



Math for the people, by the people.

## Balian-Low

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**Theorem 1 (Balian-Low)** *Suppose  $g \in L^2(\mathbb{R})$  and  $g_{m,n}(x) = e^{2\pi imx}g(x - n)$ , where  $m, n \in \mathbb{Z}$ . If  $\{g_{m,n} : m, n \in \mathbb{Z}\}$  is an orthonormal basis for  $L^2(\mathbb{R})$ , then either*

$$\int_{-\infty}^{\infty} x^2 |g(x)|^2 dx = \infty \text{ or } \int_{-\infty}^{\infty} \xi^2 |\hat{g}(\xi)|^2 d\xi = \infty.$$