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## subdifferentiable mapping

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Author matte (1858)
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Let X be a Banach space, and let  $X^*$  be the dual space of X. For a function  $f: X \to \mathbb{R}$ , and  $x \in X$ , let us define

$$\partial f(x) = \{r^* \in X^* : f(x) - f(y) \le r^*(x - y) \text{ for all } y \in X\}.$$

If  $\partial f(x)$  is non-empty, then f is *subdifferentiable* at  $x \in X$ , and if  $\partial f(x)$  is non-empty for all x, then f is *subdifferentiable* [?, ?].

## References

- [1] C. Zalinescu, Convex Analysis in General Vector Spaces, World Scientific Publishing Company, 2002.
- [2] R.T. Rockafellar, Convex Analysis, Princeton University Press, 1996.