

**SUBJECT CODE: 102405CS**  
**B.Tech.- 4<sup>th</sup> Semester Examination April-May 2022**  
**Specialization: Theory of Computation**  
**Course: B.TECH**

Maximum Marks: 100

Time Allowed: 3 Hours

Minimum Pass Marks: 35

**Note: Attempt all questions. Part A of each question is compulsory and carries 4 marks; attempt any two parts from B, C and D carrying 8 marks.**

Q. No.	Question		Marks															
1	A	Differentiate between DFA and NFA.	4															
	B	<p>Explain Moore and Mealy Machine. Construct Moore machine which is equivalent to the Mealy machine given in the diagram.</p>	8															
	C	<p>Construct equivalent DFA for NFA  <math>M= (\{p, q, r, s\}, \{0,1\}, \delta, p, \{s\})</math>, where <math>\delta</math> is given below:</p> <table> <tr> <td></td> <td>0</td> <td>1</td> </tr> <tr> <td><math>\rightarrow p</math></td> <td>p, q</td> <td>p</td> </tr> <tr> <td>q</td> <td>r</td> <td>r</td> </tr> <tr> <td>r</td> <td>s</td> <td>--</td> </tr> <tr> <td><math>\bigcirc s</math></td> <td>s</td> <td>s</td> </tr> </table>		0	1	$\rightarrow p$	p, q	p	q	r	r	r	s	--	$\bigcirc s$	s	s	8
		0	1															
$\rightarrow p$	p, q	p																
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r	s	--																
$\bigcirc s$	s	s																
D	State and prove Myhill-Nerode theorem	8																
2	A	<p>Write the regular expression</p> <ol style="list-style-type: none"> <li>Any string formed using <math>\{0,1\}</math> with 1 as the fourth symbol from the end.</li> <li>first character 'a' or 'c' followed by any string in 'b'.</li> <li>All strings of a's and b's ending in aa.</li> </ol>	4															

		4. The set of strings containing ab as a substring	
	B	For the following regular expressions, draw the corresponding finite automata:  (i) $(0+1)^*0(0+11)^*$ (ii) $10+(0+11)0^*1$	8
	C	List the identities of regular expressions. State and prove Arden's theorem.	8
	D	Give the statement of pumping lemma. List its applications. Using pumping Lemma prove that the language $\{0^n1^n \mid n \geq 0\}$ is not regular.	8
3	A	Consider production rules of a CFG : $S \rightarrow bA/aB$ , $A \rightarrow aS/aAA/a$ , $B \rightarrow bS/aBB/b$ . Find leftmost and rightmost derivations for string $w=aaabbabbba$	4
	B	Define GNF. Construct a grammar in Greibach normal form equivalent to  $S \rightarrow YY \mid 0$ , $Y \rightarrow SS \mid 1$ .	8
	C	Explain Chomsky classification of languages by giving example and discuss the relation between the classes of these languages.	8
	D	Reduce the following grammar to Chomsky Normal Form :  $S \rightarrow 1A \mid 0B$ , $A \rightarrow 1AA \mid 0S \mid 0$ , $B \rightarrow 0BB \mid 1S \mid 1$	8
4	A	Design a PDA M to accept the language $L=\{0^n1^{n+2} \mid n \geq 1\}$	4
	B	Trace the sequence of moves made for each of the input strings $bbcb$ and $baca$ for the PDA for the grammar $S \rightarrow aSa/bSb/c$	8
	C	What is Instantaneous Description? What are moves made by the Turing Machine in the processing of the string. i) 00 ii) 0101	8

Present State	Tape Symbol		
	b	0	1
$\rightarrow q_1$	1Lq2	0Rq1	--
q2	bRq3	0Lq2	1Lq2
q3	---	bRq4	bRq5
q4	0Rq5	0Rq4	1Rq4
q5	0Lq2	--	--

		<table border="1"> <tr> <th>Present State</th> <th colspan="3">Tape Symbol</th> </tr> <tr> <td></td> <td>b</td> <td>0</td> <td>1</td> </tr> <tr> <td>→q1</td> <td>1Lq2</td> <td>0Rq1</td> <td>--</td> </tr> <tr> <td>q2</td> <td>bRq3</td> <td>0Lq2</td> <td>1Lq2</td> </tr> <tr> <td>q3</td> <td>---</td> <td>bRq4</td> <td>bRq5</td> </tr> <tr> <td>q4</td> <td>0Rq5</td> <td>0Rq4</td> <td>1Rq4</td> </tr> <tr> <td>q5</td> <td>0Lq2</td> <td>--</td> <td>--</td> </tr> </table>	Present State	Tape Symbol				b	0	1	→q1	1Lq2	0Rq1	--	q2	bRq3	0Lq2	1Lq2	q3	---	bRq4	bRq5	q4	0Rq5	0Rq4	1Rq4	q5	0Lq2	--	--	
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	D	<p>Write short notes on</p> <p>(i) Universal Turing Machine</p> <p>(ii) Church's Hypothesis</p>	8																												
5	A	Explain space and time complexity theory.	4																												
	B	<p>State and explain Post correspondence problem. List its applications. Find the solution to the instance of PCP given in Table.</p> <table border="1"> <tr> <td>i</td> <td>x<sub>i</sub></td> <td>y<sub>i</sub></td> </tr> <tr> <td>1</td> <td>0</td> <td>000</td> </tr> <tr> <td>2</td> <td>01000</td> <td>01</td> </tr> <tr> <td>3</td> <td>01</td> <td>1</td> </tr> </table>	i	x <sub>i</sub>	y <sub>i</sub>	1	0	000	2	01000	01	3	01	1	8																
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C	<p>What are decidable and undecidable problem. Give the properties of recursive and recursively enumerable language.</p>	8																													
D	<p>Ackermann's function is defined by</p> $A(0, y) = y+1$ $A(x+1, 0) = A(x, 1)$ $A(x+1, y+1) = A(x, A(x+1, y))$ <p>A(x, y) can be computed for every (x, y) and hence A(x, y) is total. Ackermann's function is not primitive but recursive. Compute A(1,1), A(2,1),A(1,2),A(2,2).</p>	8																													