



Math for the people, by the people.

simple random sample

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A sample  $S$  of size  $n$  from a population  $U$  of size  $N$  is called a *simple random sample* if

1. it is a sample without replacement, and
2. the probability of picking this sample is equal to the probability of picking any other sample of size  $n$  from the same population  $U$ .

From the first part of the definition, there are  $\binom{N}{n}$  samples of  $n$  items from a population of  $N$  items. From the second part of the definition, the probability of any sample of size  $n$  in  $U$  is a constant. Therefore, the probability of picking a particular simple random sample of size  $n$  from a population of size  $N$  is  $\binom{N}{n}^{-1}$ .

**Remarks** Suppose  $x_1, x_2, \dots, x_n$  are values representing the items sampled in a simple random sample of size  $n$ .

- The sample mean  $\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$  is an unbiased estimator of the true population mean  $\mu$ .
- The sample variance  $s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$  is an unbiased estimator of  $S^2$ , where  $(\frac{N-1}{N})S^2 = \sigma^2$  is the true variance of the population given by

$$\sigma^2 := \frac{1}{N} \sum_{i=1}^N (x_i - \bar{x})^2.$$

- The variance of the sample mean  $\bar{x}$  from the true mean  $\mu$  is

$$\left( \frac{N-n}{nN} \right) S^2.$$

The larger the sample size, the smaller the deviation from the true population mean. When  $n = 1$ , the variance is the same as the true population variance.