

a)

$$\lim_n \frac{2+3n}{5n} = \lim_n \frac{3\cancel{n}}{5\cancel{n}} = \frac{3}{5}$$

b)

$$\lim_n \frac{3n^2+4n-2}{4n^2-3n+5} = \lim_n \frac{3\cancel{n^2}}{4\cancel{n^2}} = \frac{3}{4}$$

c)

$$\lim_n \frac{3n^2+1}{4n^3+5} = \lim_n \frac{3\cancel{n^2}}{4\cancel{n^3}} = \lim_n \frac{3}{4n} = 0$$

d)

$$\lim_n \frac{3n^3+4n^2-3n+2}{4n^2+3n+2} = \lim_n 3n^3 = +\infty$$

e)

$$\lim_n 5(-1)^n \begin{cases} -5 & \text{se } n \text{ é ímpar} \\ 5 & \text{se } n \text{ é par} \end{cases} \quad \text{Limite não existe}$$

f)

$$\lim_n \sqrt{n^3+3} = \lim_n \sqrt{n^2 \left( n + \frac{3}{n^2} \right)} = \lim_n |n| \sqrt{n + \frac{3}{n^2}} = \lim_n n \sqrt{n + \frac{3}{n^2}} = +\infty$$

g)

$$\lim_n \frac{\sqrt{4n^2+1}}{n+3} = \lim_n \frac{\sqrt{n^2 \left( 4 + \frac{1}{n^2} \right)}}{n \left( 1 + \frac{3}{n} \right)} = \lim_n \frac{|n| \sqrt{4 + \frac{1}{n^2}}}{n \left( 1 + \frac{3}{n} \right)} = \lim_n \frac{\cancel{n} \sqrt{4 + \frac{1}{n^2}}}{\cancel{n} \left( 1 + \frac{3}{n} \right)} = 2$$

h)

$$\begin{aligned} & \lim_n \left( \frac{1}{\sqrt{n^2+1}} - \frac{1}{\sqrt{n^2+2}} \right) \\ &= \lim_n \left( \frac{1}{\sqrt{n^2+1}} \right) - \lim_n \left( \frac{1}{\sqrt{n^2+2}} \right) \\ & \quad 0 - 0 = 0 \end{aligned}$$

i)

$$\begin{aligned} & \lim_n \left( \frac{1}{\sqrt{n^4+2} - \sqrt{n^4+3}} \right) = \lim_n \frac{\sqrt{n^4+2} + \sqrt{n^4+3}}{\left( \sqrt{n^4+2} - \sqrt{n^4+3} \right) \left( \sqrt{n^4+2} + \sqrt{n^4+3} \right)} \\ &= \lim_n \frac{\sqrt{n^4+2} + \sqrt{n^4+3}}{-1} \\ &= -\lim_n \sqrt{n^4+2} + \sqrt{n^4+3} \\ &= -\lim_n \sqrt{n^4 \left( 1 + \frac{2}{n^4} \right)} + \sqrt{n^4 \left( 1 + \frac{3}{n^4} \right)} = -\lim_n |n| \sqrt{1 + \frac{2}{n^4}} + |n| \sqrt{1 + \frac{3}{n^4}} = -\infty \end{aligned}$$

j)

$$\begin{aligned}
 & \lim_n \left( \sqrt{n^2 + 2} - \sqrt{n^2 - n} \right) \\
 &= \lim_n \frac{\left( \sqrt{n^2 + 2} - \sqrt{n^2 - n} \right) \left( \sqrt{n^2 + 2} + \sqrt{n^2 - n} \right)}{\left( \sqrt{n^2 + 2} + \sqrt{n^2 - n} \right)} \\
 &= \lim_n \frac{2 + n}{\left( \sqrt{n^2 + 2} + \sqrt{n^2 - n} \right)} \\
 &= \lim_n \frac{n \left( \frac{2}{n} + 1 \right)}{\sqrt{n^2 \left( 1 + \frac{2}{n^2} \right)} + \sqrt{n^2 \left( 1 - \frac{1}{n} \right)}} \\
 &= \lim_n \frac{n \left( \frac{2}{n} + 1 \right)}{|n| \left( \sqrt{1 + \frac{2}{n^2}} + \sqrt{1 - \frac{1}{n}} \right)} \\
 &= \lim_n \frac{\mathcal{N} \left( \frac{2}{n} + 1 \right)}{\mathcal{N} \left( \sqrt{1 + \frac{2}{n^2}} + \sqrt{1 - \frac{1}{n}} \right)} \\
 &= \frac{1}{2}
 \end{aligned}$$

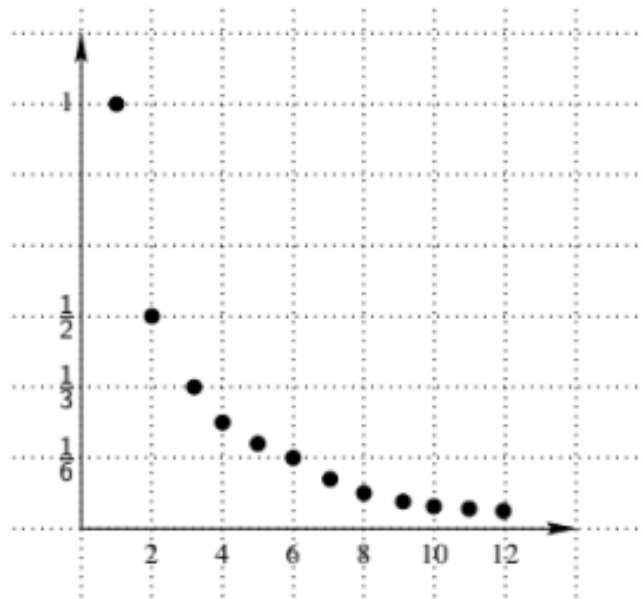


Figura 1:

$$a_n = \frac{1}{n}$$

É limitada e monótona portanto convergente

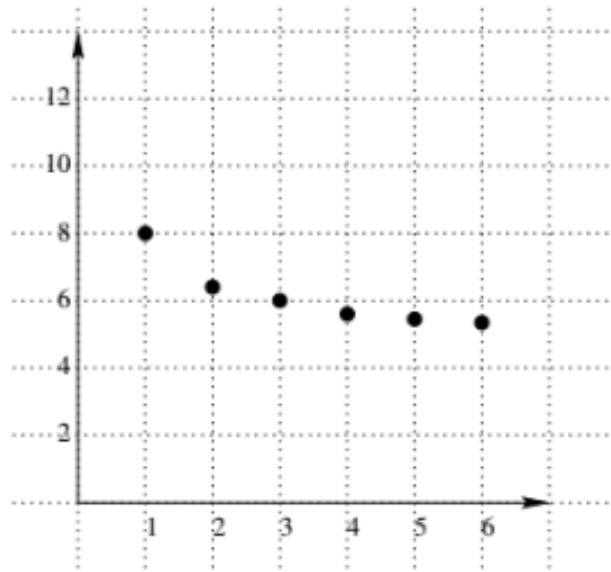


Figura 2:  
 $b_n = \frac{5n+3}{n}$   
 É limitada, monótona e por isso convergente

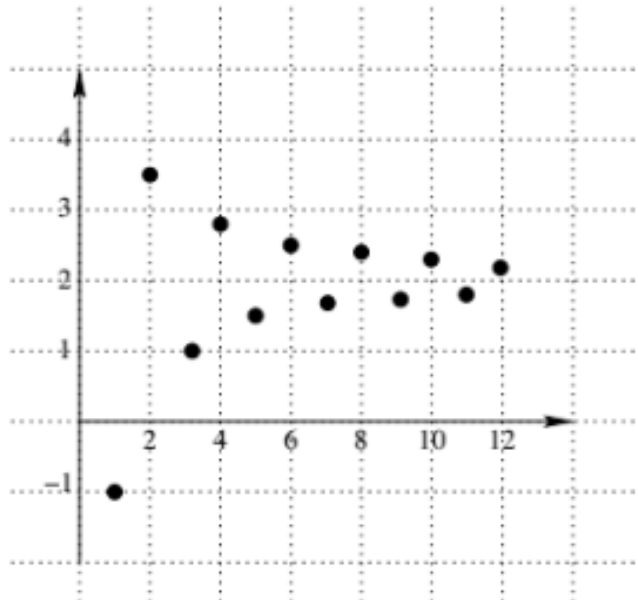


Figura 3:  
 $c_n = \frac{3(-1)^n + 2n}{n}$   
 É limitada, não monótona mas convergente

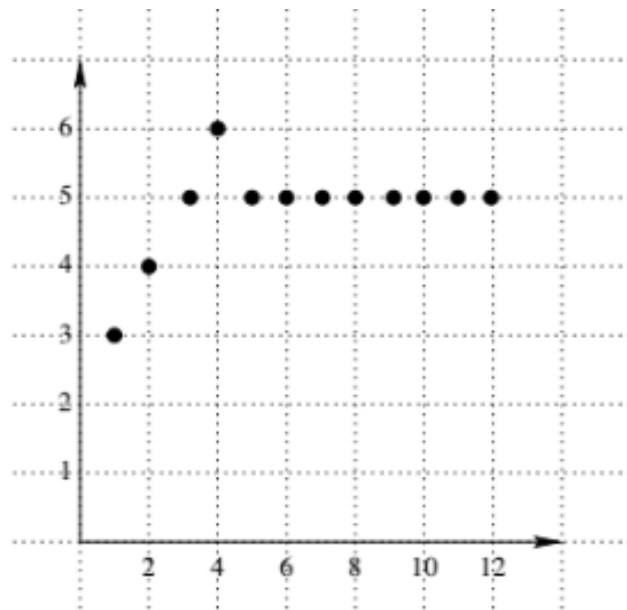


Figura 4:  

$$d_n = \begin{cases} n+2, & \text{se } n \leq 5, \\ 5, & \text{se } n \geq 5; \end{cases}$$
 É limitada, não monótona mas convergente

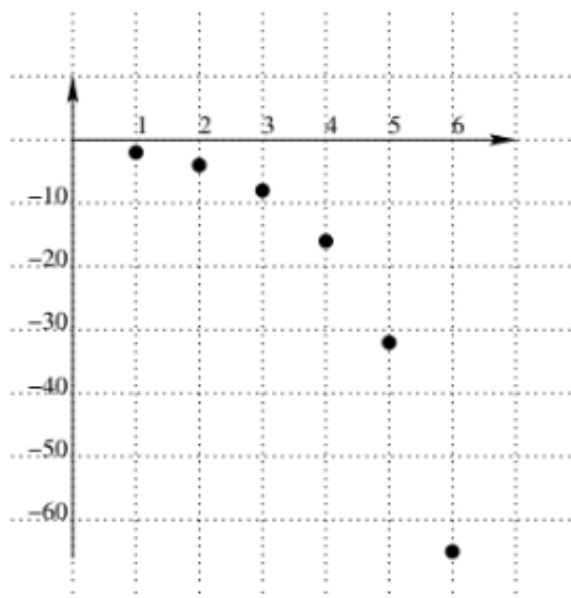


Figura 5:  

$$e_n = -2^n$$
 É monótona, não limitada e não convergente

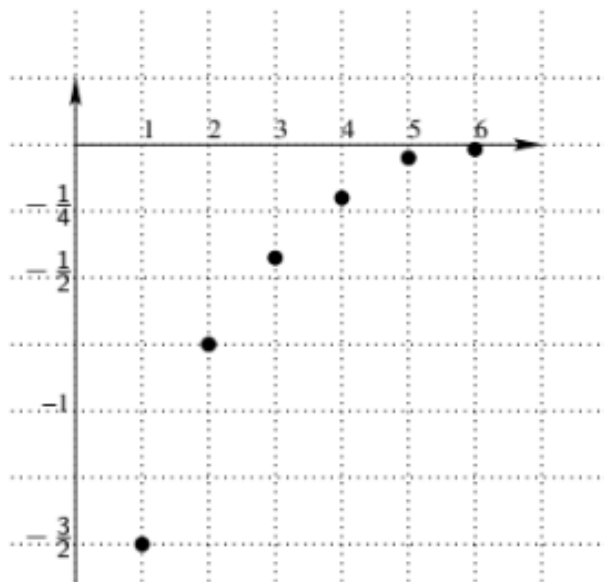


Figura 6:

$$e_n = -\frac{3}{2^n}$$

É limitada, monótona e por isso convergente