$$E = \{f: [0,1] \mapsto \mathbb{R} \text{ continua}\}$$

$$\langle f,g \rangle = \int_0^1 f(t)g(t)dt$$

$$f(t) = t^2 - t + 1$$

$$u(t) = 1 \qquad w(t) = t$$

Calcula a projeção ortogonal de f(t) sobre o plano gerado por u(t) e w(t).

Us and o Gram - Schmidt:

$$v_1 := u$$

$$\begin{aligned} v_2 &:= w - proj_{v_1} w \implies \forall t \in [0,1] : v_2(t) = w(t) - (proj_{v_1} w)(t) = t - \frac{\int_0^1 s \, \mathrm{d}s}{\int_0^1 1 \, \mathrm{d}s} u(t) = t - 1/2 \\ & ||v_2(t)|| = \sqrt{\langle v_2(t), v_2(t) \rangle} = \sqrt{\int_0^1 (t^2 + \frac{1}{4}) \, \mathrm{d}t} = \sqrt{\frac{7}{12}} \\ & \frac{v_2(t)}{||v_2(t)||} = \frac{t - \frac{1}{2}}{\sqrt{\frac{7}{12}}} \\ & b_1 := 1 \qquad b_2 := \frac{t - \frac{1}{2}}{\sqrt{\frac{7}{12}}} \end{aligned}$$

 $proj_{b_1}f + proj_{b_1}f = \langle f, b_1 \rangle b_1 + \langle f, b_2 \rangle b_2$