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## differential propositional calculus : appendix 3

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# Contents

## 0.1 Taylor Series Expansion

Taylor Series Expansion  $Df = df + d^2f$

	$df = \partial_x f \cdot dx + \partial_y f \cdot dy$	$d^2f = \partial_{xy} f \cdot dx \, dy$	$df _{x=y}$	$df _{x=(y)}$	$df _{(x)=y}$	$df _{(x)(y)}$
$f_0$	0	0	0	0	0	0
$f_1$	$(y) \, dx + (x) \, dy$	$dx \, dy$	0	$dx$	$dy$	$dx + dy$
$f_2$	$y \, dx + (x) \, dy$	$dx \, dy$	$dx$	0	$dx + dy$	$dy$
$f_4$	$(y) \, dx + x \, dy$	$dx \, dy$	$dy$	$dx + dy$	0	$dx$
$f_8$	$y \, dx + x \, dy$	$dx \, dy$	$dx + dy$	$dy$	$dx$	0
$f_3$	$dx$	0	$dx$	$dx$	$dx$	$dx$
$f_{12}$	$dx$	0	$dx$	$dx$	$dx$	$dx$
$f_6$	$dx + dy$	0	$dx + dy$	$dx + dy$	$dx + dy$	$dx + dy$
$f_9$	$dx + dy$	0	$dx + dy$	$dx + dy$	$dx + dy$	$dx + dy$
$f_5$	$dy$	0	$dy$	$dy$	$dy$	$dy$
$f_{10}$	$dy$	0	$dy$	$dy$	$dy$	$dy$
$f_7$	$y \, dx + x \, dy$	$dx \, dy$	$dx + dy$	$dy$	$dx$	0
$f_{11}$	$(y) \, dx + x \, dy$	$dx \, dy$	$dy$	$dx + dy$	0	$dx$
$f_{13}$	$y \, dx + (x) \, dy$	$dx \, dy$	$dx$	0	$dx + dy$	$dy$
$f_{14}$	$(y) \, dx + (x) \, dy$	$dx \, dy$	0	$dx$	$dy$	$dx + dy$
$f_{15}$	0	0	0	0	0	0

## 0.2 Partial Differentials and Relative Differentials

### Partial Differentials and Relative Differentials

	$f$	$\frac{\partial f}{\partial x}$	$\frac{\partial f}{\partial y}$	$\mathrm{d} f = \frac{\partial f}{\partial x} \mathrm{d} x + \frac{\partial f}{\partial y} \mathrm{d} y$	$\frac{\partial f}{\partial x} \Big _f$	$\frac{\partial f}{\partial y} \Big _f$
$f_0$	$()$	0	0	0	0	0
$f_1$	$(x)(y)$	$(y)$	$(x)$	$(y) \mathrm{d} x + (x) \mathrm{d} y$		
$f_2$	$(x) y$	$y$	$(x)$	$y \mathrm{d} x + (x) \mathrm{d} y$		
$f_4$	$x (y)$	$(y)$	$x$	$(y) \mathrm{d} x + x \mathrm{d} y$		
$f_8$	$x y$	$y$	$x$	$y \mathrm{d} x + x \mathrm{d} y$		
$f_3$	$(x)$	1	0	$\mathrm{d} x$		
$f_{12}$	$x$	1	0	$\mathrm{d} x$		
$f_6$	$(x, y)$	1	1	$\mathrm{d} x + \mathrm{d} y$		
$f_9$	$((x, y))$	1	1	$\mathrm{d} x + \mathrm{d} y$		
$f_5$	$(y)$	0	1	$\mathrm{d} y$		
$f_{10}$	$y$	0	1	$\mathrm{d} y$		
$f_7$	$(x y)$	$y$	$x$	$y \mathrm{d} x + x \mathrm{d} y$		
$f_{11}$	$(x (y))$	$(y)$	$x$	$(y) \mathrm{d} x + x \mathrm{d} y$		
$f_{13}$	$((x) y)$	$y$	$(x)$	$y \mathrm{d} x + (x) \mathrm{d} y$		
$f_{14}$	$((x)(y))$	$(y)$	$(x)$	$(y) \mathrm{d} x + (x) \mathrm{d} y$		
$f_{15}$	$(( ))$	0	0	0	0	0