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Gelfand-Naimark representation theorem

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The Gelfand-Naimark representation theorem is as follows:

Theorem 1.1

Every C^ -algebra is isometrically isomorphic to a norm closed $*$ -subalgebra $\mathbb{B}_{nc}(\mathcal{H})$ of an algebra $\mathbb{B}(\mathcal{H})$ of bounded operators on some Hilbert space \mathcal{H} . In particular, every finite dimensional C^* -algebra is isomorphic to a direct sum of matrix algebras.*