

## Exercise Sheet 3

Due Date: December 12, 8 pm

### Note on Submission

All solutions have to be uploaded together as a single zip file to LernraumPlus. Solve the exercises by implementing the functions in the file `exercise_sheet3.py`.

In this exercise sheet, you will create your own maximum entropy model by implementing the methods of the class `MaxEntModel` in the file `exercise_sheet3.py`. We use features of the following form (we already used them in the example discussed in the lecture):

$$f_{w/t}(x_i, y_i) = \begin{cases} 1 & \text{iff } x_i = w \quad \wedge \quad y_i = t \\ 0 & \text{otherwise} \end{cases}$$
$$f_{t_1/t_2}(x_i, y_i) = \begin{cases} 1 & \text{iff } y_{i-1} = t_1 \quad \wedge \quad y_i = t_2 \\ 0 & \text{otherwise,} \end{cases}$$

where  $w$  is a word,  $t$ ,  $t_1$ ,  $t_2$  are labels,  $x_i$  is the word of a sentence at position  $i$ ,  $y_i$  is a label we assigned to this word and  $y_{i-1}$  is the label of the word at position  $i-1$ . That is,  $f_{w/t}(x_i, y_i)$  is 1 if and only if the  $i$ -th word of a given sentence is  $w$  and if we assign the label  $t$  to this word. Similarly,  $f_{t_1/t_2}(x_i, y_i)$  is 1 if and only if the label of the  $(i-1)$ -word of a given sentence is  $t_1$  and if we assign the label  $t_2$  to the  $i$ -th word.

Use the provided corpus `corpus_pos.txt` for training your model. You can use the Python function `import_corpus` for importing this corpus.

### Exercise 1 - Building the Feature Set [3+2 points]

First of all, you need to build the set  $\mathcal{F}$  of all features. Therefore, do the following things:

- a) Build the set  $\mathcal{X}$  of all words and the set  $\mathcal{Y}$  of all labels occurring in the corpus. Use the variable `labels` to save the set of all labels. Then build the set of all features

$$\mathcal{F} = \{f_{w/t} | w \in \mathcal{X}, t \in \mathcal{Y}\} \cup \{f_{t_1/t_2} | t_1, t_2 \in \mathcal{Y}\}.$$

You can use pairs of strings to represent the features  $f_{w/t}$  and  $f_{t_1/t_2}$ . Note that there is no previous word for the first word of a sentence. In this case, the label of the previous word is `start`.

For example, assume we are given the "sentence" ( (the, DT), (dog, NN) ) and we decided to represent features as pairs of strings, then we would build the following sets:

$$\begin{aligned}\mathcal{X} &= \{\text{the}, \text{dog}\} \\ \mathcal{Y} &= \{\text{start}, \text{DT}, \text{NN}\} \\ \mathcal{F} &= \left\{ \begin{array}{l} (\text{the}, \text{start}), (\text{the}, \text{DT}), (\text{the}, \text{NN}), \\ (\text{dog}, \text{start}), (\text{dog}, \text{DT}), (\text{dog}, \text{NN}), \\ (\text{start}, \text{start}), (\text{start}, \text{DT}), (\text{start}, \text{NN}), \\ (\text{DT}, \text{start}), (\text{DT}, \text{DT}), (\text{DT}, \text{NN}), \\ (\text{NN}, \text{start}), (\text{NN}, \text{DT}), (\text{NN}, \text{NN}) \end{array} \right\}\end{aligned}$$

Then, assign each feature to a unique index  $i \in \{1, \dots, |\mathcal{F}|\}$ . Then the feature assigned to index  $i$  can be referenced by  $f_i$ . Finally, initialize the vector  $\theta$  of parameters. Do all this inside the method `initialize`.

- b) Implement the method `get_active_features` which returns a vector  $\vec{f} \in \{0, 1\}^{|\mathcal{F}|}$  indicating which features are active for a given word  $x_j$ . I.e., for a given word  $x_j$  and a label  $y_j$  for this word, the  $i$ -th element of this vector is set to 1 if and only if  $f_i(x_j, y_j) = 1$  and 0 otherwise.

Hint: Use a Python dictionary to store the features and their indices.

### Exercise 2 – Computing Conditional Probabilities [2+2 points]

- a) Implement the method `cond_normalization_factor`, which returns the normalization factor  $1/Z(x_i)$ , where

$$Z(x_i) = \sum_{y' \in \mathcal{Y}} e^{\vec{\theta} \cdot \vec{f}(x_i, y')}.$$

Note that the label  $y_{i-1}$  of the previous word is implicitly given by the index  $i$ , but you have to provide it explicitly in the code.

- b) Implement the method `conditional_probability`, which computes the conditional probability

$$P(y|x_i) = \frac{1}{Z(x_i)} e^{\vec{\theta} \cdot \vec{f}(x_i, y)}.$$

of a label  $y$  given the word  $x_i$ .

### Exercise 3 Empirical and Expected Feature Count [1 + 3 points]

Implement the method `empirical_feature_count`, which returns the vector  $E[\vec{f}(x_i, y_i)]$  of the empirical feature count, and the method `expected_feature_count`, which returns the vector  $E_{\vec{\theta}}[\vec{f}(x_i)]$  of the expected feature count, given the parameters  $\vec{\theta}$  of the current model.

### Exercise 4 Training the Model [2+3+2 points]

- a) Implement the method `parameter_update`, which performs one learning step according to

$$\vec{\theta}_{t+1} = \vec{\theta}_t + \alpha(E[\vec{f}(x_i, y_i)] - E_{\vec{\theta}}[\vec{f}(x_i)]),$$

where  $\alpha$  is a learning rate.

- b) Implement the method `train` for training your model via gradient descent. Use the method `parameter_update` you implemented above.
- c) Implement the method `predict`, which predicts the most probable label of a given word  $x_i$  at position  $i$  in a sentence.