



**DEPARTMENT OF COMPUTER ENGINEERING, MODELING,
ELECTRONICS AND SYSTEM ENGINEERING**

Antenna and Propagation

MATLAB Exercises Report

Group Members

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Lab 1

1. Graph the Sine and cosine function in [rad] and [deg], with : $0 < \theta < 2\pi$

```
% Define the parameters
f = 1*10^9; % Frequency of the wave in Hz
T = 1/f; % Period of the wave in seconds
omega = 2 * pi * f; % Angular frequency in rad/s
theta = 0:0.01:2*pi;
thetaDegree = 0:1:2*pi*180/pi;
x = sin(theta);
x1 = sind(thetaDegree);
y = cos(theta);
y1 = cosd(thetaDegree);
```

```
figure;
subplot(2, 2, 1);
plot(theta, x);
title('Sine function in Radian');
xlabel('\theta (radians)');
ylabel('sin(\theta)');
```

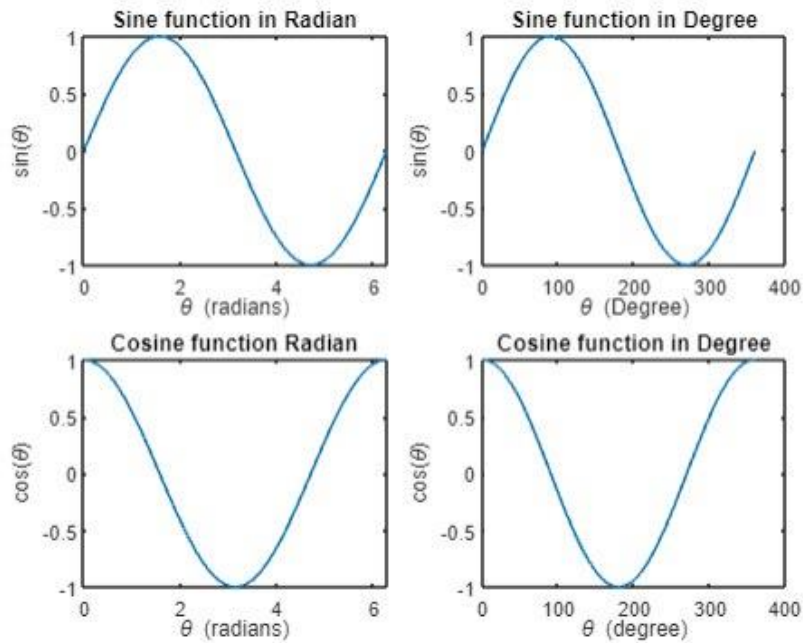
```
subplot(2, 2, 2);
plot(thetaDegree, x1);
title('Sine function in Degree');
xlabel('\theta (Degree)');
ylabel('sin(\theta)');
```

```
subplot(2, 2, 3);
```

```
plot(theta, y);
title('Cosine function Radian');
xlabel('\theta (radians)');
ylabel('cos(\theta)');
```

```
subplot(2, 2, 4);
```

```
plot(thetaDegree, y1);
title('Cosine function in Degree');
xlabel('\theta (degree)');
ylabel('cos(\theta)');
```



% plot sine and cosine in one graph using radian and degree

% define parameters

frequency = 1; % Frequency of the wave in Hz

period = 1 / frequency; % Period of the wave in seconds

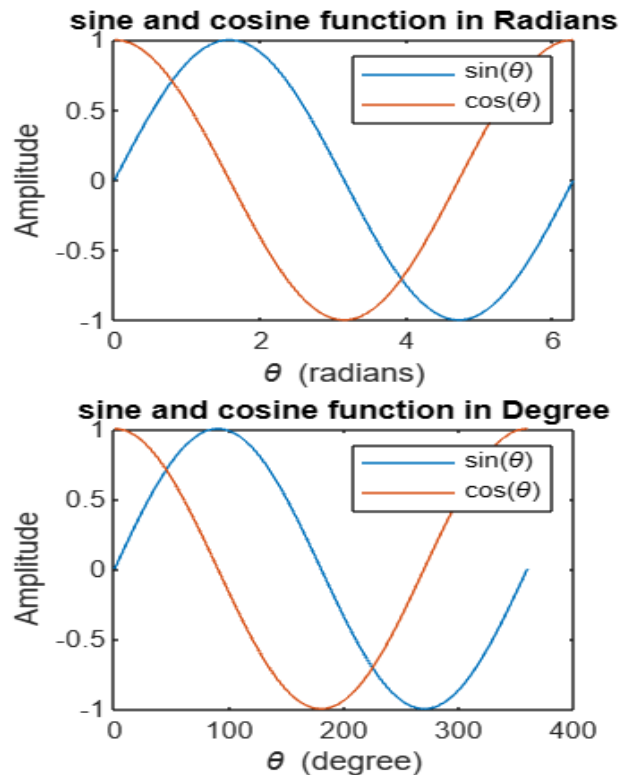
omega = 2 * pi * frequency; % Angular frequency in rad/s

theta = 0:0.01:2*pi; % Radians

thetaDegree = 0:1:2*pi*180/pi; % Degrees with finer spacing

```
figure(1);
subplot(2, 2, 1);
plot(theta, sin(theta));
hold on;
plot(theta, cos(theta));
title('sine and cosine function in Radians');
xlabel('\theta (radians)');
ylabel('Amplitude');
legend('sin(\theta)', 'cos(\theta)')
```

```
subplot(2, 2, 3);
plot(thetaDegree, sind(thetaDegree)); % Use sind for degrees
hold on;
plot(thetaDegree, cosd(thetaDegree)); % Use cosd for degrees
title('sine and cosine function in Degree');
xlabel('\theta (degree)');
ylabel('Amplitude');
legend('sin(\theta)', 'cos(\theta)')
```



2. Graph the $\cos(\omega t)$ and $\sin(\omega t)$, with a frequency of 1GHz.

```
% plot cos( wt) and sin(wt) in separate graphs and then both in single graph;
% Define the parameters
f = 1*10^9; % Frequency of the wave in Hz
T = 1/f; % Period of the wave in seconds
omega = 2 * pi * f; % Angular frequency in rad/s
t= 0: T/100: 2*T;
x = sin(omega*t);

figure;
subplot(2, 2, 1);
plot(t, x);
title('Sine function');
xlabel('Time[s]');
ylabel('sin(\omegat)');

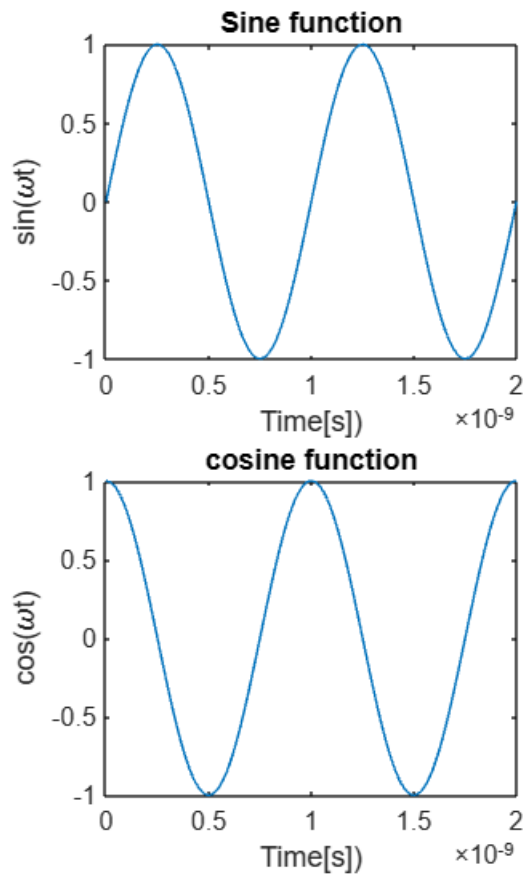
subplot(2, 2, 3);
y = cos(omega*t);
plot(t, y);
title('cosine function');
xlabel('Time[s]');
ylabel('cos(\omegat)');

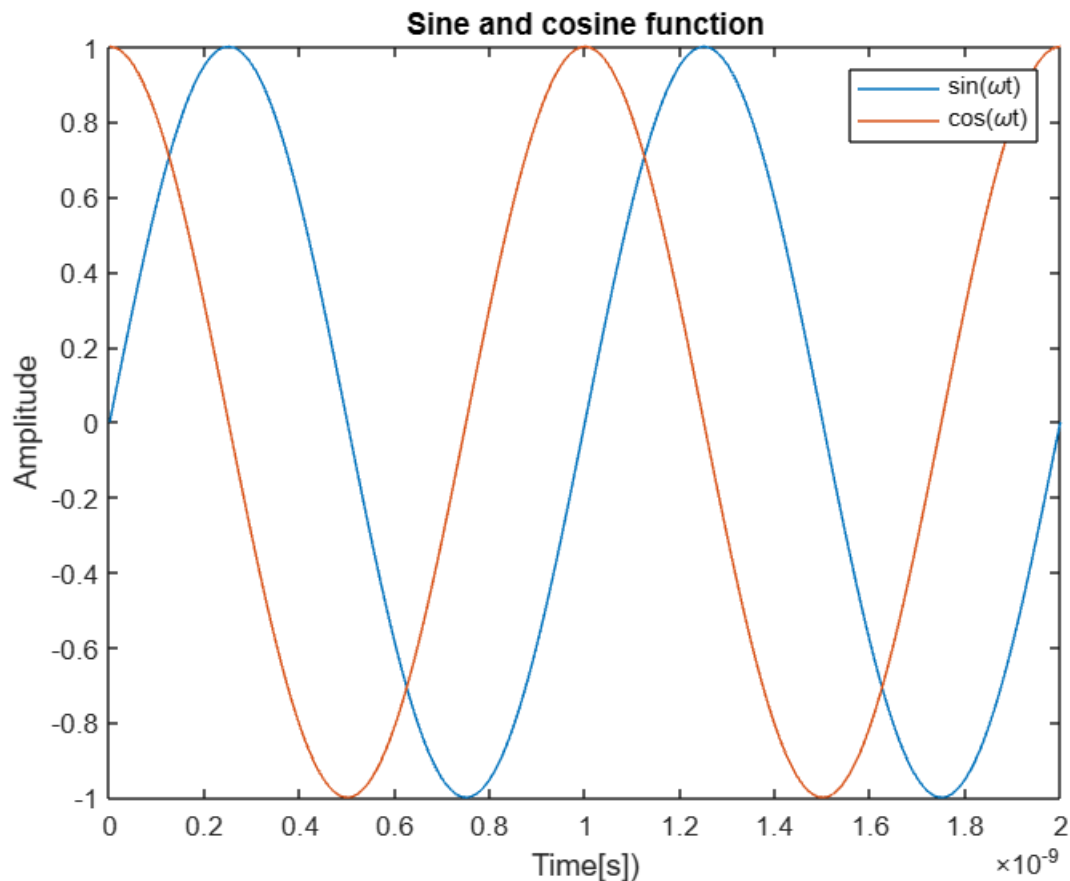
figure(2);

plot(t, x);

hold on;
y = cos(omega*t);
plot(t, y);
```

```
title('Sine and cosine function');  
xlabel('Time[s]');  
ylabel('Amplitude');  
legend('sin(\omegat)', 'cos(\omegat)')
```





3. Graph the $\sin(\omega t + \phi)$, with a frequency of 1GHz and phase: $\phi = \pi/4$ and $\phi = -\pi/4$

```
% Define the parameters
f = 1*10^9; % Frequency of the wave in Hz
T = 1/f; % Period of the wave in seconds
omega = 2 * pi * f; % Angular frequency in rad/s
t = 0: T/100: 2*T;
phi = pi/4;

%cosine

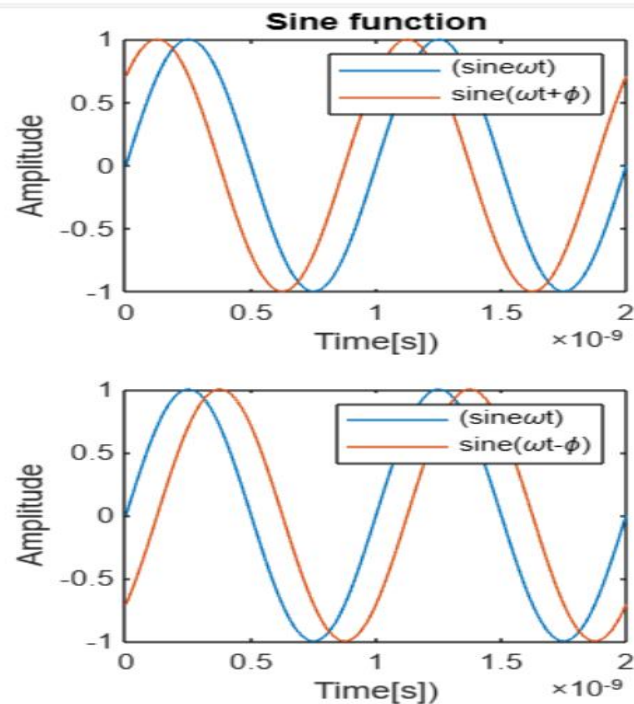
u = sin(omega*t);
v = sin(omega*t+phi);
w = sin(omega*t-phi);
figure(2);
subplot(2, 2, 1);
plot(t, u);
hold on
plot(t, v);
title('sin function');
xlabel('Time[s]');
ylabel('Amplitude');
legend("(sin\omegat)", "sin(\omegat+\phi)");

subplot(2, 2, 3);
plot(t, u);
hold on
```

```

plot(t,w);
title('sin function');
xlabel('Time[s]');
ylabel('Amplitude');
legend("(sin\omegat)", "sin(\omegat-\phi)");

```



4. Graph the $\cos(\omega t + \phi)$, with a frequency of 1GHz and phase: $\phi = \pi/4$ and $\phi = -\pi/4$

```

f = 1*10^9; % Frequency of the wave in Hz
T = 1/f; % Period of the wave in seconds
omega = 2 * pi * f; % Angular frequency in rad/s
t= 0: T/100: 2*T;
phi=pi/4;
%cos
u = cos(omega*t);
v=cos(omega*t+phi);
w=cos(omega*t-phi);
figure(2);
subplot(2, 2, 2);
plot(t,u);
hold on
plot(t,v);
title('cos function');
xlabel('Time[s]');
ylabel('Amplitude');
legend("(cos\omegat)", "cos(\omegat+\phi)");

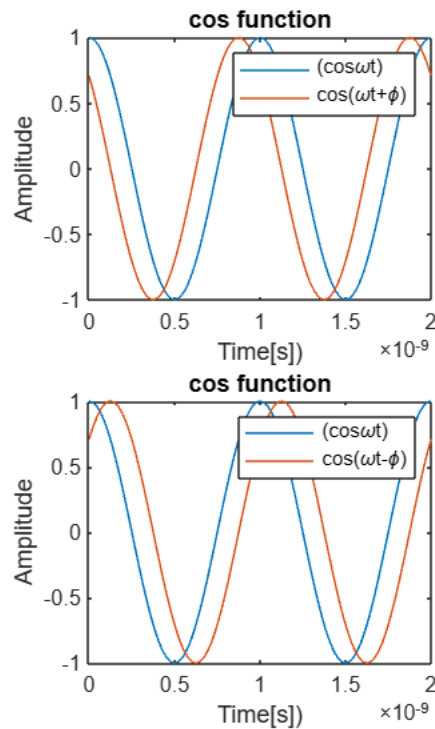
subplot(2, 2, 4);
plot(t, u);
hold on
plot(t,w);

```

```

xlabel('Time[s]');
ylabel('Amplitude');
legend("(cos\omegat)", "cos(\omegat-\phi)");

```



5. Graph the $\sin(\omega t + \phi)$ and $\cos(\omega t + \phi)$, with a frequency of 1GHz and different phases using for loop: $[\phi_1=0, \phi_2=\pi/4, \phi_3=\pi/2]$

```

% Define the parameters
f= 3*10^9;
phases = [0, pi/4, pi/2];
T= 1/f;
t= 0:T/100:2*T;
phase=0;
yPhase = zeros(length(t),length(phases));

figure;
subplot(2,2,1)
hold on
for i= 1: length(phases)
yPhase = cos(2*pi*f*t + phases(i));
plot(t,yPhase);

end
title("cosine function")
xlabel("time[s]")
ylabel("Amplitude")
legend("cos (\omegat + 0)", "cos (\omegat + \pi/4)", "cos (\omegat + \pi/2)");

subplot(2,2,3)
hold on
for i= 1: length(phases)
yPhase = sin(2*pi*f*t + phases(i));

```

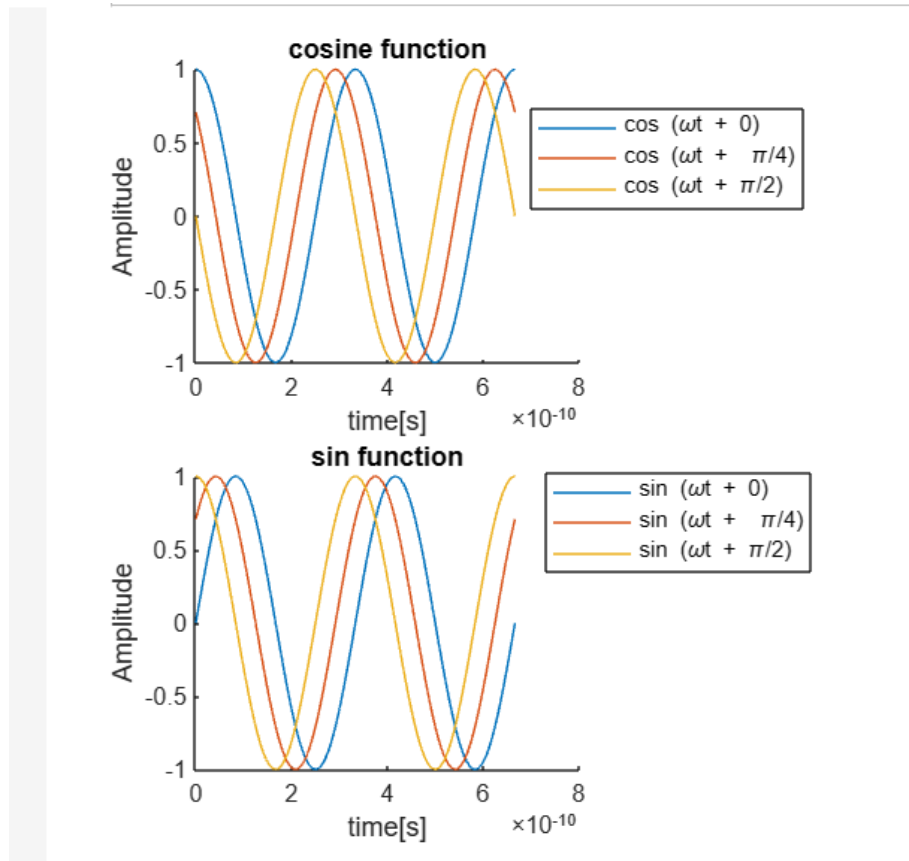


```

plot(t,yPhase);

end
title("sin function")
xlabel("time[s]")
ylabel("Amplitude")
legend("sin (\omegat + 0)", "sin (\omegat + \pi/4)", "sin (\omegat + \pi/2)");

```



Lab 2

1.Graph of the function: $u(z, t) = A \cos(\omega t - kz)$. For $z=0, t=0$ and 3-D

```

f = 3*10^9;
T= 1/f;
A = 1;
Eo = 8.85*10^-12;
No=pi*4*10^-7;
c=(Eo*No)^-0.5;
lambda=c/f;
k = 2*pi/lambda;
t= 0:T/100:3*T;
t0=0;
z1=0;
z = 0:lambda/100:3*lambda;
u = zeros(length(t), length(z));

```

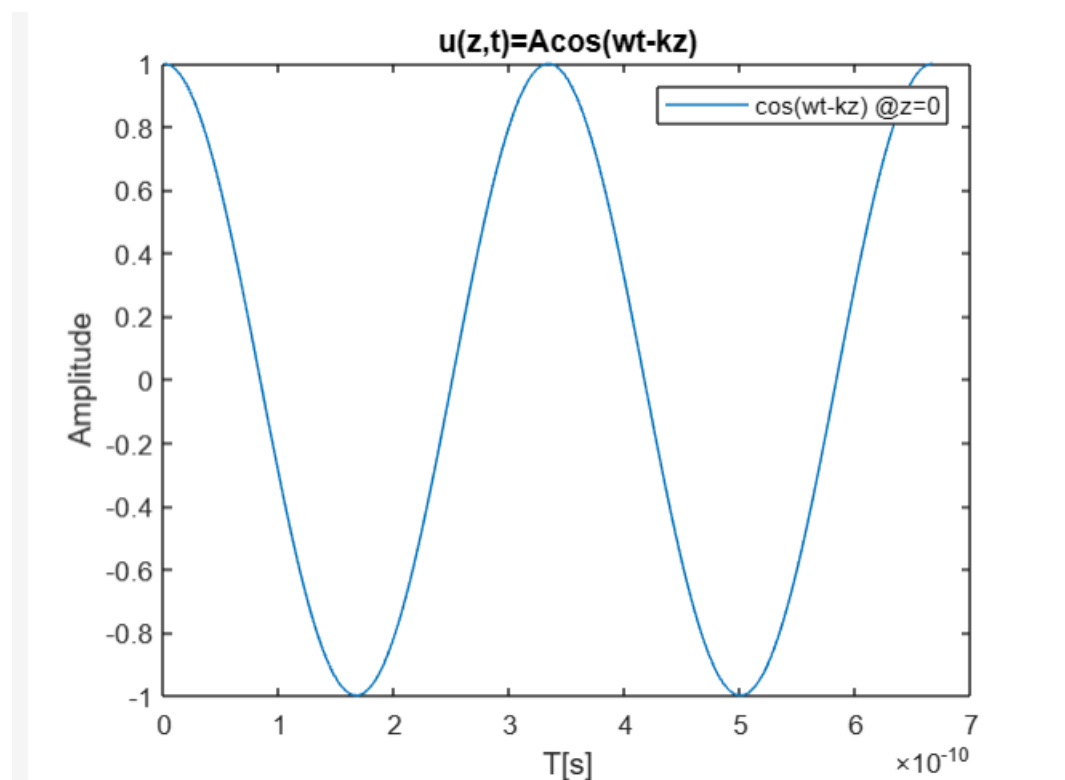
```

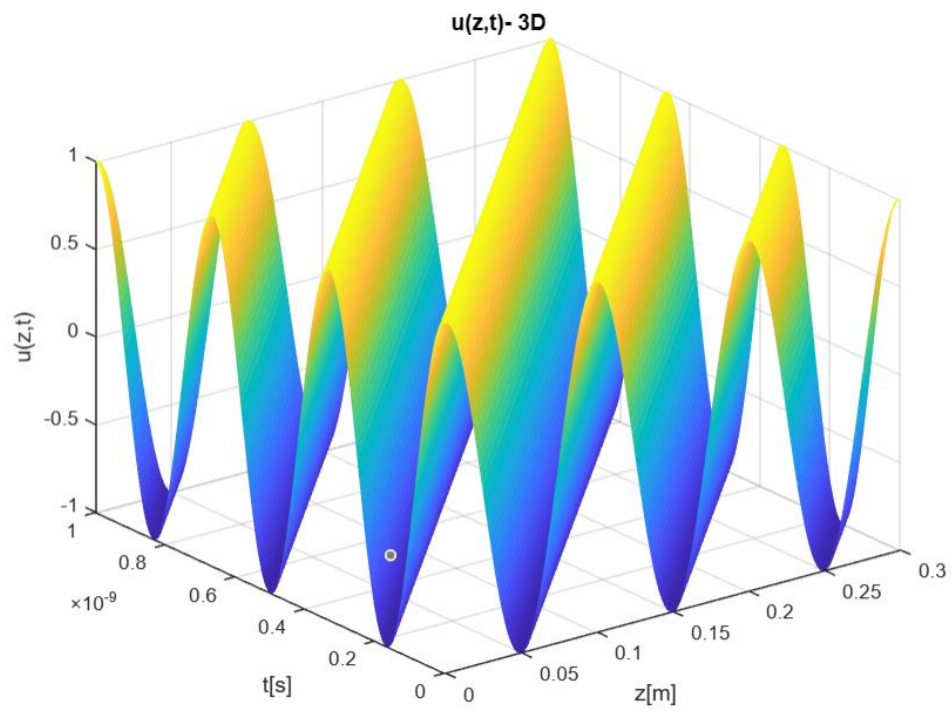
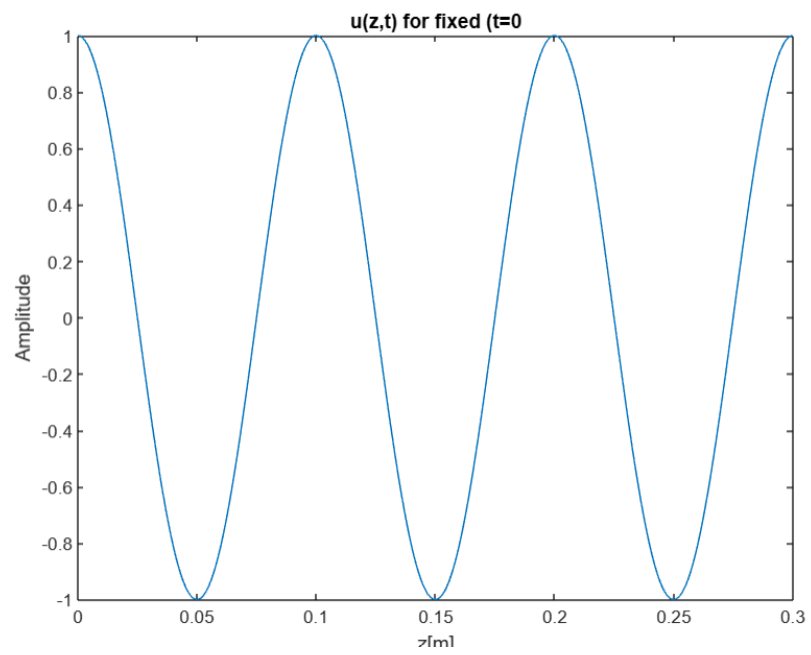
figure;
u1 = A*cos(2*pi*f*t- k*z1);
plot(z,u1);
xlabel("T[s]");
ylabel("Amplitude");
title("u(z,t) for fixed (z=0)");

figure(1);
u1 = A*cos(2*pi*f*t0- k*z);
plot(z,u1);
xlabel("z[m]");
ylabel("Amplitude");
title("u(z,t) for fixed (t=0)");

for i = 1: length(z)
    u(:,i) = A*cos(2*pi*f*t- k*z(i));
end
figure(2);
mesh(z,t,u);
xlabel("z[m]");
ylabel("t[s]");
zlabel("u(z,t)");
title("u(z,t)- 3D");

```





Lab 3

1. Graph the function: $u(z, t) = A \cos(\omega t - kz)$ for fixed $t=0$ at different frequency using for loop.

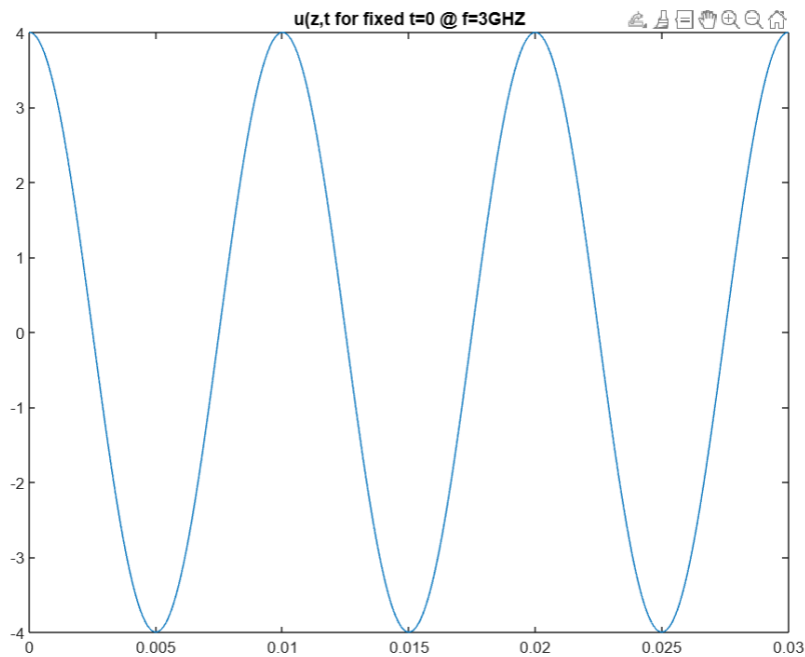
```
f = [3*10^9,10*10^9,30*10^9];
A = 4;
Eo = 8.85*10^-12;
No=pi*4*10^-7;
c=(Eo*No)^-0.5;

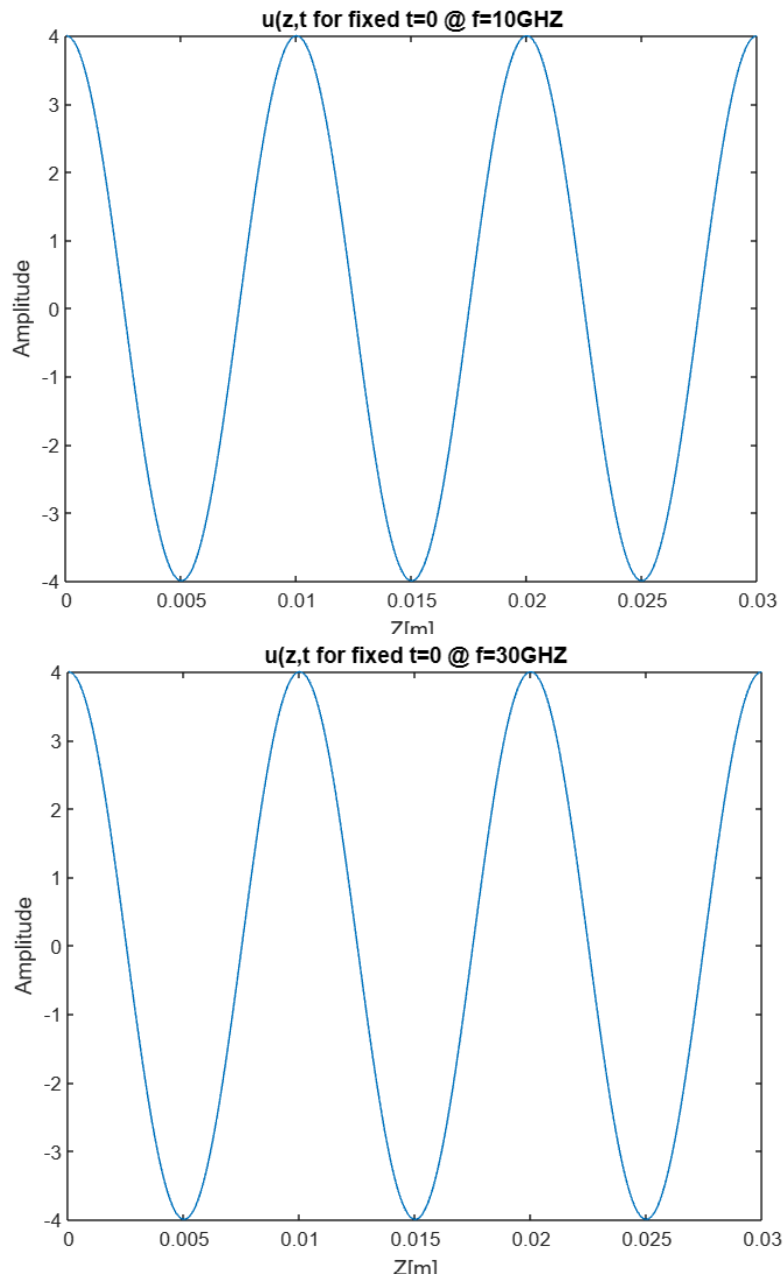
t0=0;
for i = 1: length(f)
    lambda=c/f(i);
    k = 2*pi/lambda;
    z = 0:lambda/100:3*lambda;
    u1= A*cos(2*pi*f(i)*t0- k*z);
    figure(1);
    plot(z,u1);

    title("u(z,t for fixed t=0 @ f=3GHZ")
    ylabel("Amplitude");
    xlabel("Z[m]");

    figure(2)
    title("u(z,t for fixed t=0 @ f=10GHZ")
    ylabel("Amplitude");
    xlabel("Z[m]");

    figure(3)
    title("u(z,t for fixed t=0 @ f=30GHZ")
    ylabel("Amplitude");
    xlabel("Z[m]");
end
```





2. Graph the function in 3D: $u(z, t) = A \cos(\omega t - kz)$ at different frequency using for loop.

```
f = [3*10^9,10*10^9,30*10^9];
A = 4;
Eo = 8.85*10^-12;
No=pi*4*10^-7;
c=(Eo*No)^-0.5;

for i = 1:length(f)
    T = 1/f(i);
    t = 0:T/100:2*T; % Moved this line here
    lambda = c/f(i);
    k = 2*pi/lambda;
```

```

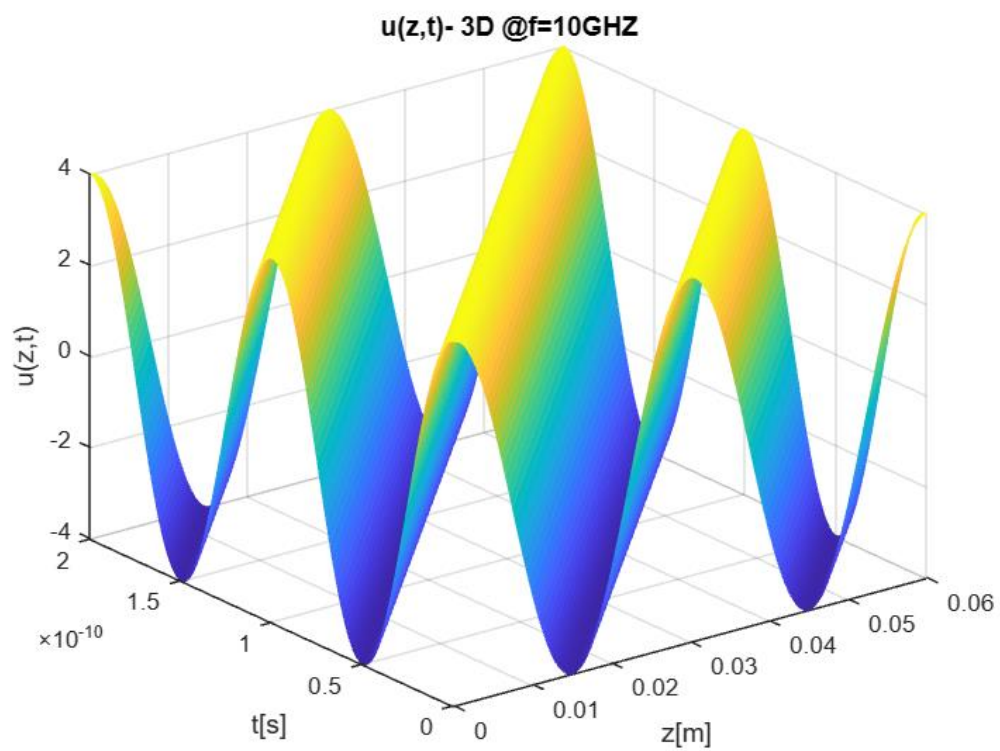
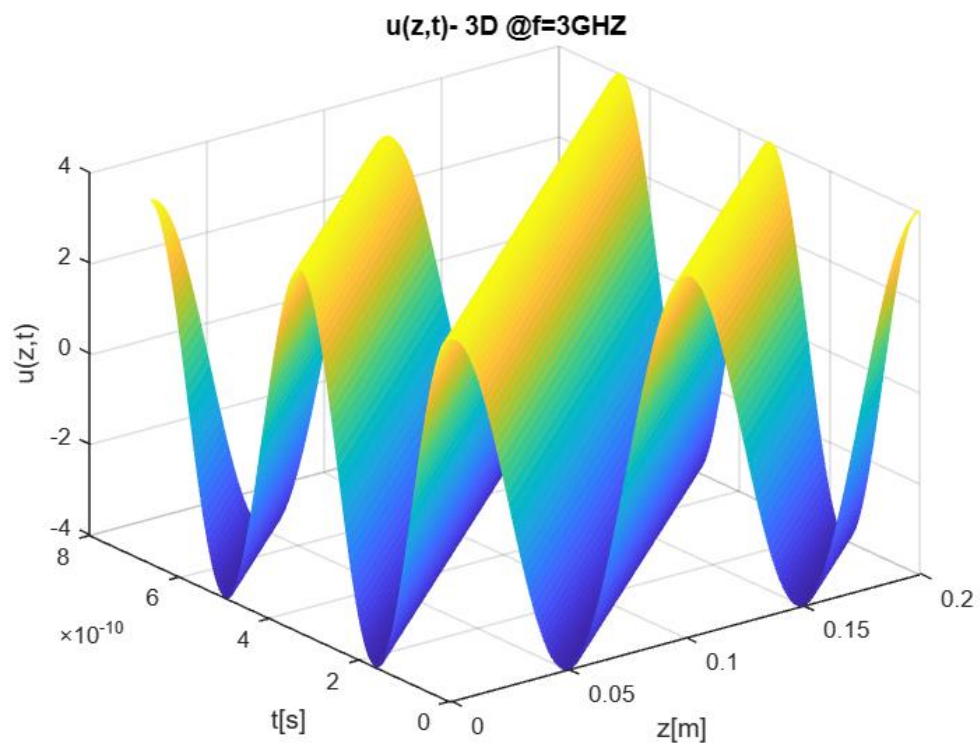
z = 0:lambda/100:2*lambda;
u = zeros(length(t), length(z));
for x = 1: length(z)
    u(:,x) = A*cos(2*pi*f(i).*t - k*z(x));

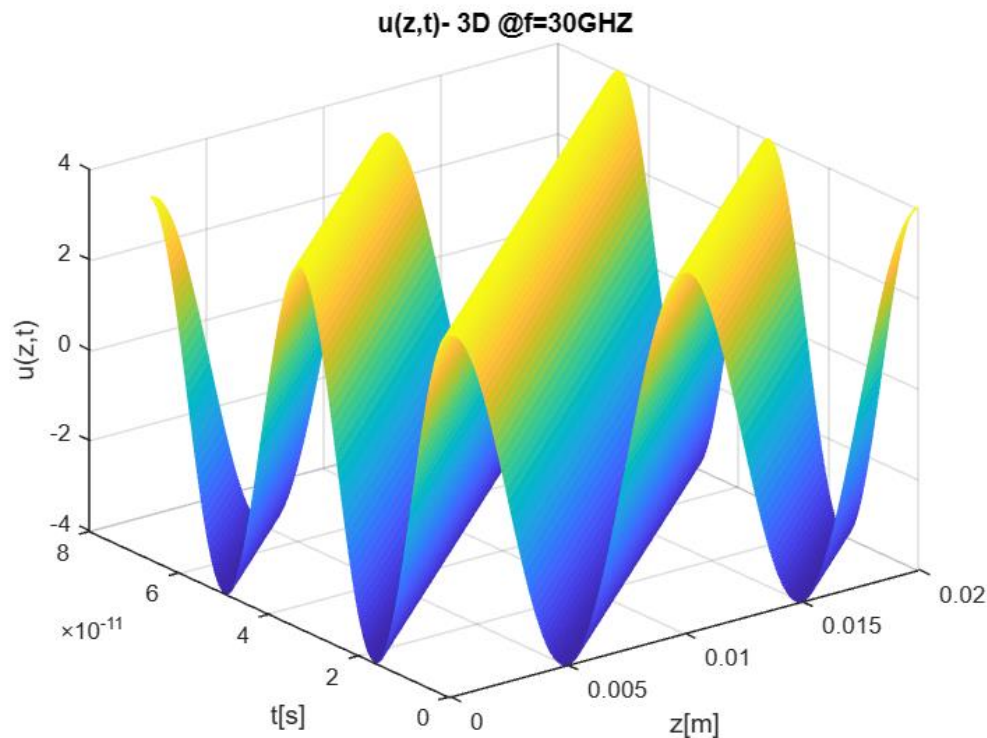
end
figure(1);
mesh(z,t,u);
xlabel("z[m]");
ylabel("t[s]");
zlabel("u(z,t)");
title("u(z,t)- 3D @f=3GHZ");

figure(2);
mesh(z,t,u);
xlabel("z[m]");
ylabel("t[s]");
zlabel("u(z,t)");
title("u(z,t)- 3D @f=10GHZ");

figure(3);
mesh(z,t,u);
xlabel("z[m]");
ylabel("t[s]");
zlabel("u(z,t)");
title("u(z,t)- 3D @f=30GHZ");
end

```





Lab 4

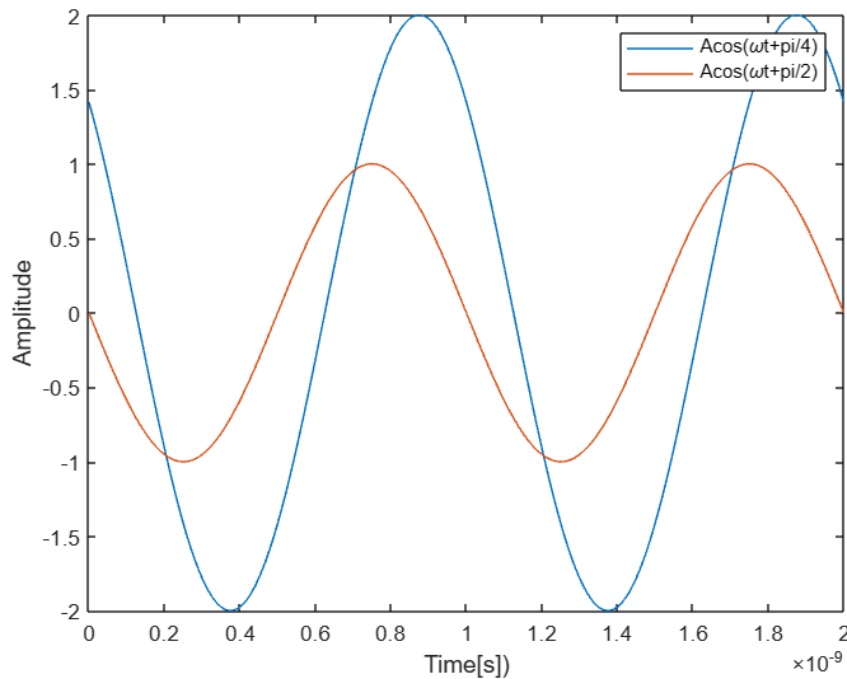
1. Converting this phasor to time domain: $U = Ae^{j\phi}$. Considering two cases:

1) $A_1=2$, $\phi_1=45$ degrees

2) $A_2=1$, $\phi_2=90$ degrees

$u(t) = \text{Re}(U e^{j\omega t})$

```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
t=0:T/100:2*T;
phi1=pi/4;
phi2=pi/2;
A1=2;
A2=1;
U1=A1*exp(1i*phi1);
U2=A2*exp(1i*phi2);
u1_t=real(U1*exp(1i*w*t));
u2_t=real(U2*exp(1i*w*t));
figure;
plot(t,u1_t);
hold on
plot(t,u2_t);
xlabel('Time[s]');
ylabel('Amplitude');
legend("Acos(\omegat+pi/4)", "Acos(\omegat+pi/2)");
```

2. Converting the phasor of Electric Field to its instantaneous expression at $z=0$ and z different from zero using 3D

$$\underline{E} = \hat{x} E_0 e^{-jkz}$$

$$\underline{e}(z, t) = \text{Re}(\underline{E} e^{j\omega t})$$

```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
t=0:T/100:2*T;
E0=2;
z=0;
c=3*10^8;
lambda=c/f;
z1=0:lambda/100:2*lambda;
k=2*pi/lambda;
E=E0*exp(-1i*k*z);
e=real(E*exp(1i*w*t));

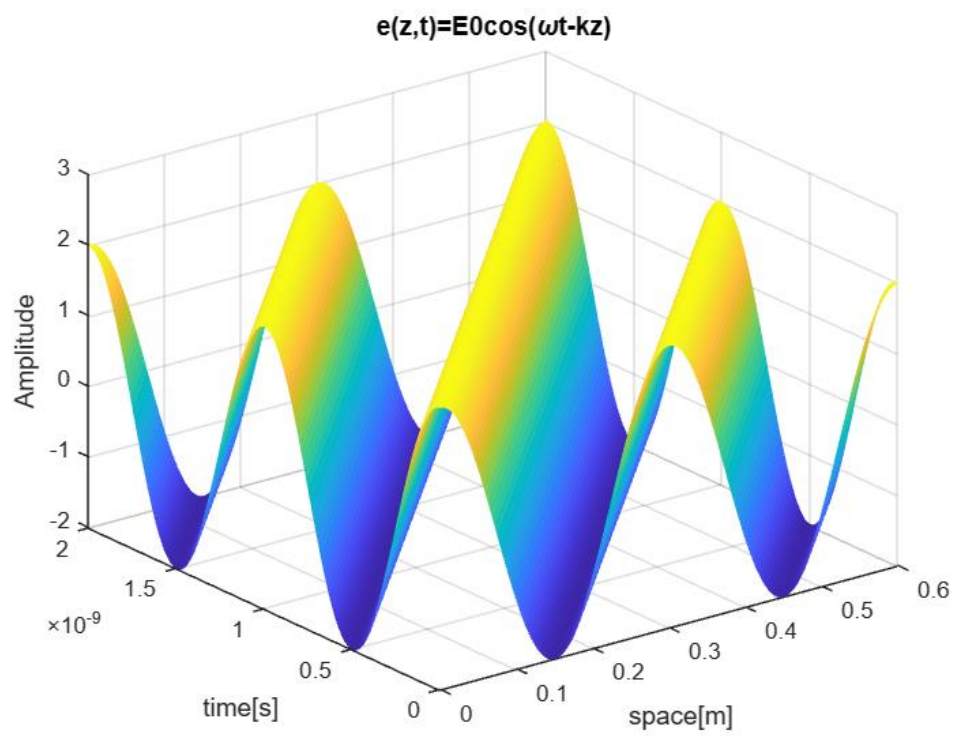
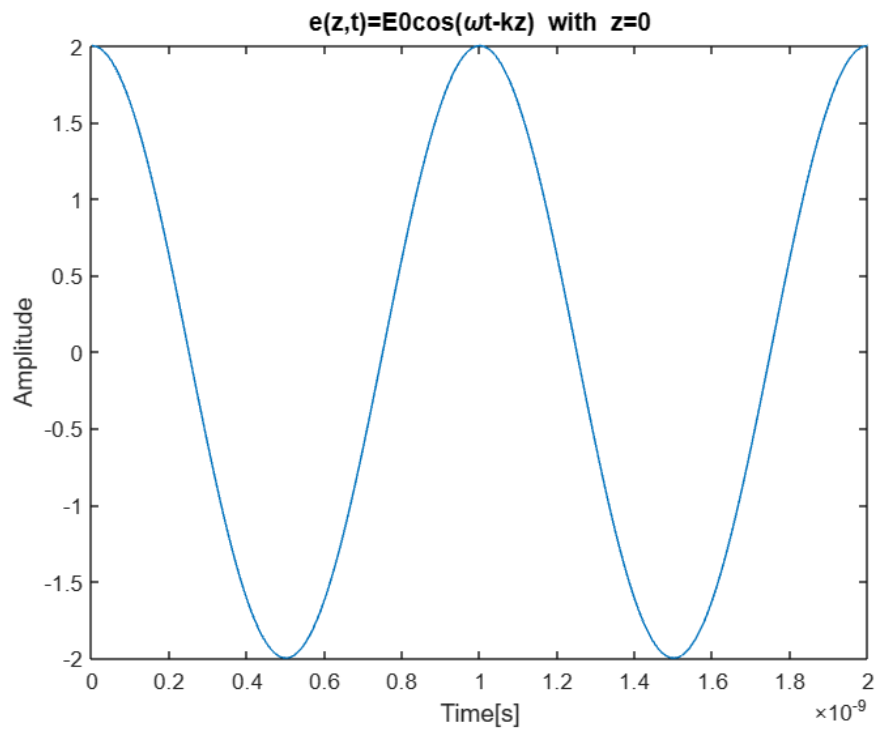
figure;
plot(t,e);
title("e(z,t)=E0cos(\omegat-kz) with z=0")
xlabel('Time[s]');
ylabel('Amplitude');

e1=zeros(length(t),length(z1));
for i=1:length(z1)
    E1=E0*exp(-1i*k*z1);
    e1(:,i)=real(E1*exp(1i*w*t(i)));
end
figure(2);
mesh(z1,t,e1)
```

```

title("e(z,t)=E0cos(\omegat-kz)")
xlabel('space[m]');
ylabel('time[s]');
zlabel("Amplitude")

```



Lab 5

1. Normal Incidence – Lossless Media

```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
c = 3 * 10^8;
t = 0 : T/100 : 2*T;
lambda = c/f;
E0 = 2;
er1 = 1;
ur1 = 1;
er2 = 3;
ur2 = 1;
e0 = 8.85*10^-12;
u0 = pi*4*10^-7;
e1 = e0*er1;
e2 = e0*er2;
u1 = u0*ur1;
u2 = u0 *ur2;
k1 = w*sqrt(e1*u1);
k2 = w*sqrt(e2*u2);
vp1 = 1/sqrt(e1*u1);
vp2 = 1/sqrt(e2*u2);
n1 = sqrt(u1/e1);
n2 = sqrt(u2/e2);
lambda1 = vp1/f;
lambda2 = vp2/f;
z1 = -3*lambda1 : lambda1/100 : 0;
z2 = 0 : lambda2/100 : 3*lambda2;
%reflection coefficient%
gamma = (n2-n1)/(n1+n2);
%transmission coefficient%
tr = 2*n2/(n1+n2);
Ei = E0*exp(-1i*k1*z1);
Er = E0*gamma*exp(1i*k1*z1);
Et = E0*tr*exp(-1i*k2*z2);
E1 = Ei + Er;
ei = zeros (length(t), length(z1));
er = zeros (length(t), length(z1));
etr = zeros (length(t),length(z2));
e1 = zeros (length(t), length(z1));
for x= 1: length(t)

    ei(x,:) = real(Ei*exp(1i*w*t(x)));
    er(x,:) = real(Er*exp(1i*w*t(x)));
    etr(x,:) = real(Et*exp(1i*w*t(x)));
    e1 (x,:) = real(E1*exp(1i*w*t(x)));

end
figure;
for y =1 : length(t)
    clf;
    plot(z1,ei(y,:))
    hold on;
    plot(z1,er(y,:))
    plot(z1,e1(y,:))
    plot(z2,etr(y,:))
```

```

    plot(z1,e1(y,:))

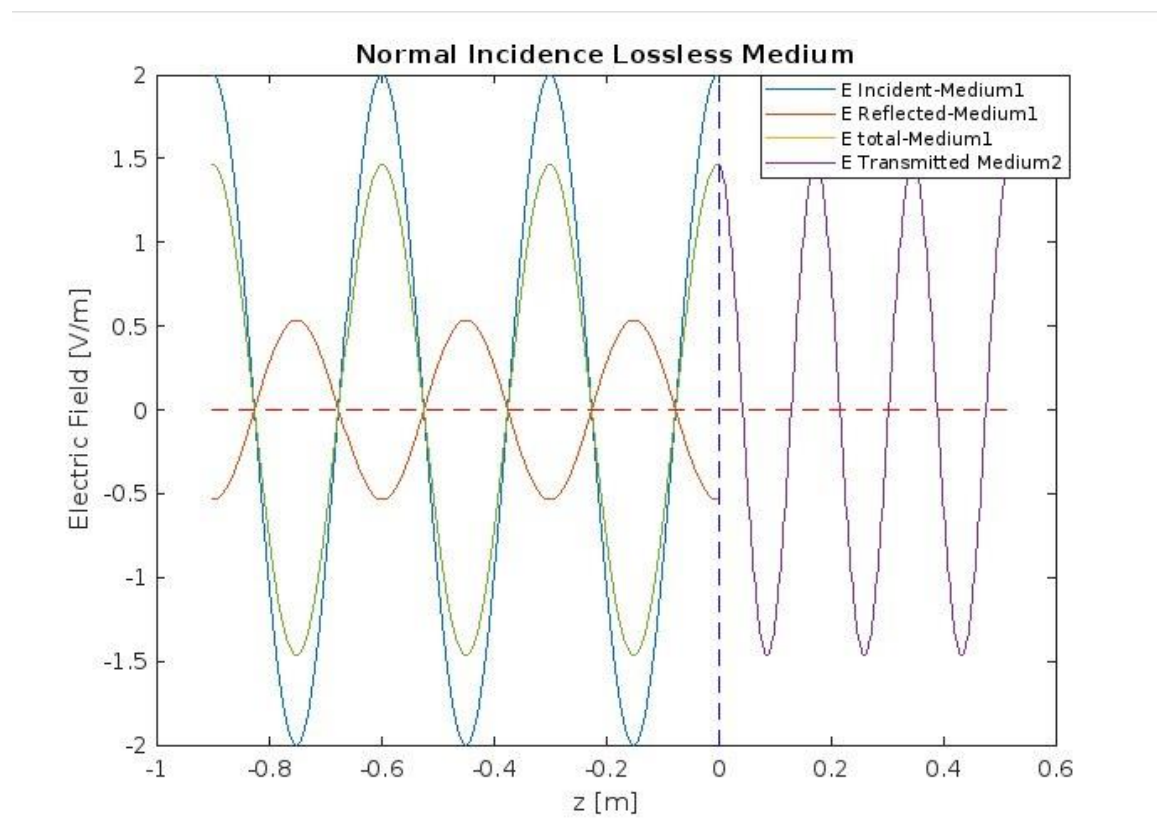
    pause(0.1);
end

a = [-3*lambda1, 3*lambda2]
b = [0,0];
c = [-E0,E0];
d = [0,0];

plot(a,b,'r',LineStyle='--');
plot(d,c,'b',LineStyle='--');

xlabel('z [m]')
ylabel('Electric Field [V/m]');
legend('E Incident-Medium1','E Reflected-Medium1','E total-Medium1','E
Transmitted Medium2','FontSize',8);
title('Normal Incidence Lossless Medium');

```



2.Normal Incidence – Lossy Media

```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
c = 3 * 10^8;
t = 0 : T/100 : 2*T;
lambda = c/f;
E0 = 2;
er1 = 1;
ur1 = 1;
er2 = 3;
ur2 = 1;
e0 = 8.85*10^-12;
u0 = pi*4*10^-7;
e1 = e0*er1;
e2 = e0*er2;
u1 = u0*ur1;
u2 = u0 *ur2;
sigma2 = 0.03
e = 2.71828;
A = 1/e;
k1 = w*sqrt(e1*u1);
k2 = w*sqrt((e2-j*sigma2/w)*u2);
%k1 = beta1-jalpha1;
%k2 = beta-jalpha2;
alpha1 = -imag(k1);
beta1 = real(k1);
alpha2 = -imag(k2);
beta2 = real(k2);
A1=1/alpha2
%vp1 = 1/sqrt(e1*u1);
%vp2 = 1/sqrt(e2*u2);
n1 = sqrt(u1/e1);
n2 = sqrt(j*w*u2/(sigma2+j*w*e2));
lambda1 = 2*pi/beta1;
lambda2 = 2*pi/beta2;
z1 = -3*lambda1 : lambda1/100 : 0;
z2 = 0 : lambda2/100 : 3*lambda2;
%reflection coefficient%
gamma = (n2-n1)/(n1+n2);
%transmission coefficient%
tr = 2*n2/(n1+n2);
Ei = E0*exp(-1i*k1*z1);
Er = E0*gamma*exp(1i*k1*z1);
Et = E0*tr*exp(-1i*k2*z2);
E1 = Ei + Er;
ei = zeros (length(t), length(z1));
er = zeros (length(t), length(z1));
etr = zeros (length(t),length(z2));
e1 = zeros (length(t), length(z1));

for x= 1: length(t)

    ei(x,:) = real(Ei*exp(1i*w*t(x)));
    er(x,:) = real(Er*exp(1i*w*t(x)));
    etr(x,:) = real(Et*exp(1i*w*t(x)));
end
```

```

    e1 (x,:) = real(E1*exp(1i*w*t(x)));

end
figure;
for y =1 : length(t)
    clf;
    plot(z1,ei(y,:))
    hold on;
    plot(z1,er(y,:))
    plot(z1,e1(y,:))
    plot(z2,etr(y,:))
    plot(z1,e1(y,:))

    amplitude = max(abs(tr*ei(y,:)));
    attenua = amplitude*exp(-alpha2*z2);
    plot(z2,attenua);

    %pause(0.1);
end

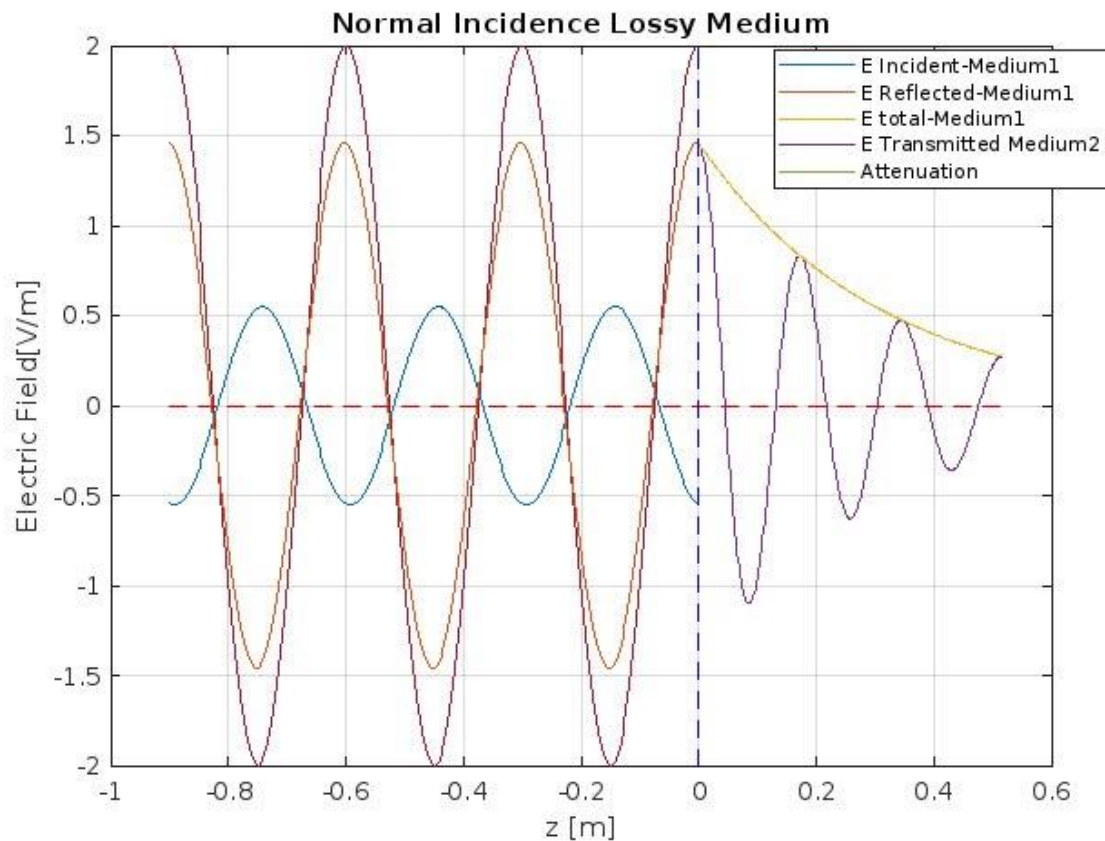
a = [-3*lambda1, 3*lambda2]
b = [0,0];
c = [-E0,E0];
d = [0,0];

amplitude = max(abs(tr*Ei(1,:)));
attenua = amplitude*exp(-alpha2*z2);
plot(z1,Ei (1,:));
hold on;
plot(z1,Er (1,:));
plot(z1,E1 (1,:));
plot(z2,abs(Et(1,:)));

plot(a,b,'r',LineStyle='--');
plot(d,c,'b',LineStyle='--');

xlabel('z [m]')
ylabel('Electric Field[V/m]');
legend('E Incident-Medium1','E Reflected-Medium1','E total-Medium1','E Transmitted Medium2','Attenuation','FontSize',8);
title('Normal Incidence Lossy Medium');
grid on;

```



3. Represent the Transmitted Electric Field in medium 2 (E_2), with its *attenuation* and *Penetration Depth* for $\sigma = 0.03$

```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
c = 3 * 10^8;
t = 0 : T/100 : 2*T;
lambda = c/f;


```

```

k1 = w*sqrt(e1*u1);
k2 = w*sqrt((e2-1i*sigma2/w)*u2);
alpha1 = -imag(k1);
beta1 = real(k1);
alpha2 = -imag(k2);
beta2 = real(k2);
%defining delta
A1=1/alpha2;
%defining intrinsic impedance n1 and n2
n1 = sqrt(u1/e1);
n2 = sqrt(1i*w*u2/(sigma2+1i*w*e2));
%defining lambda1 and lambda2
lambda1 = 2*pi/beta1;
lambda2 = 2*pi/beta2;
z2 = 0 : lambda2/200 : 3*lambda2;
%reflection coefficient(gamma)
gamma = (n2-n1)/(n1+n2);
%transmission coefficient%
tr = 2*n2/(n1+n2);
%transmitted electric field
Et = E0*tr*exp(-1i*k2*z2);
etr = zeros (length(t),length(z2));

for x= 1: length(t)
    etr(x,:) = real(Et*exp(1i*w*t(x)));
end

a = [0, 0.354639]
d = [0.354639,0.354639];
c = [0,0.488787];
b = [0.488787,0.488787];

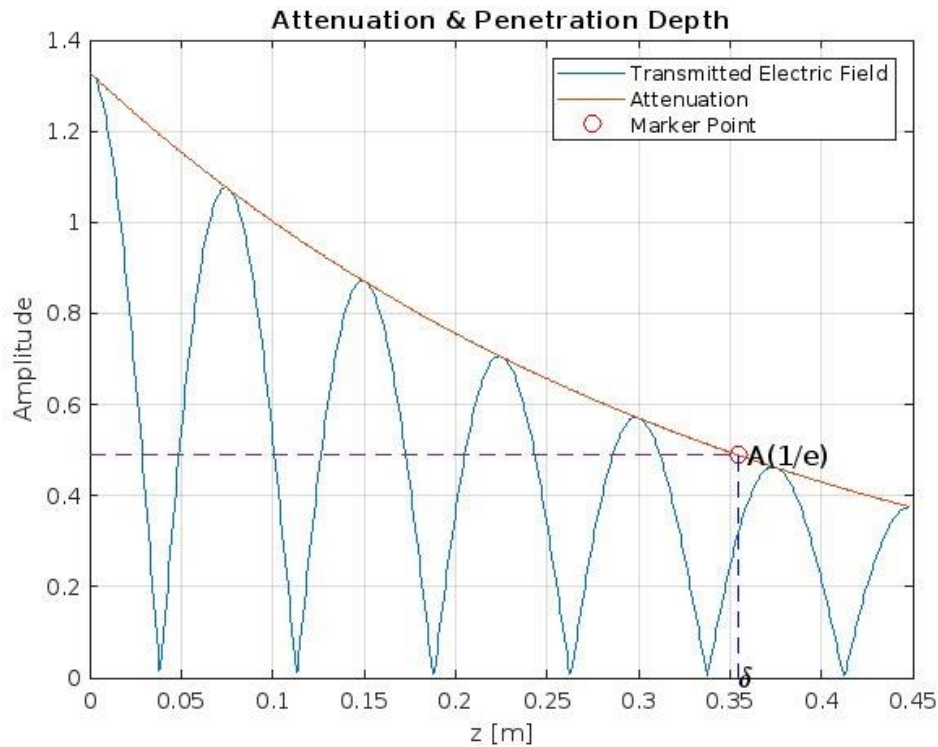
figure;
plot(z2,abs(etr(1,:)));
hold on;
%Attenuation
amplitude = max(Et(1,:));
attenua = amplitude*exp(-alpha2*z2);

plot(z2,attenua);
plot(A1,amplitude*A,'ro','MarkerSize',8);
text(0.354639,0.4887875,' A(1/e)',FontSize=12)
text(0.354639,0,'\delta', FontSize=12)

plot(a,b,'',LineStyle='--');
plot(d,c,'b',LineStyle='--');

xlabel('z [m]');
ylabel('Amplitude');
title('Attenuation & Penetration Depth');
legend('Transmitted Electric Field', 'Attenuation', 'Marker Point');
grid on;

```

4. Represent the Transmitted Electric Field in medium 2 (E_2), with its *attenuation* and *Penetration Depth* for $\sigma = 0.05$

```

c = 3 * 10^8;
t = 0 : T/100 : 2*T;
lambda = c/f;


```

```

beta2 = real(k2);
%defining delta
A1=1/alpha2;
%defining intrinsic impedance n1 and n2
n1 = sqrt(u1/e1);
n2 = sqrt(1i*w*u2/(sigma2+1i*w*e2));
%defining lambda1 and lambda2
lambda1 = 2*pi/beta1;
lambda2 = 2*pi/beta2;
z2 = 0 : lambda2/200 : 3*lambda2;
%reflection coefficient(gamma)
gamma = (n2-n1)/(n1+n2);
%transmission coefficient%
tr = 2*n2/(n1+n2);
%transmitted electric field
Et = E0*tr*exp(-1i*k2*z2);
etr = zeros (length(t),length(z2));

for x= 1: length(t)
    etr(x,:) = real(Et*exp(1i*w*t(x)));
end

a = [0, 0.2137]
d = [0.2137,0.2137];
c = [0,0.488787];
b = [0.488787,0.488787];

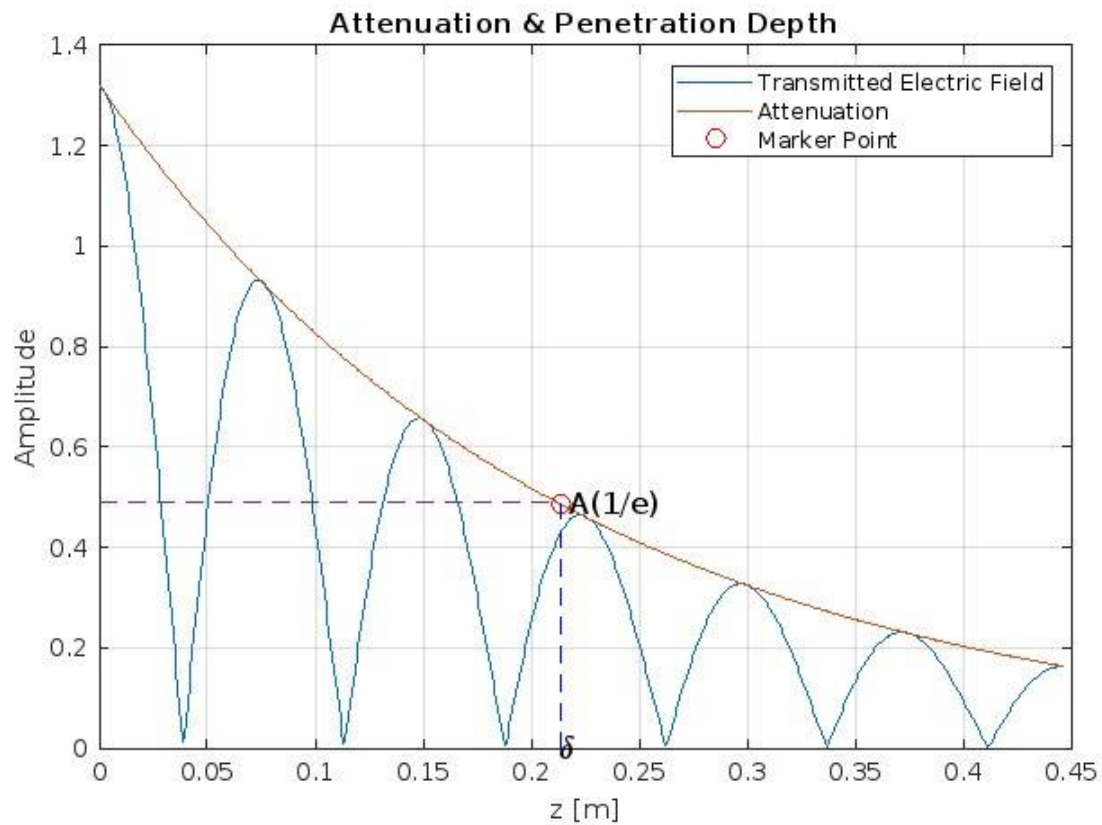
figure;
plot(z2,abs(etr(1,:)));
hold on;
%Attenuation
amplitude = max(Et(1,:));
attenua = amplitude*exp(-alpha2*z2);

plot(z2,attenua);
plot(A1,amplitude*A,'ro','MarkerSize',8);
text(0.2137,0.4887875,' A(1/e)',FontSize=12)
text(0.2137,0,'\sigma', FontSize=12)

plot(a,b,'',LineStyle='--');
plot(d,c,'b',LineStyle='--');

xlabel('z [m]');
ylabel('Amplitude');
title('Attenuation & Penetration Depth');
legend('Transmitted Electric Field', 'Attenuation', 'Marker Point');
grid on;

```



5. Represent the Transmitted Electric Field in medium 2 (E_2), considering different sigma values

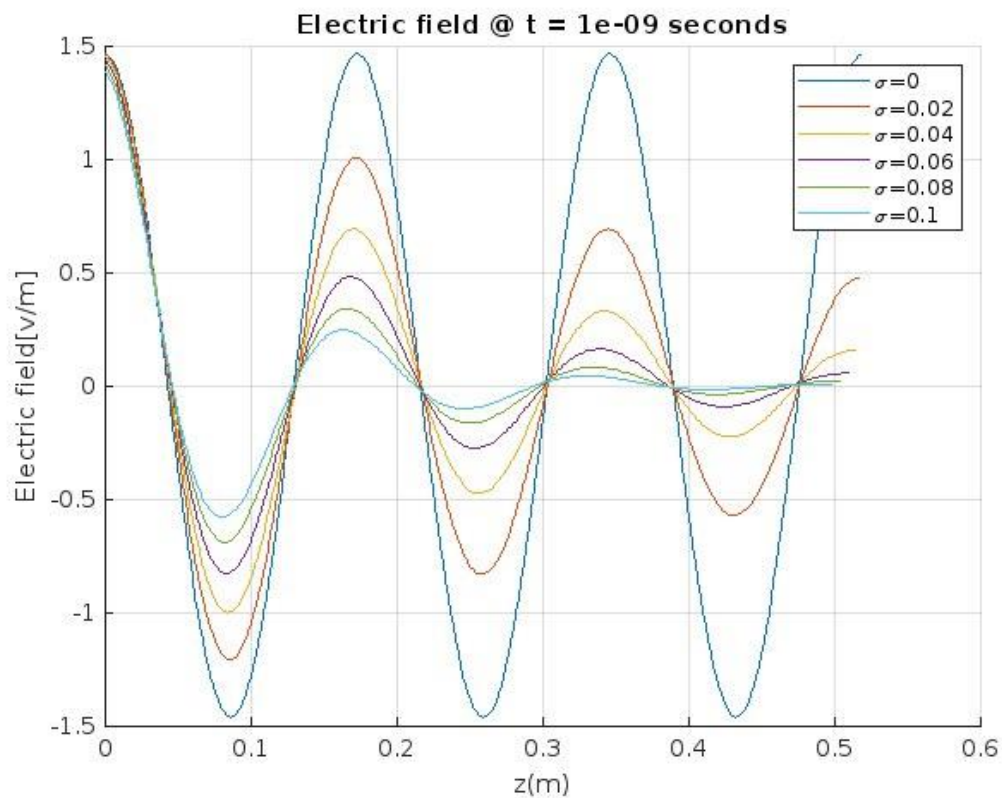
```
f = 1*10^9;
w = 2*pi*f;
T = 1/f;
c = 3 * 10^8;
t = T;
lambda = c/f;
E0 = 2;
er1 = 1;
ur1 = 1;
er2 = 3;
ur2 = 1;
e0 = 8.85*10^-12;
u0 = pi*4*10^-7;
e1 = e0*er1;
e2 = e0*er2;
u1 = u0*ur1;
u2 = u0 *ur2;
sigma2 = 0:0.1/5:0.1;
etr = zeros (length(sigma2),length(z2));
%k1 = w*sqrt(e1*u1);
n1 = sqrt(u1/e1);
figure;
hold on;
for s=1:length(sigma2)
    k2 = w*sqrt((e2-1i*sigma2(s)/w)*u2);
    alpha2 = -imag(k2);
```

```

beta2 = real(k2);
n2 = sqrt(1i*w*u2/(sigma2(s)+1i*w*e2));
lambda2 = 2*pi/beta2;
z2 = 0 : lambda2/100 : 3*lambda2;
%transmission coefficient%
tr = 2*n2/(n1+n2);
Et = E0*tr*exp(-1i*k2*z2);
etr = real(Et*exp(1i*w*t));
%plot(z2,etr,'Display name',['\sigma =']num2str(sigma2(s)));
plot(z2,etr);

end
grid on;
xlabel("z(m)");
ylabel("Electric field[v/m]");
title("Electric field @ t = 1e-09 seconds");
grid on;
legend('\sigma=0','\sigma=0.02','\sigma=0.04','\sigma=0.06','\sigma=0.08','\sigma=0.1')

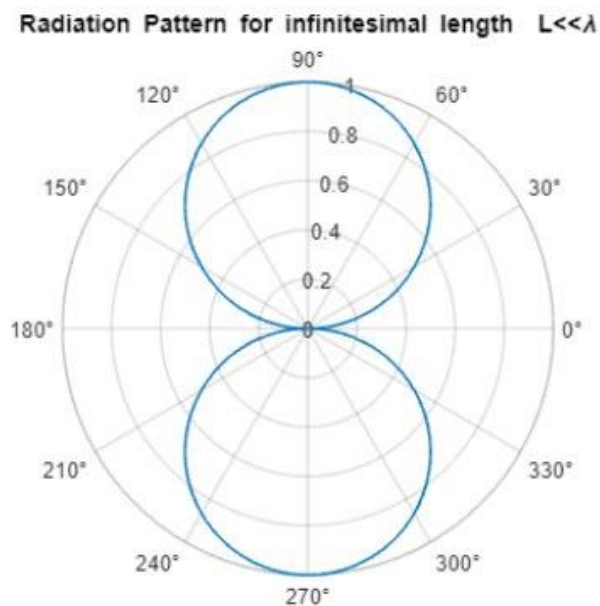
```



Antenna Lab

1. Radiation pattern for $L \ll \lambda$ for $0 < \theta < 2\pi$;

```
n=120*pi;
Io=1;
z=1;
r=10;
lambda=0.3;
k=(2*pi)/lambda;
L=lambda;
theta=0:0.01:2*pi;
%theta=pi/2;
E=1i*n*Io*z*exp(-1i*k*z)*sin(theta)*(1/(2*lambda*r));
F=sin(theta);
H=1i*Io*z*exp(-1i*k*r)*sin(theta)*(1/(2*lambda*r));
polarplot(theta, abs(F))
%plot(theta,abs(F));
%polarplot(theta, abs(H))
title('Radiation Pattern for infinitesimal length  $L \ll \lambda$ ');
```



2. Radiation pattern for $L \ll \lambda$ for $0 < \phi < 2\pi$;

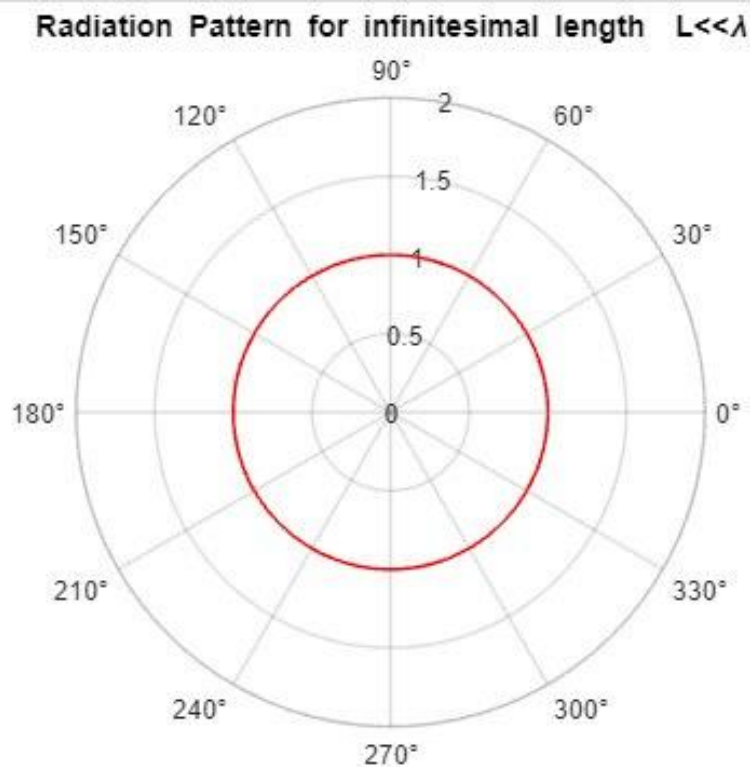
```
n = 120*pi;
Io = 1;
z=1;
r = 10;
lambda = 0.3;
%theta=0:pi/50:2*pi;
theta=pi/2;
phi=0:0.01:2*pi;
phi1=pi;
```

```

theta1=0:0.01:2*pi;
k = (2*pi) / lambda;
%L = lambda / 2;
E=1i*n*Io*z*exp(-1i*k*z)*sin(theta)*(1/(2*lambda*r))*ones(length(phi));
F=sin(theta)*ones(length(phi));
H=1i*Io*z*exp(-1i*k*r)*sin(theta)*(1/(2*lambda*r));

%polarplot(theta, E)
%polarplot(phi, abs(F),'red')
polarplot(theta1, abs(F),'red')
title('Radiation Pattern for infinitesimal length  $L \ll \lambda$ ');

```



3. Radiation pattern for $L=\lambda/2$ for $0 < \theta < 2\pi$;

```

% Define parameters
Io = 1; % Adjust the as needed
r = 10; % Adjust the as needed
theta = 0:0.1:2*pi;
lambda = 2; % Adjust the as needed
k = 2 * pi / lambda;
E_theta = 1i*n*Io*exp(-1i*k*r)*(1/(2*pi*r))*cos((pi/2)*cos(theta))./(sin(theta));
F_theta = cos((pi/2) * cos(theta)) ./ (sin(theta));

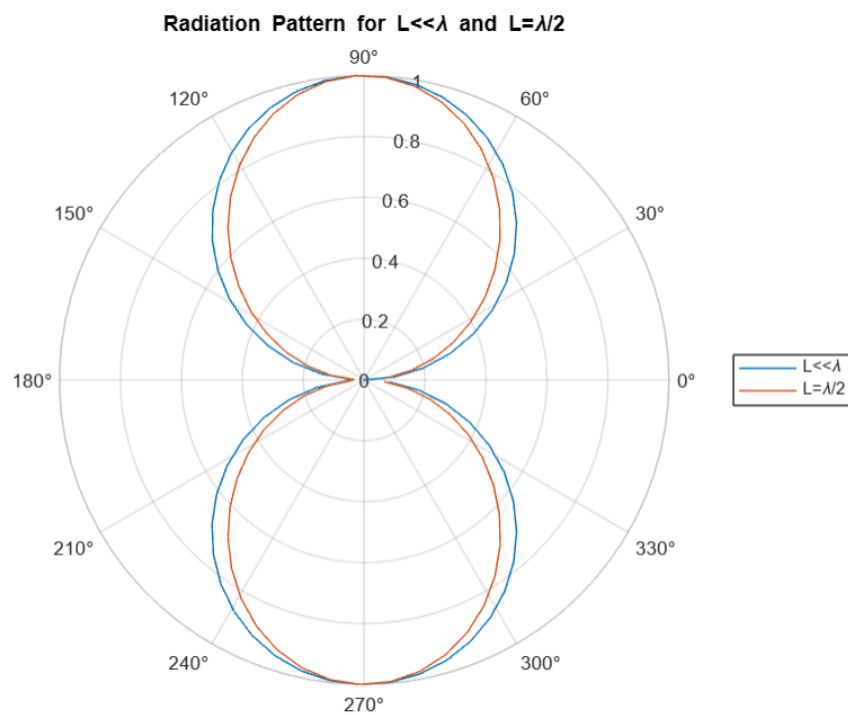
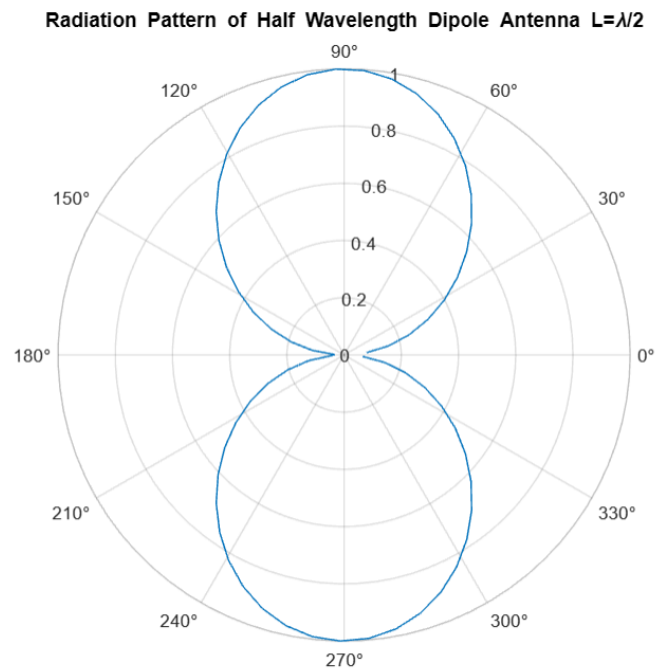
figure;

```

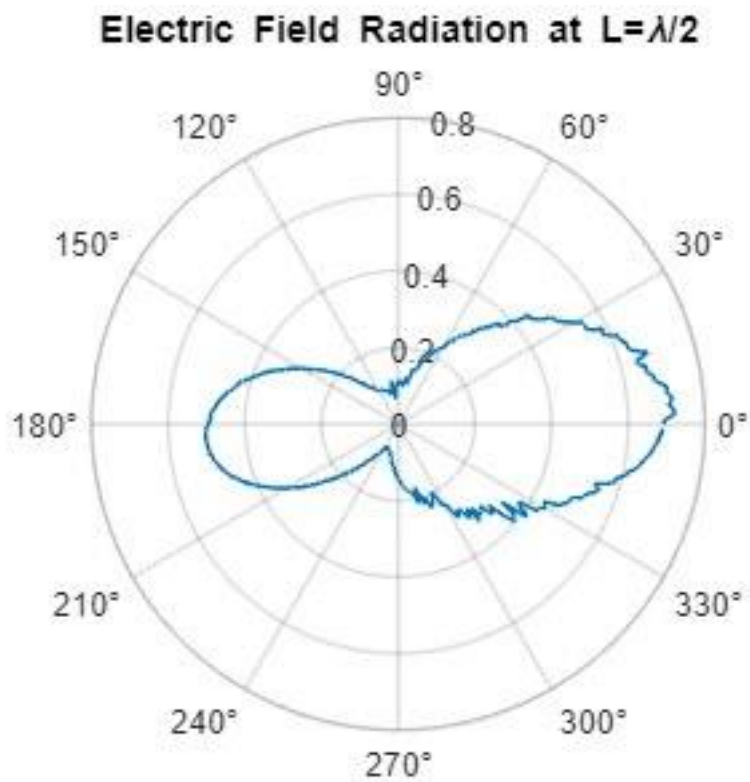
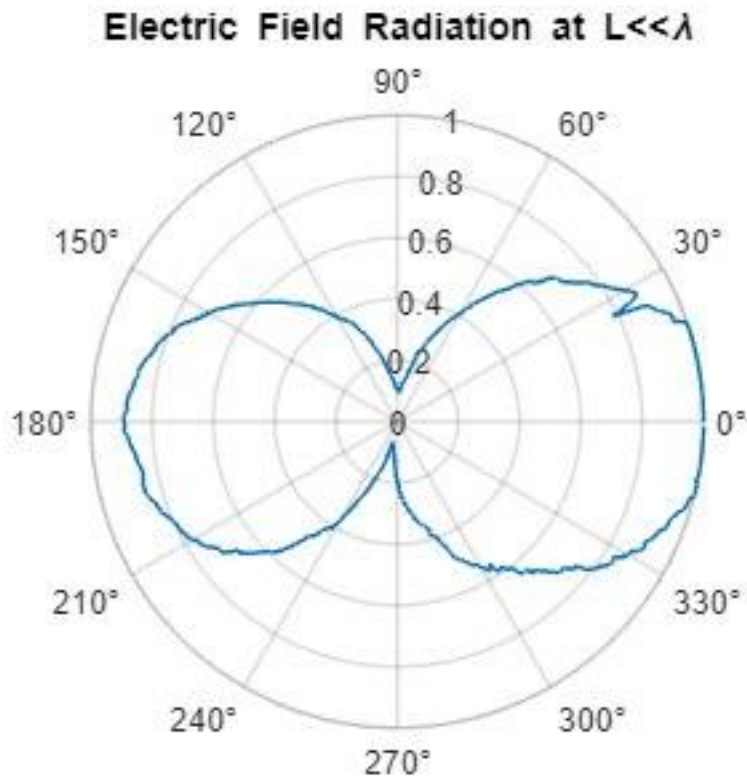
```

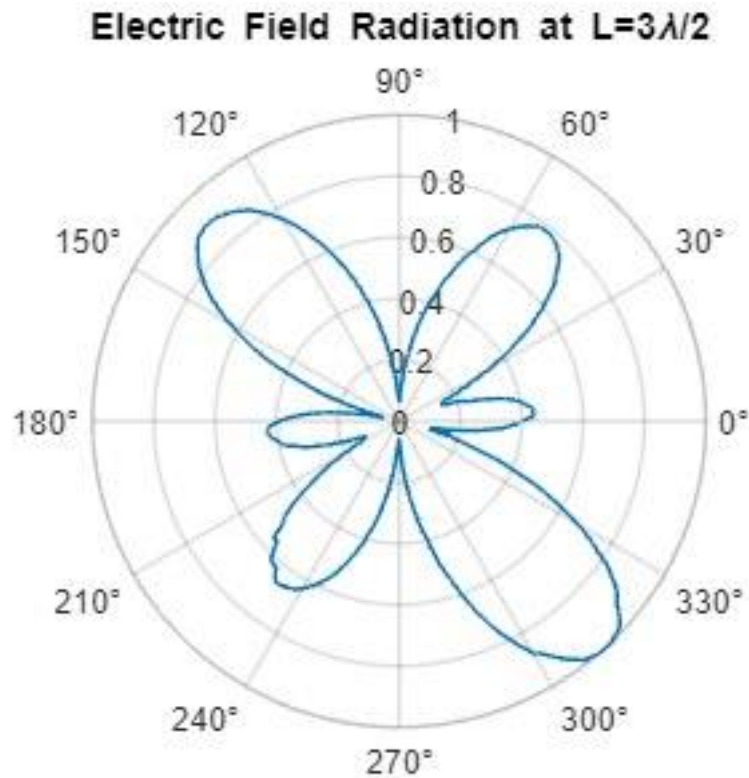
%polarplot(theta, abs(E_theta));
polarplot(theta, abs(F_theta));
title('Radiation Pattern of Half Wavelength Dipole Antenna  $L=\lambda/2$ ');

```



From the practical lab ,we realized the radiation pattern of the three different cases(when $L \ll \lambda$, $L = \lambda/2$ and $L = 3\lambda/2$).





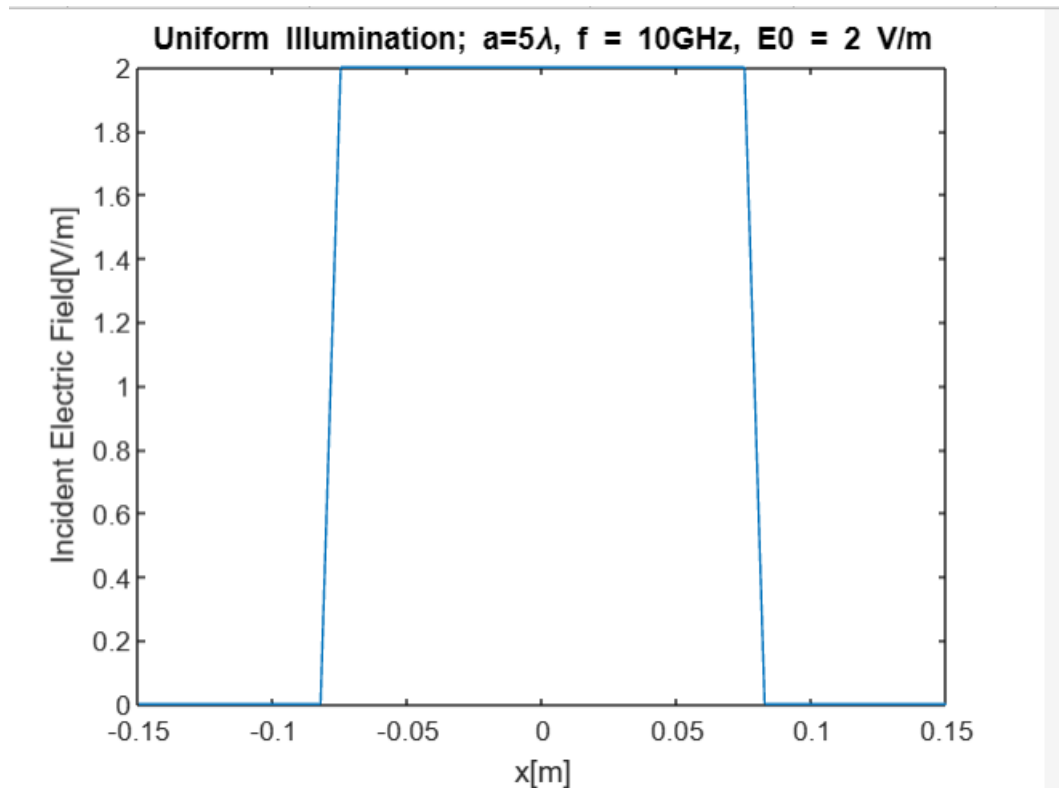
Aperture Antenna Lab

1. Implement the expression of the Incident Electric Field of an aperture antenna, with Uniform illumination:

```
E0=2;
z=0;
F=10*10^9;
c=3*10^8;
lambda=c/F;
a=5*lambda;
x1 = -a: a/20:-a/2-a/20;
x2 = -a/2: a/20:a/2;
x3 = a/2+a/20: a/20:a;
k= (2*pi)/lambda;
Ei = E0*exp(-1i*k*z);
E_inc =[zeros(1, length(x1)) ones(1, length(x2))*Ei zeros(1, length(x3))];

plot([x1 x2 x3], E_inc);

xlabel("x[m]");
ylabel("Incident Electric Field[V/m]");
%legend("uniform","Trigular","Cosine")
title('Uniform Illumination; a=5\lambda, f = 10GHz, E0 = 2 V/m')
```



2. Implement the expression of the Radiated Field of an aperture antenna with uniform Illumination:

```

E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/180 : pi/2;
Ei = a*E0*exp(-1i*k*z)*sinc(k*a/2*(sin(theta))/pi);
plot(theta, abs(Ei));

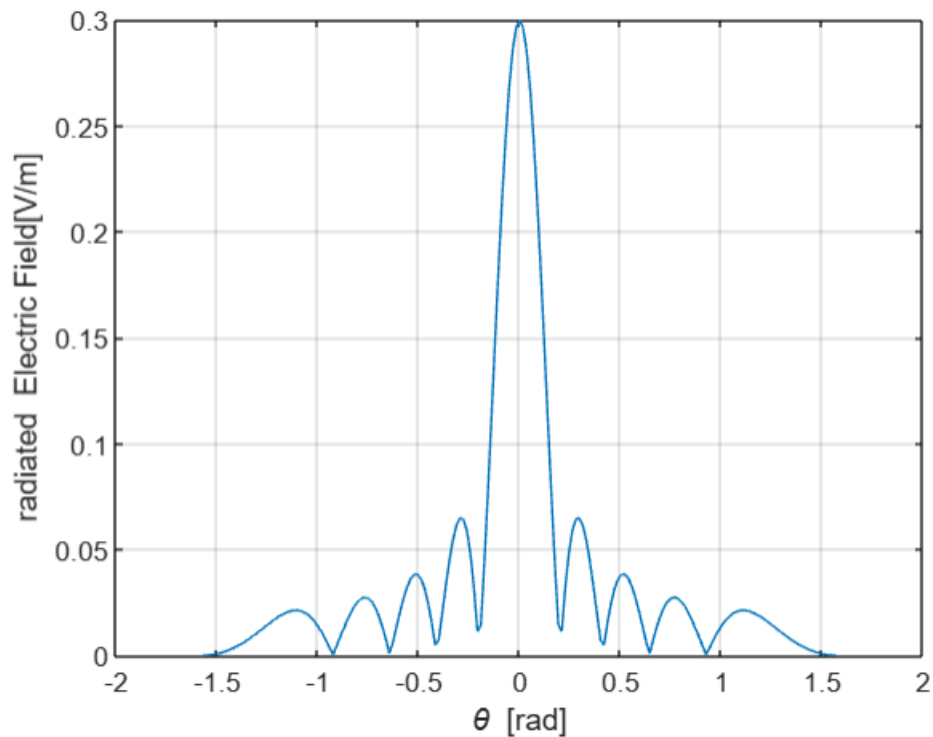
```

grid on;

```

xlabel("\theta [rad]");
ylabel("radiated Electric Field[V/m]");

```



3. Implement the expression of the Radiated Field in dB of an aperture antenna with uniform illumination:

```

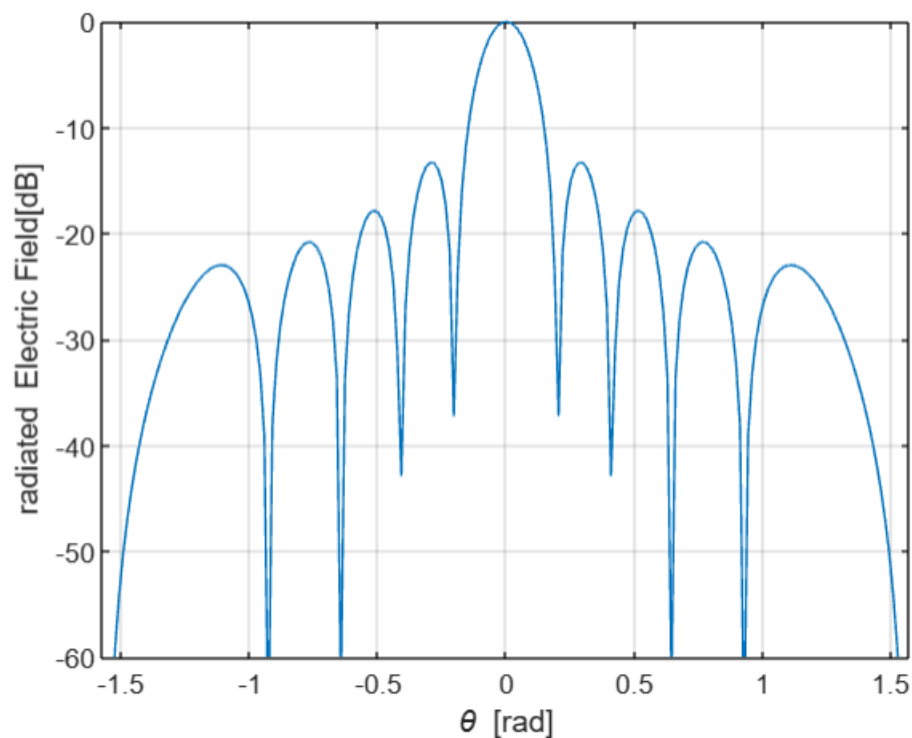
Eo=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/200 : pi/2;
Ei = a*Eo*exp(-1i*k*z)*sinc(k*a/2*(sin(theta))/pi);

Ei_dB = 20*log10(abs(Ei)/max(abs(Ei)));
plot(theta,Ei_dB);
axis([-pi/2, pi/2, -60, 0]);

grid on;

xlabel("\theta [rad]");
ylabel("radiated Electric Field[dB]");

```



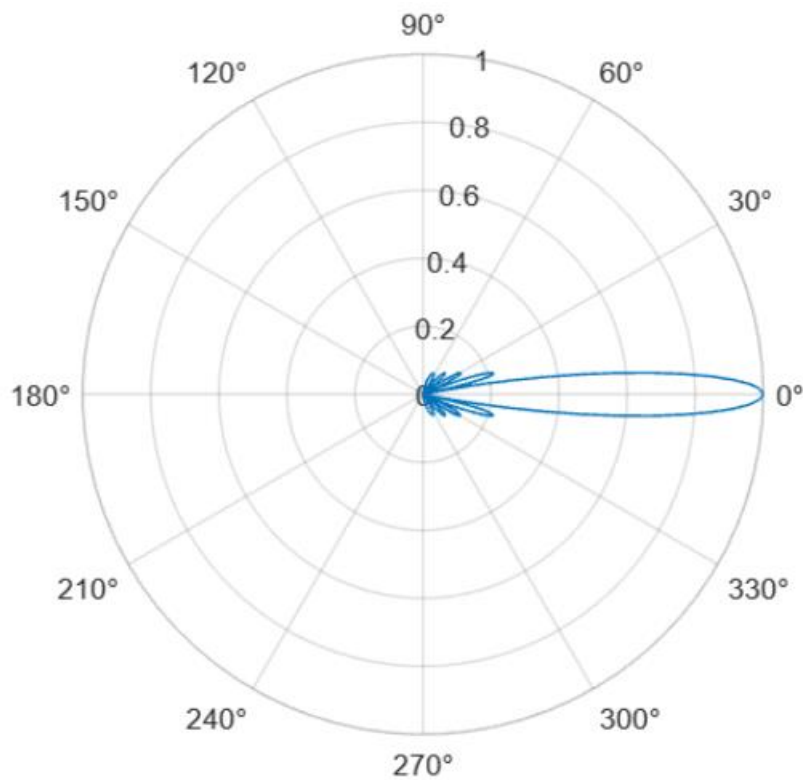
4. Implement the expression of the Radiation pattern of an aperture antenna with uniform Illumination

```

E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2:pi/200 : pi/2;

Ei = a*E0*exp(-1i*k*z)*sinc(k*a/2*(sin(theta))/pi);
Ei_dB = 20*log10(abs(Ei)/max(abs(Ei)));
%F_theta = ((a/2)*E0*exp(-
1i*k*z))*(sinc((pi/2)+(k*a/2)*(sin(theta))/pi)+sinc((pi/2)-
(k*a/2)*(sin(theta))/pi));
F_theta=sinc(((k*a/2)*sin(theta))/pi);
%plot(theta,Ei_dB);
%axis([-pi/2, pi/2, -60, 0]);
polarplot(theta, abs(F_theta));
grid on;

```



5. Implement the expression of the Incident Electric Field of an aperture antenna, with Triangular illumination

```

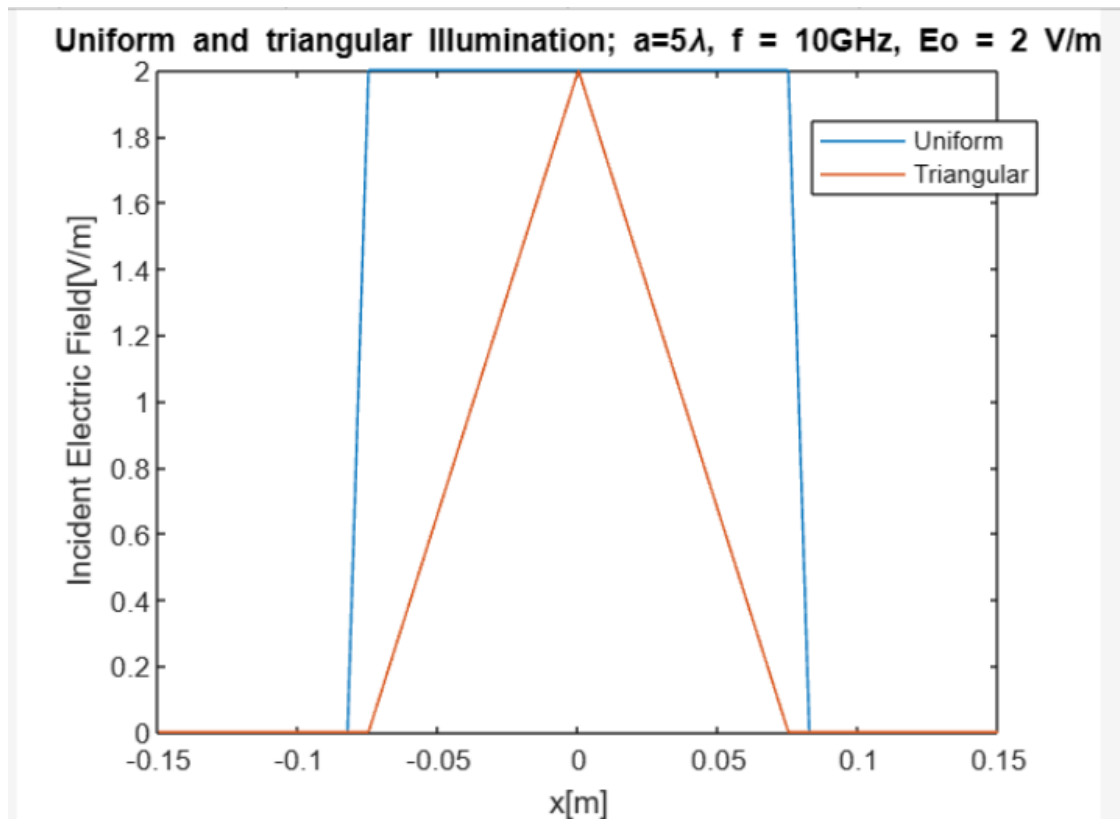
E0=2;
z=0;
F=10*10^9;
c=3*10^8;
lambda=c/F;
a=5*lambda;
x1 = -a: a/20:-a/2-a/20;
x2 = -a/2: a/20:a/2;
x3 = a/2+a/20: a/20:a;
k= (2*pi)/lambda;
Ei = E0*exp(-1i*k*z);
Ei_T = (1-abs(x2)/(a/2))*E0*exp(-1i*k*z);

E_inc =[zeros(1,length(x1)) ones(1,length(x2)).*Ei zeros(1, length(x3))];
E_inc_T =[zeros(1,length(x1)) ones(1,length(x2)).*Ei_T zeros(1, length(x3))];

plot([x1 x2 x3], abs(E_inc));
hold on;
plot([x1 x2 x3], abs(E_inc_T));

xlabel("x[m]");
ylabel("Incident Electric Field[V/m]");
title('Uniform and triangular Illumination; a=5\lambda, f = 10GHz, Eo = 2 V/m')
legend("Uniform","Triangular");

```



6. Implement the expression of the Radiated Field of an aperture antenna with Triangular Illumination.

```

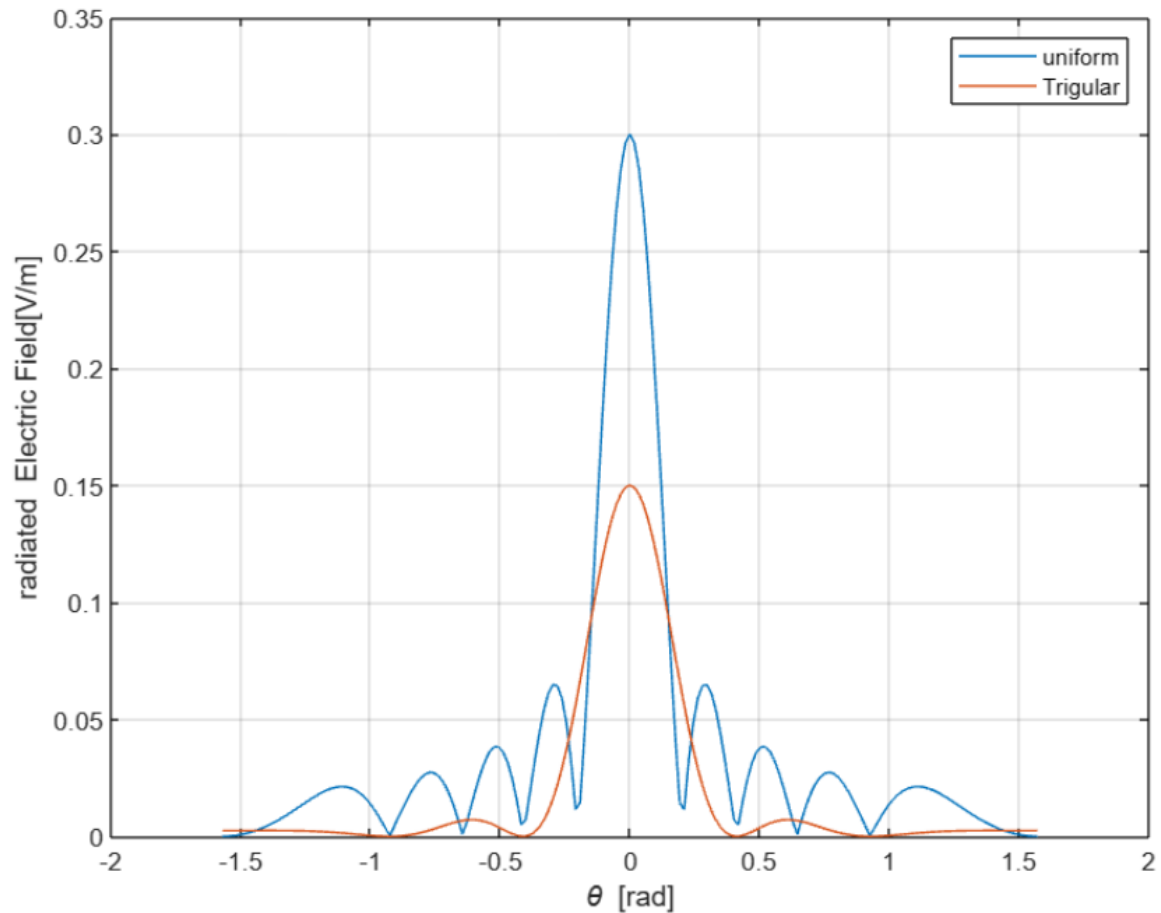
E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/180 : pi/2;

Ei = a*E0*exp(-1i*k*r)*sinc(k*a/2*(sin(theta))/pi);
Ei_T = (a/2)*E0*exp(-1i*k*r)*(sinc(k*a/4*(sin(theta))/pi)).^2;
%Ei_C = (a/2)*E0*exp(-
1i*k*r)*((sinc(((pi/2)+(k*a/2)*(sin(theta))/pi)))+(sinc(((pi/2)-
(k*a/2)*(sin(theta))/pi))));

plot(theta, abs(Ei));
hold on;
plot(theta, abs(Ei_T));
%hold on;
%plot(theta, abs(Ei_C));
grid on;

xlabel("\theta [rad]");
ylabel("radiated Electric Field[V/m]");
legend("uniform","Trigular",'cosine')

```



7. Implement the expression of the Radiated Field in dB of an aperture antenna with Triangular Illumination.

```

E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/200 : pi/2;

Ei = a*E0*exp(-1i*k*z)*sinc(k*a/2*(sin(theta))/pi);
Ei_T = (a/2)*E0*exp(-1i*k*z)*(sinc(k*a/4*(sin(theta))/pi)).^2;
Ei_T_dB = 20*log10(abs(Ei_T)/max(abs(Ei_T)));
Ei_dB = 20*log10(abs(Ei)/max(abs(Ei)));
F_theta = sinc(k*a/2*(sin(theta))/pi);

plot(theta,Ei_dB);
hold on
plot(theta,Ei_T_dB);

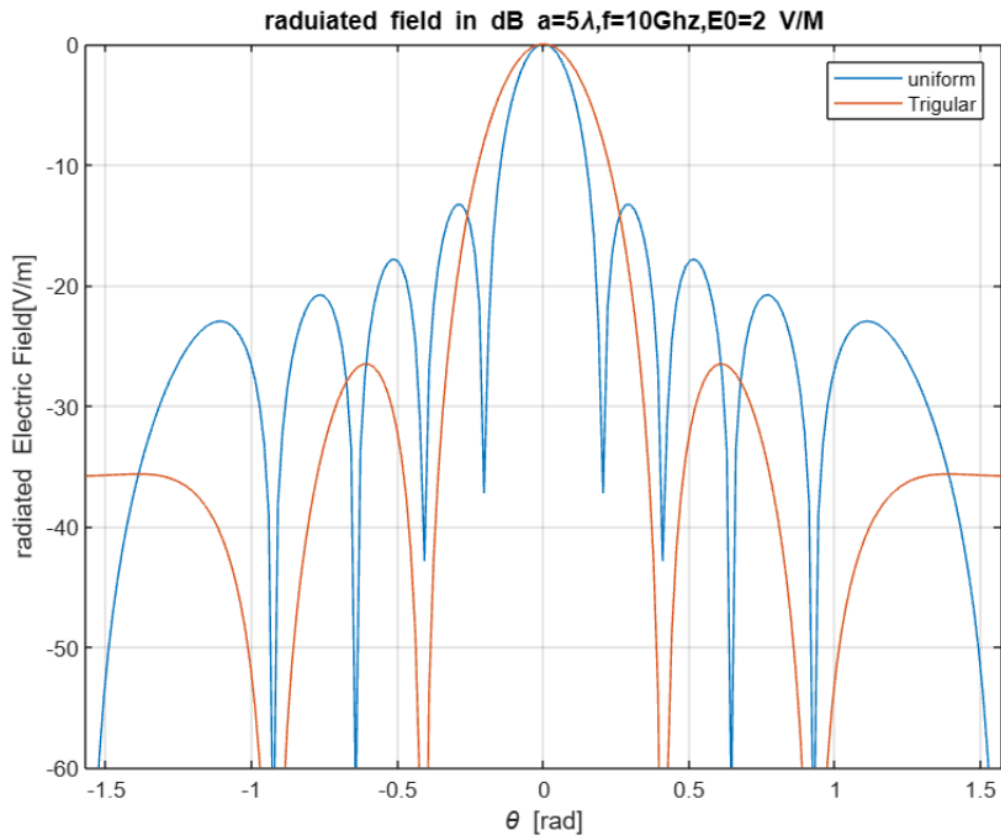
axis([-pi/2, pi/2, -60, 0]);
%polarplot(theta, F_theta);
grid on;
xlabel("\theta [rad]");

```

```

ylabel("radiated Electric Field[V/m]");
legend("uniform","Trigular")
title("radiuated field in dB a=5\lambda,f=10Ghz,E0=2 V/M")

```

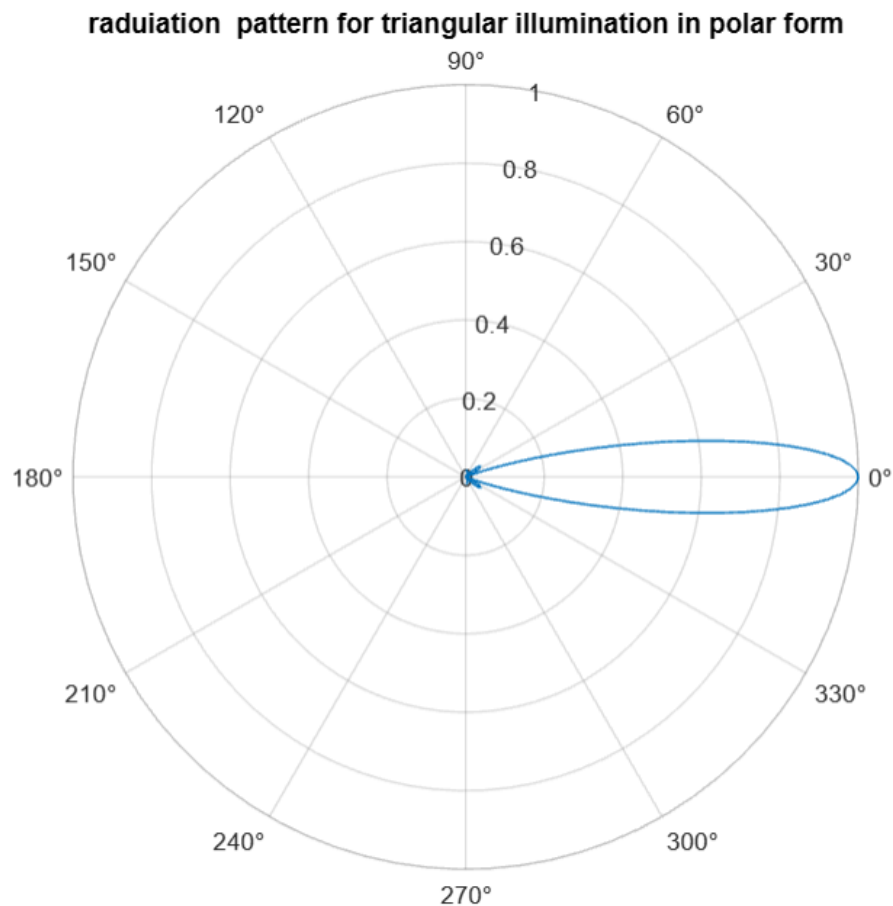


8.Implement the expression of the Radiation pattern of an aperture antenna with Triangular Illumination

```

E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/200 : pi/2;
F_theta = (sinc(k*a/4*(sin(theta))/pi)).^2;
polarplot(theta,F_theta);
title("raduiation pattern for triangular illumination in polar form")

```

9. Implement the expression of the Incident Electric Field of an aperture antenna, with Cosine illumination

```

Eo=2;
z=0;
F=10*10^9;
c=3*10^8;
lambda=c/F;
a=5*lambda;
x1 = -a: a/20:-a/2-a/20;
x2 = -a/2: a/20:a/2;
x3 = a/2+a/20: a/20:a;
k= (2*pi)/lambda;
Ei = Eo*exp(-1i*k*z);
Ei_T = (1-abs(x2)/(a/2))*Eo*exp(-1i*k*z);
Ei_C = cos(pi*x2/a)*Eo*exp(-1i*k*z);

E_inc =[zeros(1,length(x1)) ones(1,length(x2)).*Ei zeros(1, length(x3))];
E_inc_T =[zeros(1,length(x1)) ones(1,length(x2)).*Ei_T zeros(1, length(x3))];
E_inc_C =[zeros(1,length(x1)) ones(1,length(x2)).*Ei_C zeros(1, length(x3))];

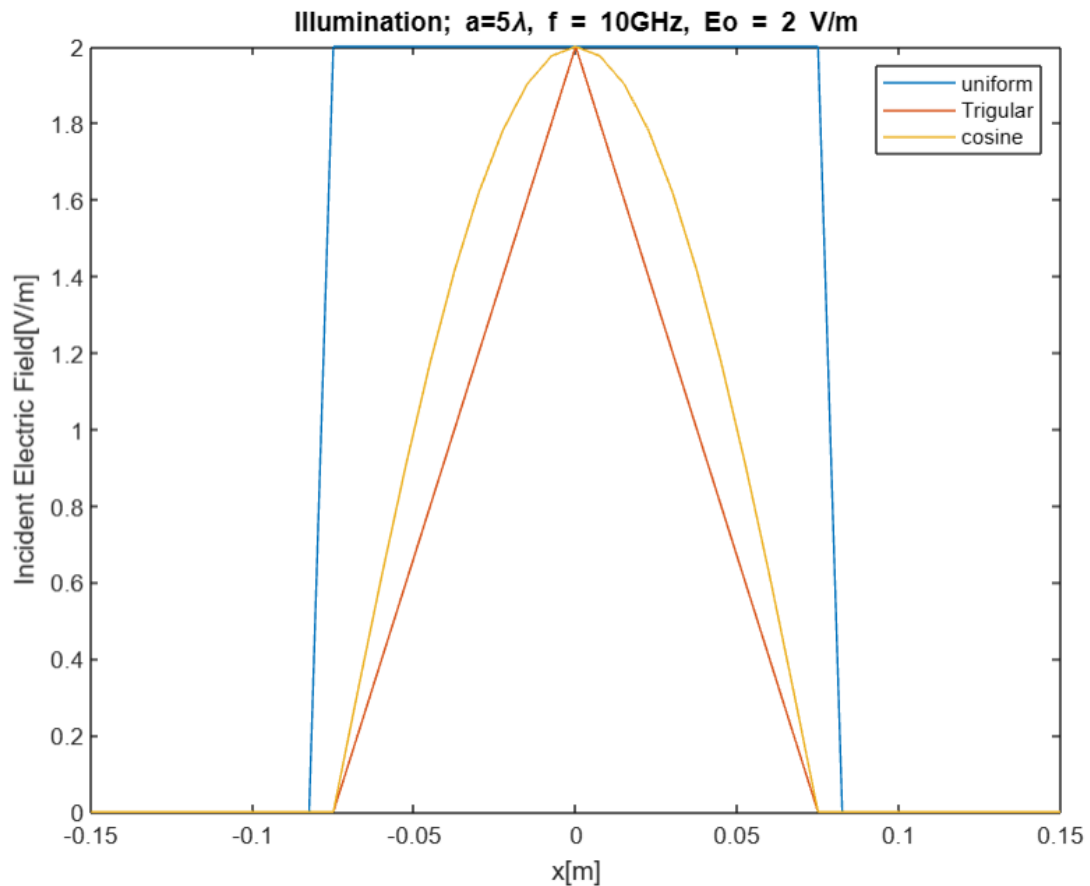
plot([x1 x2 x3], abs(E_inc));
hold on;
plot([x1 x2 x3], abs(E_inc_T));
hold on;
plot([x1 x2 x3], abs(E_inc_C));

```

```

xlabel("x[m]");
ylabel("Incident Electric Field[V/m]");
legend("uniform","Trigular","cosine")
title("Illumination; a=5\lambda, f = 10GHz, Eo = 2 V/m")

```



10. Implement the expression of the Radiated Field of an aperture antenna with Cosine Illumination.

```
% Parameters
```

```

E0 = 2;
z = 0;
F = 10 * 10^9;
c = 3 * 10^8;
r = 100;
lambda = c / F;
a = 5 * lambda;
k = (2 * pi) / lambda;

```

```
% Define theta values
```

```
theta = -pi/2 : pi/180 : pi/2;
```

```
% Calculate the radiated electric field for different distributions
```

```

E_uniform = a * E0 * exp(-1i * k * r) * sinc(k * a / 2 * sin(theta) / pi);
E_triangular = (a / 2) * E0 * exp(-1i * k * r) * (sinc(k * a / 4 * sin(theta) / pi)).^2;
x=sinc(((pi/2)+k*(a/2)*sin(theta))/pi);
y=sinc(((pi/2)-k*(a/2)*sin(theta))/pi);
%E_cosine = (a / 2) * E0 * exp(-1i * k * r) * ((sinc((pi/2) + (k * a / 2) * sin(theta)) / pi) + (sinc((pi/2) - (k * a / 2) * sin(theta)) / pi));

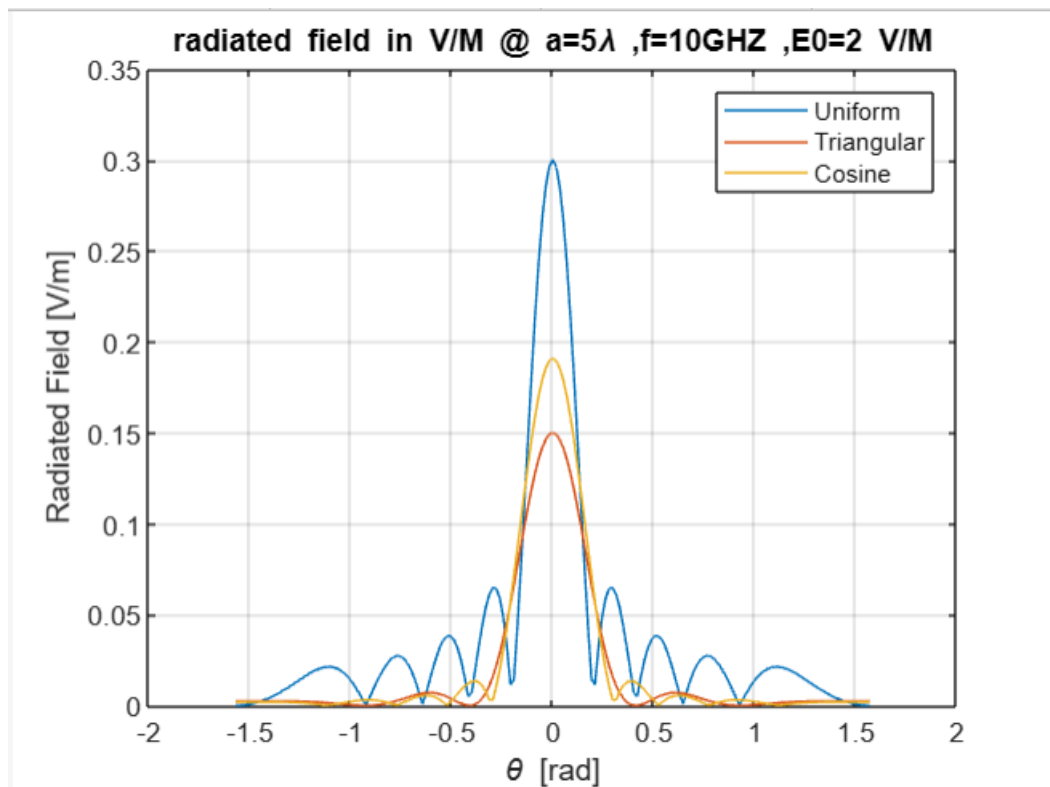
```

```

E_cosine = (a / 2) * E0 * exp(-1i * k * r)*(x+y);
% Plot the radiated electric field for different distributions
figure;
plot(theta, abs(E_uniform));
hold on;
plot(theta, abs(E_triangular));
hold on;
plot(theta, abs(E_cosine));

grid on;
xlabel('\theta [rad]');
ylabel('Radiated Field [V/m]');
title('radiated field in V/M @ a=5\lambda ,f=10GHZ ,E0=2 V/M');
legend('Uniform', 'Triangular', 'Cosine');

```



11. Implement the expression of the Radiated Field in dB of an aperture antenna with cosine Illumination.

```

% Parameters
E0 = 2;
z = 0;
F = 10 * 10^9;
c = 3 * 10^8;
r = 100;
lambda = c / F;
a = 5 * lambda;
k = (2 * pi) / lambda;

% Define theta values

```

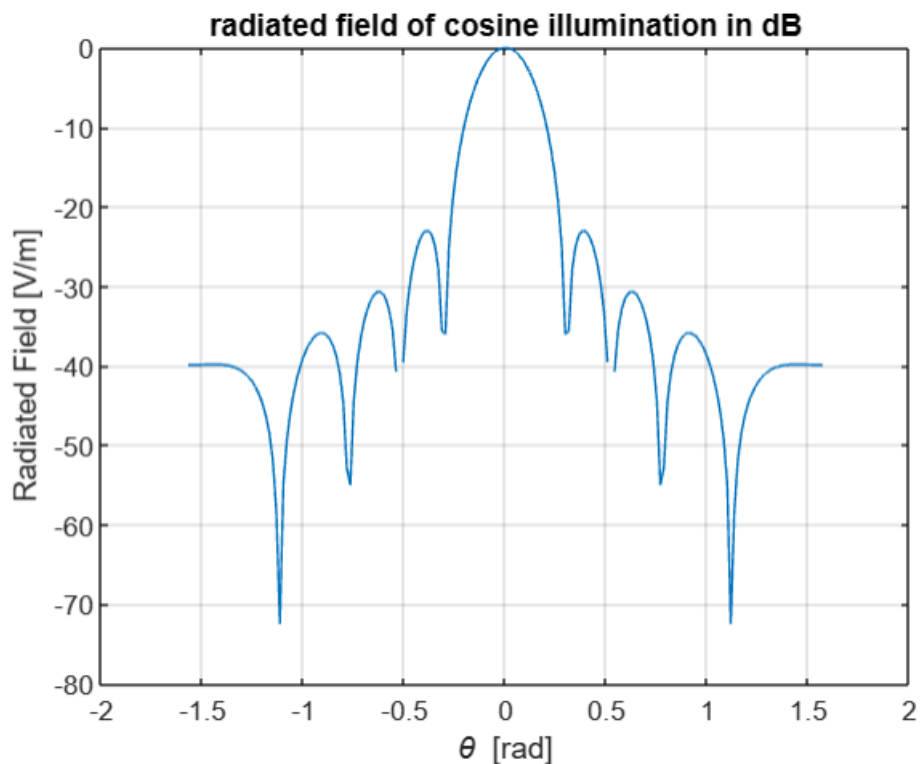
```

theta = -pi/2 : pi/180 : pi/2;

% Calculate the radiated electric field for different distributions
E_uniform = a * E0 * exp(-1i * k * r) * sinc(k * a / 2 * sin(theta) / pi);
E_triangular = (a / 2) * E0 * exp(-1i * k * r) * (sinc(k * a / 4 * sin(theta) / pi)).^2;
x=sinc(((pi/2)+k*(a/2)*sin(theta))/pi);
y=sinc(((pi/2)-k*(a/2)*sin(theta))/pi);
%E_cosine = (a / 2) * E0 * exp(-1i * k * r) * ((sinc((pi/2) + (k * a / 2) * sin(theta)) / pi) + (sinc((pi/2) - (k * a / 2) * sin(theta)) / pi));
E_cosine = (a / 2) * E0 * exp(-1i * k * r)*(x+y);
E_dB = 20*log10(abs(E_cosine)/max(abs(E_cosine)));
% Plot the radiated electric field for different distributions
figure;
axis([-pi/2, pi/2, -60, 0]);
plot(theta, (E_dB));

grid on;
xlabel('\theta [rad]');
ylabel('Radiated Field [V/m]');
title('radiated field of cosine illumination in dB');
%legend('Uniform', 'Triangular', 'Cosine');

```



12. Implement the expression of the Radiated Field in dB of an aperture antenna with uniform, triangular and cosine illumination.

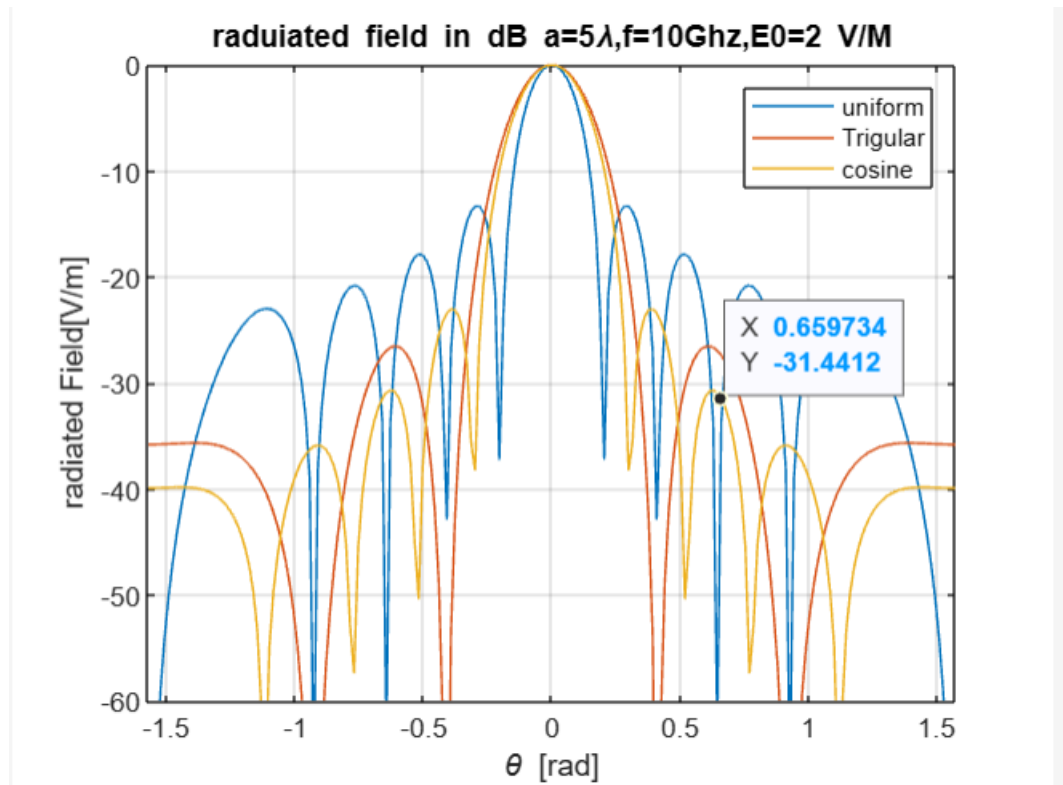
```
E0=2;
z=0;
F=10*10^9;
c=3*10^8;
r= 100;
lambda=c/F;
a=5*lambda;
k= (2*pi)/lambda;
theta=-pi/2: pi/200 : pi/2;

Ei = a*E0*exp(-1i*k*z)*sinc(k*a/2*(sin(theta))/pi);
Ei_T = (a/2)*E0*exp(-1i*k*z)*(sinc(k*a/4*(sin(theta))/pi)).^2;
Ei_T_dB = 20*log10(abs(Ei_T)/max(abs(Ei_T)));
Ei_dB = 20*log10(abs(Ei)/max(abs(Ei)));
F_theta = sinc(k*a/2*(sin(theta))/pi);

x=sinc(((pi/2)+k*(a/2)*sin(theta))/pi);
y=sinc(((pi/2)-k*(a/2)*sin(theta))/pi);
%E_cosine = (a / 2) * E0 * exp(-1i * k * r) * ((sinc((pi/2) + (k * a / 2) *
sin(theta)) / pi) + (sinc((pi/2) - (k * a / 2) * sin(theta)) / pi));
E_cosine = (a / 2) * E0 * exp(-1i * k * r)*(x+y);
E_dB = 20*log10(abs(E_cosine)/max(abs(E_cosine)));
% Plot the radiated electric field for different distributions
figure;

plot(theta,Ei_dB);
hold on
plot(theta,Ei_T_dB);
hold on
plot(theta, (E_dB));

axis([-pi/2, pi/2, -60, 0]);
%polarplot(theta, F_theta);
grid on;
xlabel("\theta [rad]");
ylabel("radiated Field[V/m]");
legend("uniform","Trigular","cosine")
title("radiated field in dB a=5\lambda,f=10Ghz,E0=2 V/M")
```



13. Implement the expression of the Radiation pattern of an aperture antenna with Cosine Illumination

```

E0 = 2;
z = 0;
F = 10 * 10^9;
c = 3 * 10^8;
r = 100;
lambda = c / F;
a = 5 * lambda;
k = (2 * pi) / lambda;

% Define theta values
theta = -pi/2 : pi/200 : pi/2;

%E_cosine = (a / 2) * E0 * exp(-1i * k * r) * ((sinc((pi/2) + (k * a / 2) *
sin(theta)) / pi) + (sinc((pi/2) - (k * a / 2) * sin(theta)) / pi));
F_theta = sinc(((pi/2) + k*(a/2)*sin(theta)) / pi) + sinc(((pi/2) -
k*(a/2)*sin(theta)) / pi);
F_theta_normalized = F_theta / max(abs(F_theta));

figure;
polarplot(theta, abs(F_theta_normalized));
title('Radiated Field of Cosine Illumination in Polar Form');

```

Radiated Field of Cosine Illumination in Polar Form

