + 2(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 8(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) - \\
& 6(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) + 2(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 8(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 16(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 2(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 + 8(a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{y2} d_{x1} - c_{x2} d_{y1})^2 - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 18(a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 18(a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 36(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 48(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 2(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - \\
& 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 6(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 10(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + \\
& 4(a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 6(a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 8 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - \\
& 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1})^2 - 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (c_{x1} c_{y2} - c_{x2} c_{y1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 30 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2})^2 - \\
& 2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - 14 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2})^2 + 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2})^2 - \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 54 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 60 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 72 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x$$



$$\begin{aligned}
& 12(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{x1}d_{y1}-c_{y1}d_{x1})- \\
& 8(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^3(c_{x1}d_{y1}-c_{y1}d_{x1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})(c_{x1}d_{y1}-c_{y1}d_{x1})+24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}d_{y1}-c_{y1}d_{x1})+24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{x1}d_{y1}-c_{y1}d_{x1})+12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(c_{x1}d_{y1}-c_{y1}d_{x1})^2-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(c_{x1}d_{y1}-c_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(c_{x1}c_{y2}-c_{x2}c_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})+4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}c_{x1}- \\
& a_{x2}c_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})(c_{x1}d_{y1}-c_{y1}d_{x1})-6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})^2-20(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(b_{x1}d_{y1}-b_{y1}d_{x1})^2+ \\
& 6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})^2(c_{x1}d_{y1}-c_{y1}d_{x1})+10(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})^2-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})^2(c_{x1}d_{y2}-c_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})^2(c_{x1}c_{y2}-c_{x2}c_{y1})+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})+ \\
& 12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})+ \\
& 24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}c_{y2}-c_{x2}c_{y1})- \\
& 4(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})+ \\
& 6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(c_{x1}d_{y2}-c_{y1}d_{x2})+24(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})+8(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^3(c_{x1}d_{y2}-c_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})-24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(b_{x1}b_{y2}- \\
& b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})+12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})^2(c_{x1}d_{y2}-c_{y1}d_{x2})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(c_{x1}c_{y2}- \\
& c_{x2}c_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})-4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y1}- \\
& b_{y1}c_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})-6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})^2-20(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(b_{x1}d_{y2}-b_{y1}d_{x2})^2+6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(b_{x1}d_{y2}-b_{y1}d_{x2})^2(c_{x1}d_{y1}-c_{y1}d_{x1})-6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})^2(c_{x1}d_{y2}-c_{y1}d_{x2})-10(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}d_{y2}- \\
& b_{y1}d_{x2})^2-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})^2(c_{x1}c_{y2}-c_{x2}c_{y1})+ \\
& 6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})^2+24(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(a_{x1}d_{y1}-a_{y1}d_{x1})(c_{x1}d_{y1}-c_{y1}d_{x1})-24(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(c_{x1}d_{y1}-c_{y1}d_{x1})^2+36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(c_{x1}d_{y1}-c_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})+36(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(c_{x1}c_{y2}-c_{x2}c_{y1})(c_{x1}d_{y1}-c_{y1}d_{x1})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})+10(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})(a_{x1}d_{y1}-a_{y1}d_{x1})^4(b_{x1}c_{y1}-b_{y1}c_{x1})+20(a_{x1}c_{y2}-a_{y1}c_{x2})^3(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}c_{y1}- \\
& b_{y1}c_{x1})-32(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(a_{x1}d_{y1}-a_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})+ \\
& 6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})-54(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})^2-84(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2})^2 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 20 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - \\
& 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 - 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 + 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1})^2 + 40 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 40 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) - 40 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^3 (b_{x2} c_{y2} - b_{y2} c_{x2}) - 88 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) + \\
& 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) - \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 72 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 144 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 48 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 120 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) - \\
& 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{y2} d_{x1} - b_{x2} d_{y1}) + \\
& 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 144 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 144 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 36 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - \\
& 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 40 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) - 24 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x2} d_{y2} - c_{y2} d_{x2}) - 16 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) - \\
& 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - \\
& 32 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (d_{x1} d_{y2} - d_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 40 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^3 - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^3 + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2})^3 - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^3 + 6 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^4 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 16 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} -
\end{aligned}$$

$$\begin{aligned}
& a_{x2} b_{y1} (b_{x1} d_{y1} - b_{y1} d_{x1})^2 + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 10(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 12(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 2(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - \\
& 4(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 16(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 16(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 4(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1})^2 + 4(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 24(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12(a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 16(a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 16(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 12(a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 12(a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 4(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 16(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2})^2 - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 2(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 10(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2})^2 + 12(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 - 2(a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 4(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - \\
& 6(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 + 4(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^4 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 36(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 16(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 36(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + \\
& 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 24(a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2})^2 - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + \\
& 30 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 40 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 48 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) - \\
& 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 30 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} -
\end{aligned}$$



$$\begin{aligned}
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 24 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 24 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^3 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 8 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 4 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 8 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2})^2 - 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 4 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^3 - 8 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) +
\end{aligned}$$

$$12(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})+12(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})-2(a_{x1}b_{y1}-a_{y1}b_{x1})^3(c_{x1}c_{y2}-c_{x2}c_{y1})^3-8(a_{x1}c_{y1}-a_{y1}c_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})-4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{x1}c_{y2}-c_{x2}c_{y1})+20(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{y2}c_{x1}-b_{x2}c_{y1})(c_{x1}c_{y2}-c_{x2}c_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})$$

$$c_4 = 30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^4+15(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^4-120(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(a_{x1}d_{y2}-a_{y1}d_{x2})-60(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^3(a_{x1}d_{y2}-a_{y1}d_{x2})-60(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^3+180(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2+90(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2+180(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})+15(a_{x1}c_{y2}-a_{y1}c_{x2})^4(a_{x1}d_{y1}-a_{y1}d_{x1})^2-120(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^3-60(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^3-180(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2-30(a_{x1}c_{y2}-a_{y1}c_{x2})^4(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})+30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^4+15(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^4+60(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^3+15(a_{x1}c_{y2}-a_{y1}c_{x2})^4(a_{x1}d_{y2}-a_{y1}d_{x2})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})^2+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})^2-24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})^2(b_{x1}d_{y1}-b_{y1}d_{x1})+2(a_{x1}c_{y1}-a_{y1}c_{x1})^4(a_{y2}c_{x1}-a_{x2}c_{y1})(c_{x1}c_{y2}-c_{x2}c_{y1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})^2+(a_{x1}c_{y1}-a_{y1}c_{x1})^4(b_{y2}c_{x1}-b_{x2}c_{y1})^2+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2(b_{x1}d_{y2}-b_{y1}d_{x2})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})^2(b_{x1}d_{y2}-b_{y1}d_{x2})+(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}c_{y2}-b_{y1}c_{x2})^4+21(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(c_{x1}d_{y1}-c_{y1}d_{x1})^2+3(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{y2}c_{x1}-b_{x2}c_{y1})^2+6(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2+21(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(c_{x1}d_{y2}-c_{y1}d_{x2})^2+3(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{y2}c_{x1}-b_{x2}c_{y1})^2+6(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2(c_{x1}c_{y2}-c_{x2}c_{y1})^2+(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}c_{y1}-b_{y1}c_{x1})^2(b_{y2}c_{x1}-b_{x2}c_{y1})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})+20(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(b_{x1}b_{y2}-b_{x2}b_{y1})^2-96(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(c_{x1}c_{y2}-c_{x2}c_{y1})-24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(b_{y2}c_{x1}-b_{x2}c_{y1})-40(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(b_{x1}c_{y1}-b_{y1}c_{x1})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})-18(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})^2+96(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{x1}c_{y2}-c_{x2}c_{y1})+144(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{y2}c_{x1}-b_{x2}c_{y1})+48(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}c_{y2}-b_{y1}c_{x2})+36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-$$





$$\begin{aligned}
& a_{y1} b_{x2} (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 48 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - \\
& 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 - 6 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{y2} d_{x1} - b_{x2} d_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^3 - 10 (a_{x1} c_{y2} - a_{y1} c_{x2})^4 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1})^2 + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2})^2 - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2})^2 + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1})^2 - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x2} d_{y2} - c_{y2} d_{x2}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 144 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^3 - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 36 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 8 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} -
\end{aligned}$$

$$\begin{aligned}
& c_{x2} d_{y1}) - 2(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 - 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 18(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 + 12(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{x2} d_{y2} - b_{y2} d_{x2}) - \\
& 8(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 12(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 2(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 12(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 12(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 - 12(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - \\
& 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) + 12(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 16(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 18(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 36(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + \\
& 18(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 18(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 - 24(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 72(a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) - 24(a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 12(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 24(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 72(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 36(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12(a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - \\
& 36 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 144 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 18 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - \\
& 18 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 12 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{y2} d_{x1} - b_{x2} d_{y1}) + 18 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2})^2 + \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y2} -
\end{aligned}$$





$$\begin{aligned}
& 144(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(c_{x2}d_{y2}- \\
& c_{y2}d_{x2})-72(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(c_{x1}c_{y2}- \\
& c_{x2}c_{y1})-72(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})+4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x2}c_{y2}- \\
& b_{y2}c_{x2})+4(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(b_{x1}c_{y1}-b_{y1}c_{x1})(b_{x2}c_{y2}-b_{y2}c_{x2})(c_{x1}c_{y2}- \\
& c_{x2}c_{y1})+48(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})+16(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}b_{x1}-a_{x2}b_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})(c_{y2}d_{x1}- \\
& c_{x2}d_{y1})+48(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x1}c_{y2}- \\
& c_{x2}c_{y1})-32(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}b_{x1}-a_{x2}b_{y1})(c_{x1}c_{y2}-c_{x2}c_{y1})(d_{x1}d_{y2}-d_{x2}d_{y1})- \\
& 4(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(d_{x1}d_{y2}-d_{x2}d_{y1})+12(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})+4(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^3(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+8(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}c_{x1}- \\
& a_{x2}c_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+12(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(a_{x2}d_{y2}-a_{y2}d_{x2})-36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(c_{x1}d_{y2}-c_{y1}d_{x2})+12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{x1}d_{y1}-a_{y1}d_{x1})(c_{x2}d_{y2}- \\
& c_{y2}d_{x2})-16(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+ \\
& 72(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x2}c_{y2}-a_{y2}c_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})- \\
& 72(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}c_{x1}-a_{x2}c_{y1})(c_{x1}c_{y2}-c_{x2}c_{y1})+ \\
& 24(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}c_{y1}-b_{y1}c_{x1})^2- \\
& 24(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})+ \\
& 72(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}d_{x1}-a_{x2}d_{y1})(c_{x1}d_{y2}-c_{y1}d_{x2})- \\
& 36(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}d_{x1}-a_{x2}d_{y1})(c_{x2}d_{y2}-c_{y2}d_{x2})
\end{aligned}$$

$$\begin{aligned}
c_5 = & 30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^4-120(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^3(a_{x1}d_{y2}-a_{y1}d_{x2})-60(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})^3-60(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^3+180(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2+180(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})+180(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})+60(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(a_{x1}d_{y1}-a_{y1}d_{x1})^2- \\
& 120(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^3-180(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2-180(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2-120(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^3(a_{x1}d_{y1}- \\
& a_{y1}d_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})-6(a_{x1}c_{y2}-a_{y1}c_{x2})^5(a_{x1}d_{y1}-a_{y1}d_{x1})+30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^4+60(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^3+ \\
& 60(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^3+60(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})^3(a_{x1}d_{y2}-a_{y1}d_{x2})^2+6(a_{x1}c_{y2}-a_{y1}c_{x2})^5(a_{x1}d_{y2}-a_{y1}d_{x2})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})^2-24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}- \\
& b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x1}d_{y2}-b_{y1}d_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}- \\
& b_{y1}c_{x2})^2(b_{x1}d_{y1}-b_{y1}d_{x1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}- \\
& b_{y1}d_{x1})+2(a_{x1}c_{y1}-a_{y1}c_{x1})^4(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{y2}c_{x1}-b_{x2}c_{y1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-
\end{aligned}$$





$$\begin{aligned}
& a_{y1} c_{x2} (b_{x1} c_{y2} - b_{y1} c_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^4 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 48 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) - 16 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + \\
& 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 2 (a_{x1} c_{y2} - a_{y1} c_{x2})^5 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2})^2 - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\
& 2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 6 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})^2 + 4 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 144 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 72 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} -
\end{aligned}$$

$$\begin{aligned}
& a_{y2} b_{x2}) - 72 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 72 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) - 72 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 18 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 4 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1})^2 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + \\
& 4 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1})^2 - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 4 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 10 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 24 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) - 84 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + \\
& 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} -
\end{aligned}$$

$$\begin{aligned}
& b_{y1} c_{x2} (c_{y2} d_{x1} - c_{x2} d_{y1}) - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - 48 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) - 30 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 132 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 18 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 204 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 16 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) - 8 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 12 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) - 16 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 + \\
& 6 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - 6 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^3 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 72 (a_{x1} a_{y2} -
\end{aligned}$$

$$\begin{aligned}
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + \\
& 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 18 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 12 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) - 18 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 8 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^4 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 24 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + \\
& 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) - 124 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 20 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 148 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1} (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 42 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^2 + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 60 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (c_{y2} d_{x1} - c_{x2} d_{y1})^2 - 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^3 - 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1})^2 - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + \\
& 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) - 16 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2})
\end{aligned}$$

$$\begin{aligned}
c_6 = & 15 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^4 - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) - 120 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^3 - \\
& 20 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 + 90 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 + 360 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} -
\end{aligned}$$





$$\begin{aligned} & (c_{x1} d_{y1} - c_{y1} d_{x1})^2 - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\ & a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 20 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} d_{y1} - b_{y1} d_{x1})^2 + \\ & 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 + 72 (a_{x1} a_{y2} - \\ & a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\ & b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\ & 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\ & 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - \\ & a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 2 (a_{x1} b_{y2} - \\ & a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - \\ & a_{x2} b_{y1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - \\ & a_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\ & a_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 20 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + \\ & 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 36 (a_{x1} a_{y2} - \\ & a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 288 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\ & a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 48 (a_{x1} b_{y1} - \\ & a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\ & a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 120 (a_{x1} a_{y2} - \\ & a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 20 (a_{x1} b_{y2} - \\ & a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 432 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\ & a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 56 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\ & a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 84 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\ & a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 42 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\ & a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 288 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\ & a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - \\ & a_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 120 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\ & a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 20 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\ & 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - \\ & a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 32 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\ & a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - \\ & a_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\ & b_{x2} b_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 84 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} c_{x1} - \\ & b_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 16 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} d_{y1} - \\ & b_{y1} d_{x1}) - 24 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\ & 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1$$



$$\begin{aligned}
& a_{x2} d_{y1} (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 6 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^4 (b_{x1} b_{y2} - b_{x2} b_{y1}) + 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) + \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} c_{x1} - b_{x2} c_{y1})^3 + 4 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^4 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - \\
& 6 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1})^2 - 14 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2})^2 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2})^2 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1})^2 + 288 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + 144 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 2 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (d_{x1} d_{y2} - d_{x2} d_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2})^2 + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1})^2 + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1})^2 + 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + \\
& 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + 36 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 2 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) - 24 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{x2} d_{y2} - b_{y2} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} d_{y1} -
\end{aligned}$$

$$\begin{aligned}
& b_{y1} d_{x1} (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 - 12 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 24 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 36 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 72 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 36 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + \\
& 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 4 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 4 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 48 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} d_{x1} - b_{x2} d_{y1}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) - 60 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - \\
& 84 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 4 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 8 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 8 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^3 - 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^3 + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 12 (a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^3 + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 4 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) + \\
& 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x2} d_{y2} - \\
& c_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 4 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} d_{x1} - \\
& b_{x2} d_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 42 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 96 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 84 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (c_{x2} d_{y2} - c_{y2} d_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 48 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 36 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 80 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} -
\end{aligned}$$



$$\begin{aligned}
& b_{y2} c_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 12 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 35 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 56 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + \\
& 40 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 42 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 14 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 28 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x2} c_{y2} - b_{y2} c_{x2}) (d_{x1} d_{y2} - \\
& d_{x2} d_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{y2} d_{x1} - \\
& c_{x2} d_{y1}) + 48 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 96 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 48 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - \\
& 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} d_{y2} - b_{y1} d_{x2}) + 28 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) - \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x2} d_{y2} - c_{y2} d_{x2}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 72 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (c_{x1} d_{y2} -
\end{aligned}$$







$$\begin{aligned}
& a_{y2} c_{x2} (b_{x1} c_{y1} - b_{y1} c_{x1})^2 - 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 - 6 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (b_{x2} c_{y2} - b_{y2} c_{x2}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1})^3 + 2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 4 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) + 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1})^2 + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 2 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^3 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (c_{x2} d_{y2} - c_{y2} d_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) + 30 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 (c_{y2} d_{x1} - c_{x2} d_{y1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 10 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 28 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 8 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 14 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2})^2 + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x2} d_{y2} - b_{y2} d_{x2})^2 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 14 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) -
\end{aligned}$$

$$\begin{aligned}
& 12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x2}c_{y2}-a_{y2}c_{x2})(a_{x2}d_{y2}-a_{y2}d_{x2})-24(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x2}c_{y2}-a_{y2}c_{x2})(a_{x2}d_{y2}-a_{y2}d_{x2})-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{y2}d_{x1}-b_{x2}d_{y1})(b_{x2}d_{y2}-b_{y2}d_{x2})-18(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x2}b_{y2}-a_{y2}b_{x2})(b_{y2}d_{x1}-b_{x2}d_{y1})+18(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}d_{x1}-a_{x2}d_{y1})(a_{x2}c_{y2}-a_{y2}c_{x2})+42(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^3(b_{y2}d_{x1}-b_{x2}d_{y1})^2+12(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{y2}d_{x1}-a_{x2}d_{y1})(b_{y2}d_{x1}-b_{x2}d_{y1})-6(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}d_{x1}-a_{x2}d_{y1})^2-2(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})-16(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^3(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})+24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(c_{x2}d_{y2}-c_{y2}d_{x2})-12(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}d_{y2}-b_{y1}d_{x2})(c_{x2}d_{y2}-c_{y2}d_{x2})+12(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y2}-b_{y1}d_{x2})-4(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})+16(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x2}c_{y2}-b_{y2}c_{x2})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x2}d_{y2}-b_{y2}d_{x2})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(b_{x1}d_{y2}-b_{y1}d_{x2})(b_{x2}c_{y2}-b_{y2}c_{x2})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})^2-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})(b_{x2}c_{y2}-b_{y2}c_{x2})-24(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x2}d_{y2}-b_{y2}d_{x2})+10(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{y2}c_{x1}-b_{x2}c_{y1})+20(a_{x1}c_{y1}-a_{y1}c_{x1})^3(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(a_{y2}c_{x1}-a_{x2}c_{y1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})-12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})+6(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})-18(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{x2}b_{y2}-a_{y2}b_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})-36(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})-6(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})^2-36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})+12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x2}d_{y2}-a_{y2}d_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})-48(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{x2}b_{y2}-a_{y2}b_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})-6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y1}-a_{y1}d_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})+12(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})+12(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})-30(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{y2}d_{x1}-a_{x2}d_{y1})(b_{y2}c_{x1}-b_{x2}c_{y1})-30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{y2}c_{x1}-a_{x2}c_{y1})(c_{y2}d_{x1}-c_{x2}d_{y1})+4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^3(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{x1}d_{y1}-b_{y1}d_{x1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(b_{x1}c_{y2}-b_{y1}c_{x2})(b_{y2}d_{x1}-b_{x2}d_{y1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{y2}d_{x1}-b_{x2}d_{y1})+24(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})+36(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{y2}d_{x1}-b_{x2}d_{y1})+48(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})+36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}c_{y2}-b_{y1}c_{x2})(c_{y2}d_{x1}-c_{x2}d_{y1})+36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})(d_{x1}d_{y2}-d_{x2}d_{y1})+12(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}d_{y2}-a_{y1}d_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}d_{y1}-
\end{aligned}$$





$$\begin{aligned}
& a_{y1} d_{x2}) - 360 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) - 120 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) - \\
& 30 (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) - 60 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^3 + \\
& 90 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + 180 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + 120 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^5 + 15 (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 + 60 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 15 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^4 - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) + (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})^4 + 21 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1})^2 + 3 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 + \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + 6 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 + 144 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 96 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 96 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - \\
& 48 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 96 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) - 48 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 10 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 2 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 10 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y2} -
\end{aligned}$$

$$\begin{aligned}
& b_{y1} c_{x2})^2 - 20(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 36(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})(a_{x1} b_{y2} - a_{y1} b_{x2})(a_{x1} c_{y2} - a_{y1} c_{x2})(b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 84(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})(a_{y2} c_{x1} - a_{x2} c_{y1})(c_{x1} d_{y1} - c_{y1} d_{x1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})(b_{y2} c_{x1} - b_{x2} c_{y1}) + 4(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - a_{y1} b_{x2})^4 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 84(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})(a_{y2} c_{x1} - a_{x2} c_{y1})(c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})(b_{y2} c_{x1} - b_{x2} c_{y1}) - \\
& 4(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - a_{y1} b_{x2})^4 (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})(c_{x1} c_{y2} - c_{x2} c_{y1}) + 72(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})(a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 10(a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y1} - a_{y1} c_{x1})(b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})(b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 8(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 40(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) - 12(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})(b_{x1} c_{y2} - b_{y1} c_{x2})(b_{y2} c_{x1} - b_{x2} c_{y1}) - 36(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})(a_{y2} b_{x1} - a_{x2} b_{y1})(b_{x1} b_{y2} - b_{x2} b_{y1})(c_{x1} c_{y2} - c_{x2} c_{y1}) + 84(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})(b_{y2} c_{x1} - b_{x2} c_{y1})(c_{x1} c_{y2} - c_{x2} c_{y1}) + 36(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 48(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})(b_{x1} b_{y2} - b_{x2} b_{y1})(b_{x1} d_{y1} - b_{y1} d_{x1}) + 16(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) + 10(a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y1} - a_{y1} c_{x1})(b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 20(a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})(b_{y2} d_{x1} - b_{x2} d_{y1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})(b_{x2} d_{y2} - b_{y2} d_{x2}) - 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})(a_{x2} b_{y2} - a_{y2} b_{x2})(b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 - 6(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})(a_{x2} c_{y2} - a_{y2} c_{x2}) + \\
& 4(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})(b_{x1} c_{y1} - b_{y1} c_{x1})^3 - 4(a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) + 4(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 12(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})(b_{x1} c_{y1} - b_{y1} c_{x1})(b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})(a_{y2} c_{x1} - a_{x2} c_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) + 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x2} c_{y2} - \\
& a_{y2} c_{x2})(b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} c_{y2} - a_{y1} c_{x2})(a_{y2} b_{x1} - \\
& a_{x2} b_{y1})(b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 18(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) - 36(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) - 36(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})(a_{x2} d_{y2} - a_{y2} d_{x2})(b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) - 36(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} c_{y1} - a_{y1} c_{x1})(a_{x1} d_{y2} - a_{y1} d_{x2})(a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 18(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{y2} d_{x1} - b_{x2} d_{y1}) - \\
& 36(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})(a_{y2} b_{x1} - a_{x2} b_{y1})(a_{x2} b_{y2} - a_{y2} b_{x2})(b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2})(b_{x1} b_{y2} - b_{x2} b_{y1})(b_{y2} c_{x1} - b_{x2} c_{y1}) - 8(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2})(b_{x1} c_{y1} - b_{y1} c_{x1})(b_{x2} c_{y2} - b_{y2} c_{x2}) - 12(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - \\
& a_{y2} c_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 18(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1})(a_{x2} c_{y2} - a_{y2} c_{x2})(c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) - 6(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})(a_{y2} b_{x1} - a_{x2} b_{y1})(a_{x2} c_{y2} - a_{y2} c_{x2})(b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 8(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24(a_{x1} b_{y1} - a_{y1} b_{x1})(a_{x1} b_{y2} - \\
& a_{y1} b_{x2})(a_{x1} d_{y2} - a_{y1} d_{x2})(a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 16(a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2})(a_{x2} d_{y2} - a_{y2} d_{x2})(b_{x1} c_{y1} - b_{y1} c_{x1}) - 24(a_{x1} a_{y2} - a_{x2} a_{y1})(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} d_{x1} -
\end{aligned}$$



$$\begin{aligned}
& a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2})^2 + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 14 (a_{x1} c_{y1} - a_{y1} c_{x1})^4 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2})^2 + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x2} c_{y2} - a_{y2} c_{x2})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{y2} d_{x1} - b_{x2} d_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + \\
& 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) - 6 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1})^2 - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} c_{y2} - \\
& b_{y1} c_{x2})^2 - 2 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} d_{y2} - b_{y1} d_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 3 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 20 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - \\
& 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 24 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 72 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 48 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) - 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - \\
& 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + \\
& 12 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 30 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 36 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 12 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) + 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 36 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 36 (a_{x1} a_{y2} -
\end{aligned}$$



$$\begin{aligned}
& a_{y1} b_{x2} (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - 72 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 72 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) - 144 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (d_{x1} d_{y2} - d_{x2} d_{y1}) - 72 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 72 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y1} - c_{y1} d_{x1})
\end{aligned}$$

$$\begin{aligned}
c_9 = & -20 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^3 + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) + 180 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 + \\
& 60 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 - 360 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) - \\
& 120 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) - 180 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) - 30 (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) + 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^3 + 180 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + 180 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 30 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^4 + 30 (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) + 20 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^3 (b_{x1} d_{y1} - b_{y1} d_{x1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^3 (b_{x1} d_{y2} - b_{y1} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^3 - 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2})^2 + 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 20 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1})^2 - 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} d_{y1} - \\
& c_{y1} d_{x1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 96 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + \\
& 96 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - \\
& 48 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 36 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 18 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1} (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 - 56 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 56 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) + 144 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - \\
& 16 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 20 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^3 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - 8 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 4 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 10 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 20 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} d_{y2} - \\
& c_{y1} d_{x2}) - 20 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (c_{x1} d_{y2} - c_{y1} d_{x2}) + \\
& 84 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + \\
& 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})^2 (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) - 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1})^2 + 10 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^4 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) - \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2}) - 2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) + 2 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} c_{x1} - a_{x2} c_{y1})^3 - \\
& 8 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^3 - 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x2} c_{y2} - b_{y2} c_{x2}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) + 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + \\
& 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (b_{x2} c_{y2} - b_{y2} c_{x2})^2 + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x2} d_{y2} - b_{y2} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 14 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2})^2 + \\
& 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} d_{y2} - a_{y2} d_{x2})^2 - 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1})^2 - \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (c_{x2} d_{y2} - c_{y2} d_{x2}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 36 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 16 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) - \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} d_{y2} - \\
& a_{y2} d_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + \\
& 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 4 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 36 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{y2} d_{x1} - b_{x2} d_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 28 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 30 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1})^2 - 60 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) + 4 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 18 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{y2} c_{x1} - \\
& b_{x2} c_{y1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} d_{y1} -
\end{aligned}$$

$$\begin{aligned}
& b_{y1} d_{x1}) + 6(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 18(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + 6(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) + 18(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) - 24(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 32(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 24(a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 24(a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - 24(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} d_{y2} - c_{y1} d_{x2}) - 72(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 72(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 144(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 72(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 60(a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) + 72(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) - 72(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) + 96(a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) + \\
& 72(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) + \\
& 144(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) + 36(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - \\
& 24(a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + 36(a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - 24(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 72(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{y2} d_{x1} - b_{x2} d_{y1}) - 144(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) - 72(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) - 48(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 72(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} d_{x1} - a_{x2} d_{y1}) - 48(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1})
\end{aligned}$$

$$\begin{aligned}
c_{10} = & 60(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 + 90(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1})^2 + 4(a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^3 (b_{x1} c_{y2} - b_{y1} c_{x2}) - \\
& 6(a_{x1} b_{y2} - a_{y1} b_{x2})^5 (a_{x1} d_{y1} - a_{y1} d_{x1}) + 6(a_{x1} b_{y2} - a_{y1} b_{x2})^5 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 6(a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 15(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^4 + \\
& 15(a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 + 60(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2})^2 + 60(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2})^3 + 90(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2})^2 - 120(a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - \\
& a_{y1} d_{x2}) - 120(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) + \\
& 120(a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) - 180(a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) - 180(a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} -
\end{aligned}$$

$$\begin{aligned}
& a_{y1} b_{x2} (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) + 180 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 3 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{x2} b_{y2} - a_{y2} b_{x2})^2 + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} d_{y2} - c_{y1} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 32 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) - 32 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - \\
& 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (c_{x1} d_{y1} - c_{y1} d_{x1}) - 48 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) - 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (c_{y2} d_{x1} - c_{x2} d_{y1}) - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) - 144 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) - \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + 8 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) + 144 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^3 (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) - \\
& 2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 72 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^5 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 144 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (c_{x1} c_{y2} - c_{x2} c_{y1}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) - 8 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^3 - 16 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x1} d_{y2} - \\
& b_{y1} d_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} d_{y2} - a_{y2} d_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 16 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (a_{x2} d_{y2} - a_{y2} d_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + 16 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} d_{x1} - a_{x2} d_{y1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - \\
& 16 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (c_{x1} c_{y2} - c_{x2} c_{y1}) - 12 (a_{x1} a_{y2} -
\end{aligned}$$

$$\begin{aligned}
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{y2} d_{x1} - a_{x2} d_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 6 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) + 24 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} d_{x1} - \\
& a_{x2} d_{y1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x2} d_{y2} - \\
& b_{y2} d_{x2}) + 12 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + \\
& 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x2} d_{y2} - b_{y2} d_{x2}) + 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 + 36 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 18 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^2 - 10 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^3 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x2} c_{y2} - b_{y2} c_{x2}) - 18 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (b_{x1} c_{y2} - b_{y1} c_{x2}) (b_{x2} c_{y2} - \\
& b_{y2} c_{x2}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 - \\
& 6 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - 12 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) - 36 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) - 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - a_{y2} b_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (b_{x1} c_{y2} - b_{y1} c_{x2})^2 + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1})^2 - 8 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1})^2 + 12 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 6 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1})^2 (a_{y2} b_{x1} - \\
& a_{x2} b_{y1})^2 + 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1})^2 + \\
& 42 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) (c_{x1} c_{y2} - c_{x2} c_{y1}) \\
\\
c_{11} = & 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1})^2 - 120 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) + 4 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^3 (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 6 (a_{x1} b_{y2} - a_{y1} b_{x2})^5 (a_{x1} c_{y2} - a_{y1} c_{x2}) - 30 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} d_{y1} - \\
& a_{y1} d_{x1}) + 30 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} d_{y2} - a_{y1} d_{x2}) - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2})^2 + \\
& 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^3 + 60 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2})^2 - \\
& 180 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) + 180 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) + 6 (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^4 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (c_{x1} d_{y1} - c_{y1} d_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (b_{y2} c_{x1} - b_{x2} c_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - \\
& b_{y1} c_{x1}) + 40 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 72 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} c_{x1} - a_{x2} c_{y1}) +
\end{aligned}$$



$$\begin{aligned}
& 24(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}d_{y2}-a_{y1}d_{x2})(b_{y2}c_{x1}-b_{x2}c_{y1})+8(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})^3(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})(b_{x1}c_{y1}-b_{y1}c_{x1})+56(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(c_{x1}d_{y2}-c_{y1}d_{x2})+2(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}c_{y1}-a_{y1}c_{x1})^2(b_{y2}c_{x1}- \\
& b_{x2}c_{y1})-72(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x2}d_{y2}- \\
& a_{y2}d_{x2})+6(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})+ \\
& 36(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})+20(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})^3(a_{x1}c_{y2}-a_{y1}c_{x2})^2(b_{x1}c_{y1}-b_{y1}c_{x1})-72(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x2}b_{y2}-a_{y2}b_{x2})+60(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})^2(a_{y2}c_{x1}-a_{x2}c_{y1})+24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})(b_{x1}c_{y1}-b_{y1}c_{x1})+24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})(a_{x2}c_{y2}-a_{y2}c_{x2})+144(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})(b_{y2}c_{x1}-b_{x2}c_{y1})-8(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}b_{x1}-a_{x2}b_{y1})(a_{y2}c_{x1}-a_{x2}c_{y1})(a_{x2}b_{y2}- \\
& a_{y2}b_{x2})-8(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{y2}b_{x1}-a_{x2}b_{y1})^3+ \\
& 16(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})-16(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})+24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{y2}d_{x1}-a_{x2}d_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})+24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x2}d_{y2}- \\
& a_{y2}d_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})+24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}d_{y1}-b_{y1}d_{x1})-24(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}d_{y2}-b_{y1}d_{x2})-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{y2}d_{x1}-a_{x2}d_{y1})(a_{x2}b_{y2}- \\
& a_{y2}b_{x2})-12(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x2}b_{y2}-a_{y2}b_{x2})(a_{x2}d_{y2}-a_{y2}d_{x2})- \\
& 2(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(b_{x1}c_{y2}-b_{y1}c_{x2})^2-16(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})^2(b_{y2}c_{x1}-b_{x2}c_{y1})+6(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})(a_{x2}c_{y2}-a_{y2}c_{x2})+6(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})^2(a_{x2}b_{y2}-a_{y2}b_{x2})-18(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})-24(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^3(a_{x2}b_{y2}-a_{y2}b_{x2})(b_{x2}c_{y2}- \\
& b_{y2}c_{x2})+4(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x2}b_{y2}-a_{y2}b_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})+ \\
& 12(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})^2(b_{x1}b_{y2}-b_{x2}b_{y1})(b_{x2}c_{y2}-b_{y2}c_{x2})-10(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^2(b_{x1}b_{y2}-b_{x2}b_{y1})^2-6(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{y2}b_{x1}-a_{x2}b_{y1})^2-8(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}c_{y1}-a_{y1}c_{x1})(b_{x1}b_{y2}- \\
& b_{x2}b_{y1})(b_{x1}c_{y1}-b_{y1}c_{x1})-36(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}c_{y2}-b_{y1}c_{x2})+12(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}c_{y1}-a_{y1}c_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(b_{x1}b_{y2}- \\
& b_{x2}b_{y1})-18(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}c_{y2}-a_{y1}c_{x2})(b_{x1}b_{y2}-b_{x2}b_{y1})^2+ \\
& 18(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{y2}c_{x1}-a_{x2}c_{y1})^2+6(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})^2(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}c_{x1}-a_{x2}c_{y1})(b_{y2}c_{x1}-b_{x2}c_{y1})
\end{aligned}$$

$$\begin{aligned}
c_{12} = & 15(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}d_{y1}-a_{y1}d_{x1})^2-30(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}d_{y1}-a_{y1}d_{x1})(a_{x1}d_{y2}- \\
& a_{y1}d_{x2})+(a_{x1}b_{y2}-a_{y1}b_{x2})^6+(a_{x1}b_{y1}-a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})^4+15(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}d_{y2}- \\
& a_{y1}d_{x2})^2+20(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}c_{y2}-a_{y1}c_{x2})^3+30(a_{x1}a_{y2}-a_{x2}a_{y1})(a_{x1}b_{y2}-a_{y1}b_{x2})^4(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})-60(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^3(a_{x1}d_{y1}-a_{y1}d_{x1})+60(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})^3(a_{x1}d_{y2}-a_{y1}d_{x2})+90(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})^2- \\
& 120(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}-a_{y1}c_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})+120(a_{x1}a_{y2}-
\end{aligned}$$

$$\begin{aligned}
& a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) + 3 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 + 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} d_{y1} - a_{y1} d_{x1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} d_{y2} - a_{y1} d_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 30 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (b_{x1} d_{y1} - b_{y1} d_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) - \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{y2} d_{x1} - a_{x2} d_{y1}) + 24 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y2} - a_{y1} d_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) + 40 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (b_{x1} c_{y2} - \\
& b_{y1} c_{x2}) + 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2})^3 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{y2} c_{x1} - b_{x2} c_{y1}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (b_{y2} c_{x1} - b_{x2} c_{y1}) + 56 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (c_{x1} c_{y2} - \\
& c_{x2} c_{y1}) - 24 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) - 72 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} c_{y2} - \\
& a_{y2} c_{x2}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} d_{y2} - a_{y2} d_{x2}) - \\
& 10 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y2} - b_{y1} d_{x2}) + 6 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} d_{y1} - a_{y1} d_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 - 2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 + 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} d_{y1} - \\
& b_{y1} d_{x1}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x2} b_{y2} - a_{y2} b_{x2}) (b_{x1} b_{y2} - \\
& b_{x2} b_{y1}) - 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1}) - \\
& 18 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) - \\
& 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) - 16 (a_{x1} a_{y2} - \\
& a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 3 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (b_{x1} c_{y1} - \\
& b_{y1} c_{x1})^2 + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x2} c_{y2} - a_{y2} c_{x2}) (b_{x1} b_{y2} - b_{x2} b_{y1}) + \\
& 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{y2} c_{x1} - a_{x2} c_{y1})^2 - 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (b_{x1} c_{y1} - b_{y1} c_{x1}) - 12 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^3 (a_{x2} b_{y2} - \\
& a_{y2} b_{x2}) (a_{x2} c_{y2} - a_{y2} c_{x2})
\end{aligned}$$

$$\begin{aligned}
c_{13} = & -30 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{x1} d_{y1} - a_{y1} d_{x1}) - 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^2 (a_{x1} d_{y1} - a_{y1} d_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^5 + 30 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y2} - \\
& a_{y1} c_{x2}) (a_{x1} d_{y2} - a_{y1} d_{x2}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{x1} d_{y2} - a_{y1} d_{x2}) + \\
& 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y2} - a_{y1} c_{x2})^2 + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2})^3 (a_{x1} c_{y2} - a_{y1} c_{x2}) + 4 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y2} - a_{y1} c_{x2}) (b_{x1} c_{y1} - b_{y1} c_{x1}) + \\
& 20 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (b_{x1} c_{y1} - b_{y1} c_{x1}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^4 (a_{x1} c_{y1} - \\
& a_{y1} c_{x1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) + 60 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2})^2 (a_{y2} c_{x1} - \\
& a_{x2} c_{y1}) + 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} c_{y2} - a_{y1} c_{x2}) (a_{y2} c_{x1} - a_{x2} c_{y1}) + \\
& 24 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{x1} c_{y1} - a_{y1} c_{x1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) - \\
& 2 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (b_{x1} b_{y2} - b_{x2} b_{y1})^2 + 6 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - \\
& a_{y1} b_{x1})^2 (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} c_{y2} - a_{y2} c_{x2}) + 6 (a_{x1} a_{y2} - a_{x2} a_{y1}) (a_{x1} b_{y1} - a_{y1} b_{x1})^2 (a_{x1} b_{y2} - \\
& a_{y1} b_{x2}) (a_{y2} b_{x1} - a_{x2} b_{y1}) (a_{x2} b_{y2} - a_{y2} b_{x2}) - 10 (a_{x1} a_{y2} - a_{x2} a_{y1})^3 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} c_{y2} - b_{y1} c_{x2}) - 18 (a_{x1} a_{y2} - a_{x2} a_{y1})^2 (a_{x1} b_{y1} - a_{y1} b_{x1}) (a_{x1} b_{y2} - a_{y1} b_{x2}) (a_{y2} b_{x1} - \\
& a_{x2} b_{y1}) (b_{x1} b_{y2} - b_{x2} b_{y1})
\end{aligned}$$

$$\begin{aligned}
c_{14} = & -30(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}d_{y1}-a_{y1}d_{x1})+30(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})(a_{x1}d_{y2}-a_{y1}d_{x2})+15(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}c_{y2}-a_{y1}c_{x2})^2+15(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y2}- \\
& a_{y1}b_{x2})^4+60(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y2}-a_{y1}b_{x2})^2(a_{x1}c_{y2}-a_{y1}c_{x2})+6(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}c_{y1}- \\
& a_{y1}c_{x1})(b_{x1}b_{y2}-b_{x2}b_{y1})+4(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y2}-a_{y1}b_{x2})(b_{x1}c_{y1}-b_{y1}c_{x1})+24(a_{x1}a_{y2}- \\
& a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{y2}c_{x1}-a_{x2}c_{y1})+6(a_{x1}a_{y2}-a_{x2}a_{y1})^2(a_{x1}b_{y1}- \\
& a_{y1}b_{x1})^2(a_{y2}b_{x1}-a_{x2}b_{y1})(a_{x2}b_{y2}-a_{y2}b_{x2})-10(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})(b_{x1}b_{y2}-b_{x2}b_{y1})
\end{aligned}$$

$$\begin{aligned}
c_{15} = & -6(a_{x1}a_{y2}-a_{x2}a_{y1})^5(a_{x1}d_{y1}-a_{y1}d_{x1})+6(a_{x1}a_{y2}-a_{x2}a_{y1})^5(a_{x1}d_{y2}-a_{y1}d_{x2})+ \\
& 20(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y2}-a_{y1}b_{x2})^3+30(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y2}-a_{y1}b_{x2})(a_{x1}c_{y2}- \\
& a_{y1}c_{x2})+2(a_{x1}a_{y2}-a_{x2}a_{y1})^5(b_{x1}c_{y1}-b_{y1}c_{x1})-2(a_{x1}a_{y2}-a_{x2}a_{y1})^3(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{y2}b_{x1}- \\
& a_{x2}b_{y1})^2+6(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y1}-a_{y1}b_{x1})(a_{y2}c_{x1}-a_{x2}c_{y1})
\end{aligned}$$

$$c_{16} = 6(a_{x1}a_{y2}-a_{x2}a_{y1})^5(a_{x1}c_{y2}-a_{y1}c_{x2})+15(a_{x1}a_{y2}-a_{x2}a_{y1})^4(a_{x1}b_{y2}-a_{y1}b_{x2})^2$$

$$c_{17} = 6(a_{x1}a_{y2}-a_{x2}a_{y1})^5(a_{x1}b_{y2}-a_{y1}b_{x2})$$

$$c_{18} = (a_{x1}a_{y2}-a_{x2}a_{y1})^6$$

$$c_{18} = (a_{x1}a_{y2}-a_{x2}a_{y1})^6$$

## 5 Analysis

The previous sections outlined the math involved in determining the polynomial equation used to identify where two cubic parametric curves intersect. This section discusses that derivation and its implications.

The original intention of this project was to find a fast/simple method to identify where curves intersected. This project failed in this respect, because the result is very impractical. There are much faster ways to numerically approximate where two curves intersect than to resolve such a complex polynomial with potentially huge exponents. Also large exponents can lead to significant machine error when cast into IEEE double precision. Or alternatively: performance degrades sharply if we use classes like the `BigDecimal` to maintain several significant digits.

Meanwhile one of the peculiar successes of this project was identifying the fractional cubic root elimination transform. Maybe this is well-known to some readers, but it was a novel discovery for me when I first stumbled across it. It's trivial to apply a similar trick to square roots, and so it follows that if you apply it twice consecutively you can resolve quartic roots. Also you could combine this cubic root transform with a square root transform to resolve sextic roots. You could even combine two cubic transforms to make a (very hairy) transform for 9th degree roots. This raises the question: if we can transform 9th degree roots, what about simpler cases like 5th degree or 7th degree roots? Are they impossible because they are relatively prime, or are they just very hard to identify? If I were to continue investing time and energy in this direction: I would love to try to numerically (in a brute-force approach) explore this question.

This paper omits how exactly I factored this equation into the coefficients listed in the previous section. The reason for this omission is: I can't find my notes on this subject. (I actually completed this project a few years ago, and this writeup is long overdue.) So I wrote down what the factored coefficients are, and I confirmed that these figures are correct for this paper—but I don't know exactly how to derive them. But one thing that immediately jumps out at me is: this looks like the result of a matrix transformation. I wonder if I invested more time in factoring this if I would find an even simpler expression? One that either involves matrices or squaring a 9th degree polynomial?

There is also the sticky question: why, philosophically, should this be an 18th degree polynomial? (That is: why so many roots?) For comparison: if you study the intersection of two quadratic parametric curves you'll get a 4th degree polynomial. 4 roots makes sense, because if you imagine two curves (one shaped like the letter C and a copy of that shape rotated 90 degrees), then it's easy to see where they intersect in 4 places. But should two cubic curves have 18 intersections? I initially justified the 18th degree away because we could graphically identify up to 9 solutions, but the polynomial has to have an even degree

to account for the possibility of zero solutions. (So what is the smallest multiple of 9 that is even? 18.) But now I believe that explanation is inadequate. Instead if you look at how the equations unravelled mathematically: I think the solution to two  $n$ -degree curves is going to be  $n * (n!)$ . So 1 maps to 1, 2 maps to 4, 3 maps to 18, and 4 will map to 96. But this question might be better understood if there are more complete ways to factor this particular equation. If this equation is, for example, two 9th-degree equations multiplied together, then that raises a whole new set of fascinating questions and may simplify how to identify roots.

Considering how this equation was derived, it is not surprising that this equation cannot identify  $t$  values where a cubic parametric curve intersects itself. If we set  $a_{x2} = a_{x1}$ ,  $b_{x2} = b_{x1}$ ,  $c_{x2} = c_{x1}$ , etc then the resulting equation is simply zero. But what did surprise me is the realization that every cluster of variables contains an  $a$  term that cannot be factored out. For some reason I instinctively (and mistakenly) expected to be able to set all the  $a$  terms to zero and end up with a quadratic-quadratic solution.

This project did not yield the desired results, but I still wanted to share them in case someone finds it useful or insightful. The computer program (including the source code) used to write sections 3 and 4 is available here:

<https://javagraphics.java.net/jars/CubicPaper.jar>