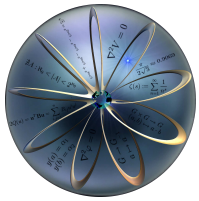

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hypergeometric function

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Defines	Gauss hypergeometric function

Let (a, b, c) be a triple of complex numbers with c not belonging to the set of negative integers. For a complex number w and a non negative integer n, use Pochhammer symbol $(w)_n$, to denote the expression :

$$(w)_n = w(w+1)\dots(w+n-1).$$

The *Gauss hypergeometric function*, ${}_2F_1$, is then defined by the following power series expansion :

$${}_2F_1(a, b;\, c\,; z) = \sum_{n=0}^{\infty} \frac{(a)_n (b)_n}{(c)_n n!} z^n.$$