Laboratory Session 05: May 4, 2020

Exercises due: May 20, 2020

Exercise 1

• A publishing company has recently launched a new journal. In order to determine how effective it is in reaching its possible audience, a market survey company selects a random sample of people from a possible target audience and interviews them. Out of 150 interviewed people, 29 have read the last issue of the journal.

- a) What kind of distribution would you assume for y, the number of people that have seen the last issue of the yournal?
- b) Assuming a uniform prior, what is the posterior distribution for y?
- c) Plot both posterior and likelihood ditributions functions

Exercise 2

- Three students want to construct their prior probability about the proportion of residents that support the building of a new concert hall in their small town.
- Anna thinks that her prior is a beta distribution with mean 0.2 and a standard deviation of 0.08.
- Benny moved only recently to this new town and therefore he does non have the slightest idea about it. Therefore he decides to use a uniform prior.
- Chris believes that his prior should have a trapezoidal shape

$$f(X) = \begin{cases} 20x & 0 \le 1 < 0.1\\ 2 & 0.1 \le 1 < 0.3\\ 5 - 10x & 0.3 < \le 0.5\\ 0 & x > 0.5 \end{cases}$$

- a) Draw and compare the three prior distributions.
- The next day the three students decide to interview a sample of 100 citizens of the small town, asking for their opinion. Out of the interviewed sample, 26 support the building of the new concert hall.
- b) Evaluate and draw the three prior distributions.
- c) Give an estimate of the most probable value and the 95% credibility interval.

Exercise 3

• A coin is flipped n = 30 times with the following outcomes:

- a) Assuming a flat prior, and a beta prior, plot the likelihood, prior and posterior distributions for the data set.
- b) Evaluate the most probable value for the coin probability p and, integrating the posterior probability distribution, give an estimate for a 95% credibility interval.
- c) Repeat the same analysis assuming a sequential analysis of the data. Show how the most probable value and the credibility interval change as a function of the number of coin tosses (i.e. from 1 to 30).
- d) Do you get a different result, by analyzing the data sequentially with respect to a one-step analysis (i.e. considering all the data as a whole)?

1