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bound on error of Simpson's rule

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If f is Riemann integrable on $[a, b]$ and $|f^{(4)}(x)| \leq M$ for all $x \in [a, b]$,
then

$$\left| \int_a^b f(x) \, dx - \left(\frac{b-a}{3n} \right) \left(f(a) + f(b) + 4 \sum_{j=1}^{\frac{n}{2}} f\left(a + \frac{(b-a)(2j-1)}{n}\right) + 6 \sum_{j=1}^{\frac{n-2}{2}} f\left(a + \frac{(b-a)(2j)}{n}\right) \right) \right| \leq \frac{M(b-a)^5}{180n^4}$$