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symmetry of an ordinary differential equation

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Let $f : \mathbb{R}^n \rightarrow \mathbb{R}^n$ be a smooth function and let

$$\dot{x} = f(x)$$

be a system of ordinary differential equations, in addition let γ be an invertible matrix. Then γ is a *symmetry* of the ordinary differential equation if

$$f(\gamma x) = \gamma f(x).$$

Example:

- Natural symmetry of the Lorenz equation is an example of a symmetry of a differential equation.

References

- [GSS] Golubitsky, Martin. Stewart, Ian. Schaeffer, G. David: Singularities and Groups in Bifurcation Theory (*Volume II*). Springer-Verlag, New York, 1988.