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right hand rule

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The *right hand rule* for computing the Riemann integral $\int_a^b f(x) dx$ is

$$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{j=1}^n f\left(a + j\left(\frac{b-a}{n}\right)\right) \left(\frac{b-a}{n}\right).$$

If the Riemann integral is considered as a measure of area under a curve, then the expressions $f\left(a + j\left(\frac{b-a}{n}\right)\right)$ the of the rectangles, and $\frac{b-a}{n}$ is the common of the rectangles.

The Riemann integral can be approximated by using a definite value for n rather than taking a limit. In this case, the partition is $\left\{ \left[a, a + \frac{b-a}{n} \right), \dots, \left[a + \frac{(b-a)(n-1)}{n}, b \right] \right\}$ and the function is evaluated at the endpoints of each of these intervals. Note that this is a special case of a <http://planetmath.org/RightRiemannSumright> Riemann sum in which the x_j 's are evenly spaced.