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topics on low dimensional topology

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Related topic	Topology

List of topic on low dimensional topology that should be here at PM

1 Manifolds in general

- manifold
- homotopy, homotopy groups,
- isotopy, mapping class group, homeotopy
- homology and cohomology
- fiber bundle, characteristic classes
- piecewise linear topology
- topological methods in group theory
- CW complex

2 1-manifolds

- real line vs projective line
- circle from a Euclidean loop to a Lie group
- curve
- knot, link and Jones polynomial. Prime knots
- torus knots
- braid
- loop and string, Witten M-Theory
- fundamental group
- graph and graph theory

3 2-manifolds

- Mobius strip
- surface
- two sphere
- torus
- projective plane
- Klein bottle
- genus (genus of topological surface)
- Euler characteristic (Euler's polyhedron formula)
- Gaussian curvature
- Nielsen-Thurston classification of surface homeomorphisms

4 3-manifolds

- \mathbb{R}^3 Euclidean three-space
- S^3 three sphere, $SO(3)$, $SU(2)$
- surface bundle
- circle bundle, lens space, <http://planetmath.org/SeifertFiberSpaceSeifert> fiber space
- homology sphere
- Poincare conjecture
- Dehn's lemma, loop theorem, sphere theorem
- annulus and torus theorems
- Hopf bundle

5 4-manifolds

- Donaldson's theory
- quaternions
- relativity, space-time
- surface bundles over surfaces
- spin structures
- there are homeomorphic four-manifolds with differentiable structures each, which make them non-diffeomorphic.
- gauge theory: monopoles
- classification of simply connected 4-manifolds
- intersection form
- geometrization

6 Mathematical physics