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**submersion**

Canonical name	Submersion
Date of creation	2013-03-22 15:28:49
Last modified on	2013-03-22 15:28:49
Owner	pbruin (1001)
Last modified by	pbruin (1001)
Numerical id	4
Author	pbruin (1001)
Entry type	Definition
Classification	msc 53-00
Classification	msc 57R50
Related topic	Immersion

A differentiable map  $f: X \rightarrow Y$  differential manifolds  $X$  and  $Y$  is called a *submersion at a point*  $x \in X$  if the tangent map

$$Tf(x): TX(x) \rightarrow TY(f(x))$$

between the tangent spaces of  $X$  and  $Y$  at  $x$  and  $f(x)$  is surjective.

If  $f$  is a submersion at every point of  $X$ , then  $f$  is called a *submersion*. A submersion  $f: X \rightarrow Y$  is an open mapping, and its image is an open submanifold of  $Y$ .

A fibre bundle  $p: X \rightarrow B$  over a manifold  $B$  is an example of a submersion.