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## hyperplane

Canonical name Hyperplane

Date of creation 2013-03-22 15:15:12 Last modified on 2013-03-22 15:15:12 Owner georgical (7242)

Last modified by georgiosl (7242)

Numerical id 9

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Entry type Definition
Classification msc 46H05
Defines real hyperplane
Defines complex hyperplane

Let E be a linear space over a field k. A hyperplane H in E is defined as the set of the form

$$H = \{x \in E : f(x) = a\}$$

where  $a \in k$  and f is a nonzero linear functional,  $f: E \to k$ . If  $k = \mathbb{R}$  or  $\mathbb{C}$ , then H is called a *real hyperplane* or *complex hyperplane* respectively.

**Remark**. When  $k = \mathbb{C}$ , the word "hyperplane" also has a more restrictive meaning: it is the zero set of a complex linear functional (by setting a = 0 above).