Serre-Swan theorem

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Let X be a compact Hausdorff space. Let $\mathbf{Vec}(X)$ be the category of complex vector bundles over X. And, let $\mathbf{ProjMod}(C(X))$ be the category of finitely generated projective modules over the C^*-algebra $C(X)$. There is a functor $\Gamma\colon \mathbf{Vec}(X) \to \mathbf{ProjMod}(C(X))$ which sends each complex vector bundle $E \to X$ to the $C(X)$-module $\Gamma(X, E)$ of continuous sections.

The functor Γ is an equivalence of categories.