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## catacaustic

Canonical name Catacaustic

Date of creation 2013-03-22 18:52:56 Last modified on 2013-03-22 18:52:56

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Numerical id 10

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Entry type Definition
Classification msc 53A04
Classification msc 51N20
Classification msc 26B05
Classification msc 26A24
Synonym caustic

Related topic HeronsPrinciple

Related topic ExampleOfFindingCatacaustic

Given a plane curve  $\gamma$ , its *catacaustic* (Greek  $\varkappa\alpha\tau\acute{\alpha}\,\varkappa\alpha\upsilon\sigma\tau\iota\varkappa\acute{o}\varsigma$  'burning along') is the envelope of a family of rays reflected from  $\gamma$  after having emanated from a point (which may be infinitely far, in which case the rays are initially parallel).

For example, the catacaustic of a logarithmic spiral reflecting the rays emanating from the origin is a congruent spiral. The catacaustic of the http://planetmath.org/ExponentialFunctionexponential curve  $y=e^x$  reflecting the vertical rays x=t is the catenary  $y=\cosh(x+1)$ .