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## oriented cobordism

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Two oriented n-manifolds M and M' are called cobordant if there is an oriented n+1 manifold with boundary N such that  $\partial N = M \coprod M'^{opp}$  where  $M'^{opp}$  is M' with orientation reversed. The triple (N, M, M') is called a  $oriented\ cobordism$ . Cobordism is an equivalence relation, and a very coarse invariant of manifolds. For example, all surfaces are cobordant to the empty set (and hence to each other).

There is a cobordism category, where the objects are manifolds, and the morphisms are cobordisms between them. This category is important in topological .