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Pareto random variable

Canonical name ParetoRandomVariable

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Synonym Pareto distribution

X is a **Pareto random variable** with parameters a, b if $f_X(x) = \frac{ab^a}{x^{a+1}}, x \in [b, \infty)$ Parameters:

$$J_X(x) = \frac{x}{x^{a+1}}, x \in [$$

$$\star \quad a \in (0, \infty)$$

$$\star \quad b \in (0, \infty)$$

Syntax:

$$X \sim Pareto(a, b)$$

Notes:

- 1. X represents a random variable with shape parameter a and scale parameter b.
- 2. The expected value of X is noted as $E[X] = \frac{ab}{a-1}$ with $a \in \{2, 3, \ldots\}$
- 3. The variance of X is noted as $Var[X] = \frac{ab^2}{(a-1)^2(a-2)}, \ a \in \{3,4,\ldots\}$
- 4. The cumulative distribution function of X is noted as $F(x) = 1 (\frac{b}{x})^a$
- 5. The moments of X around 0 are noted as $E[X^n] = \frac{ab^n}{a-n}, n \in \{1, 2, ..., a-1\}$