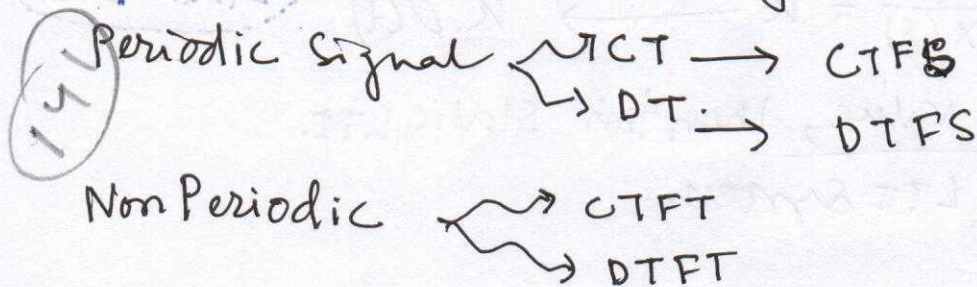


# Fourier Series Expansion

97

Fourier series expansion is used for <sup>①</sup>period signals to expand them in terms of their harmonics which are <sup>②</sup>Sinusoideal and <sup>③</sup>orthogonal to another.



- use of Laplace Transform  $\rightarrow$  Design Purpose (Cont Time)
- Fourier Transform  $\rightarrow$  Analysis
- Z transform  $\rightarrow$  Discrete Time.

## • Periodic Signal

$$x(t \pm T) = x(t)$$

Time Period

Fourier series Expansion condition check.

$\rightarrow$  Dirichlet cond<sup>n</sup>.

Harmonic  $f = \frac{\text{Cycles}}{\text{Sec}}$

$$x(t) = 2 \sin \omega t + 4 \sin 2\omega t + 7 \sin 3\omega t + \dots$$

First Harmonic

Even Harmonic

Odd Harmonic

$\omega \leftarrow$  Fundamental freq.

freq  $\rightarrow$  Rate of change

Effects of Third Harmonic move dominant.





Fourier Series  $\approx$  DC + sin + cosine

- DC + Sin
- DC + Cosine
- DC + Sin + Cosine.

$$\omega = 2\pi f$$

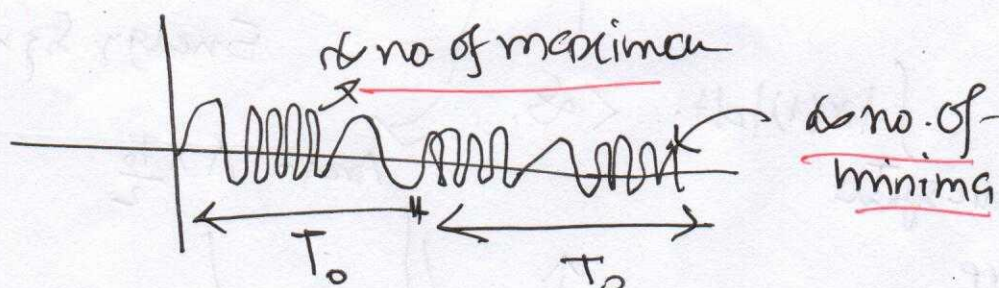
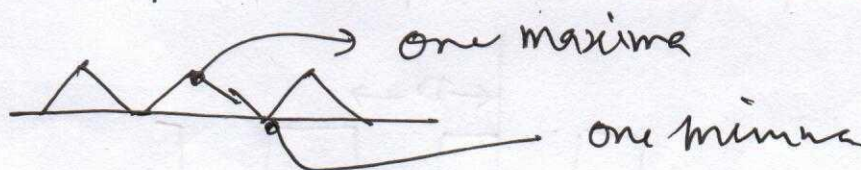
↑  
Fundamental  
Angular Freq.

- Trigonometric Fourier Series Expansion
- complex exp. Fourier "
- Polar/Harmonic " " "

Condition for existence of Fourier Series

Condition 1  $\rightarrow$  Signal should have finite number of maxima and minima over the range of time period.

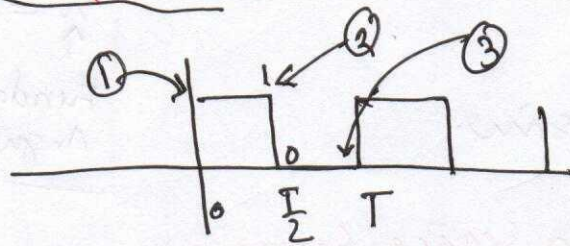
$\rightarrow$  means one Maxima and one minima over time period.



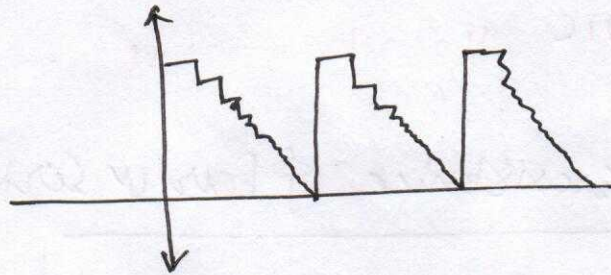
$$T_0 = 2T_1 = 4T_2 \dots$$



Condition 2: Periodic Signal should have finite number of discontinuities over the range of time period.



NO. of discontinuities is (3)



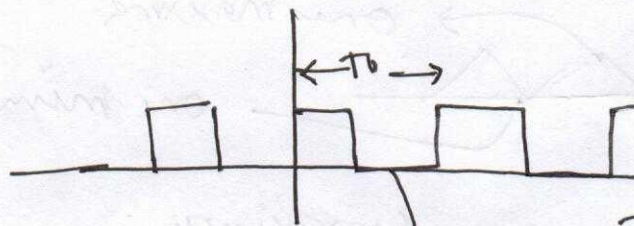
$$\begin{array}{c} h, w \\ \downarrow \quad \downarrow \\ \frac{h}{2} \quad \frac{w}{2} \end{array}$$

$\therefore$  So.  $\infty$  infinite discontinuities

$\therefore$  FS not possible

Condition-3

Signal should be absolutely integrable over the range of time period.

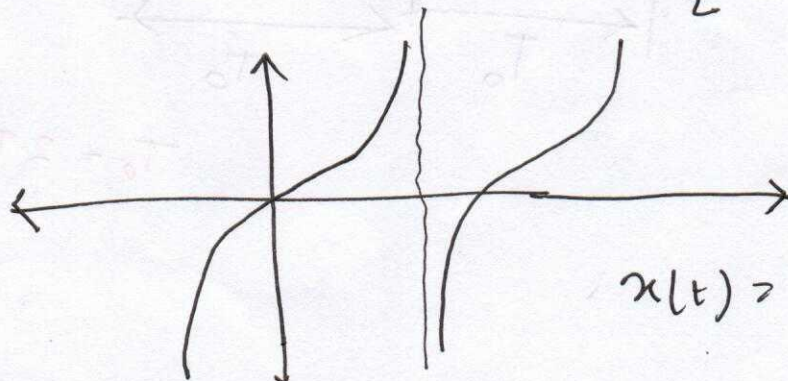


$$\int |x(t)| dt < \infty$$

Energy Signal

$$\text{Area} = A \times \frac{T_0}{2}$$

PS  $\rightarrow$  Periodic signal  
 $\rightarrow$  NENP



$$x(t) = \tan t$$