

令 $E(x)$ 為有 x 顆頭的揮劍次數期望值，則

$$E(5) = 10 + 0.8 \times E(5) + 0.2 \times E(4)$$

$$E(4) = \frac{10}{3} + 0.8 \times E(5) + 0.2 \times E(3)$$

$$E(3) = \frac{10}{5} + 0.8 \times E(4) + 0.2 \times E(2)$$

$$E(2) = \frac{10}{7} + 0.8 \times E(3) + 0.2 \times E(1)$$

$$E(1) = \frac{10}{9}$$

整理過後，

$$E(5) = 50 + E(4)$$

$$E(4) = \frac{650}{3} + E(3) = \frac{290320}{63}$$

$$E(3) = \frac{2630}{3} + E(2)$$

$$E(2) = \frac{221440}{63}$$

$$E(1) = \frac{10}{9}$$

$$\text{ANS} = \frac{290320}{63}$$