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negative binomial random variable

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Synonym	negative binomial distribution

X is a *negative binomial random variable* with parameters r and p if

$$f_X(x) = \binom{r+x-1}{x} p^r (1-p)^x, \quad x = \{0, 1, \dots\}$$

Parameters:

$$\star \quad r > 0$$

$$\star \quad p \in [0, 1]$$

Syntax:

$$X \sim \text{NegBin}(r, p)$$

Notes:

1. If $r \in \mathbb{N}$, X represents the number of failed Bernoulli trials before the r th success. Note that if $r = 1$ the variable is a geometric random variable.
2. $E[X] = r \frac{1-p}{p}$
3. $\text{Var}[X] = r \frac{1-p}{p^2}$
4. $M_X(t) = \left(\frac{p}{1-(1-p)e^t} \right)^r$