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isometric isomorphism

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Owner Gorkem (3644)
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Author Gorkem (3644)
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Defines isometrically isomorphic

Let $(X, \|\ \|_X)$ and $(Y, \|\ \|_Y)$ be normed vector spaces. A surjective linear map $T\colon X\to Y$ is called an $isometric\ isomorphism$ between X and Y if

$$||Tx||_Y = ||x||_X$$
, for all $x \in X$.

In this case, X and Y are said to be isometrically isomorphic.

Two isometrically isomorphic normed vector spaces share the same , so they are usually identified with each other.