## 1.

Determine as seguintes integrais:

1)

$$\int_0^{\sqrt{\frac{\pi}{2}}} x \sin x^2 dx$$

$$= \frac{1}{2} \int_0^{\sqrt{\frac{\pi}{2}}} 2x \sin x^2 dx$$

$$= \frac{1}{2} (-\cos x^2) \Big|_0^{\frac{\pi}{2}}$$

$$= \frac{1}{2} (-\cos (\sqrt{\frac{\pi}{2}})^2 + \cos 0)$$

$$= \frac{1}{2}$$

2)

$$\int_0^{\pi} (x+2)\cos x dx$$

$$f' = \cos x \qquad f = \sin x$$

$$g = x+2 \qquad g' = 1$$

$$(x+2)\sin x \Big|_0^{\pi} - \int_0^{\pi} \sin x dx$$

$$(\pi+2)\sin \pi - 2\sin 0 + \cos x \Big|_0^{\pi}$$

$$= -2$$

3)

$$\int_{1}^{2} x 2^{x} dx$$

$$f' = 2^{x} \qquad f = \frac{2^{x}}{\ln 2}$$

$$g = x \qquad g' = 1$$

$$\frac{2^{x}}{\ln 2} x \Big|_{1}^{2} - \int_{1}^{2} \frac{2^{x}}{\ln 2}$$

$$= \frac{8}{\ln 2} - \frac{2}{\ln 2} - \frac{1}{\ln 2} \frac{2^{x}}{\ln 2} \Big|_{1}^{2}$$

$$= \frac{6}{\ln 2} - \frac{2}{\ln^2 2}$$
$$= \frac{6 \ln 2 - 2}{\ln^2 2}$$

4)

$$\int_0^1 \frac{e^x}{\sqrt{e^x + 1}} dx$$
$$2(e^x + 1)^{\frac{1}{2}}) \Big|_0^1$$
$$2((e+1)^{\frac{1}{2}} - (2)^{\frac{1}{2}})$$

2.

a)

Calcule  $\int_0^{\frac{\pi}{2}} e^x \sin(x) dx$ :

$$\int_{0}^{\frac{\pi}{2}} e^{x} \sin(x) dx$$

$$f' = \sin(x) \qquad f = -\cos(x)$$

$$g = e^{x} \qquad g' = e^{x}$$

$$= \int_{0}^{\frac{\pi}{2}} e^{x} \sin(x) dx = -\cos(x) e^{x} \Big|_{0}^{\frac{\pi}{2}} - \int_{0}^{\frac{\pi}{2}} -\cos(x) e^{x} dx$$

$$f' = \cos(x) \qquad f = \sin(x)$$

$$g = e^{x} \qquad g' = e^{x}$$

$$= \int_{0}^{\frac{\pi}{2}} e^{x} \sin(x) dx = 1 + e^{\frac{\pi}{2}} - \int_{0}^{\frac{\pi}{2}} \sin(x) e^{x} dx$$

$$= \int_{0}^{\frac{\pi}{2}} e^{x} \sin(x) dx = \frac{1}{2} (1 + e^{\frac{\pi}{2}})$$

3.

Usando uma substituição, calcule os seguintes integrais

$$\int_{-1}^{1} e^{\arcsin(x)} dx$$

$$\sin(x) : \left[ -\frac{\pi}{2}, \frac{\pi}{2} \right] \to [-1, 1]$$

$$x = \sin(t) \qquad dx = \cos(t) dt$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{\arcsin(\sin(t))} \cos(t) dt$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{t} \cos(t) dt$$

$$f' = \cos(t) \qquad f = \sin(t)$$

$$g = e^{t} \qquad g' = e^{t}$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{t} \cos(t) dt = (\sin(t)e^{t}) \Big|_{-\frac{\pi}{2}}^{\frac{\pi}{2}} - \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{t} \sin(t) dt$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{t} \cos(t) dt = e^{\frac{\pi}{2}} - e^{\frac{-\pi}{2}} + (\cos(t)e^{t}) \Big|_{-\frac{\pi}{2}}^{\frac{\pi}{2}} + \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} e^{t} \cos(t) dt$$