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## commuting vector fields

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Vector fields X, Y on a manifold are *commuting* at  $p \in M$  if

$$[X,Y]_p = 0$$

where  $[\cdot, \cdot]$  is the Lie bracket.

If S is a subset of M, then we say that vector fields X and Y commute on S if they commute at every point of S. In the case where S = M, i.e. when the vector fields commute at every point of the manifold, then we simply say that X and Y are commute.

A set V of vector fields on a manifold is said to be commuting on a set S if, for every pair of vector fields  $A \in V$  and  $B \in V$ , it is the case that A and B commute.

If S is an open set and V is a set of commuting vector fields on S, then the cardinality of V is not greater than the dimension of the manifold and one can find a local coordinate system about any point of S for which these vector fields are coordinate vector fields.