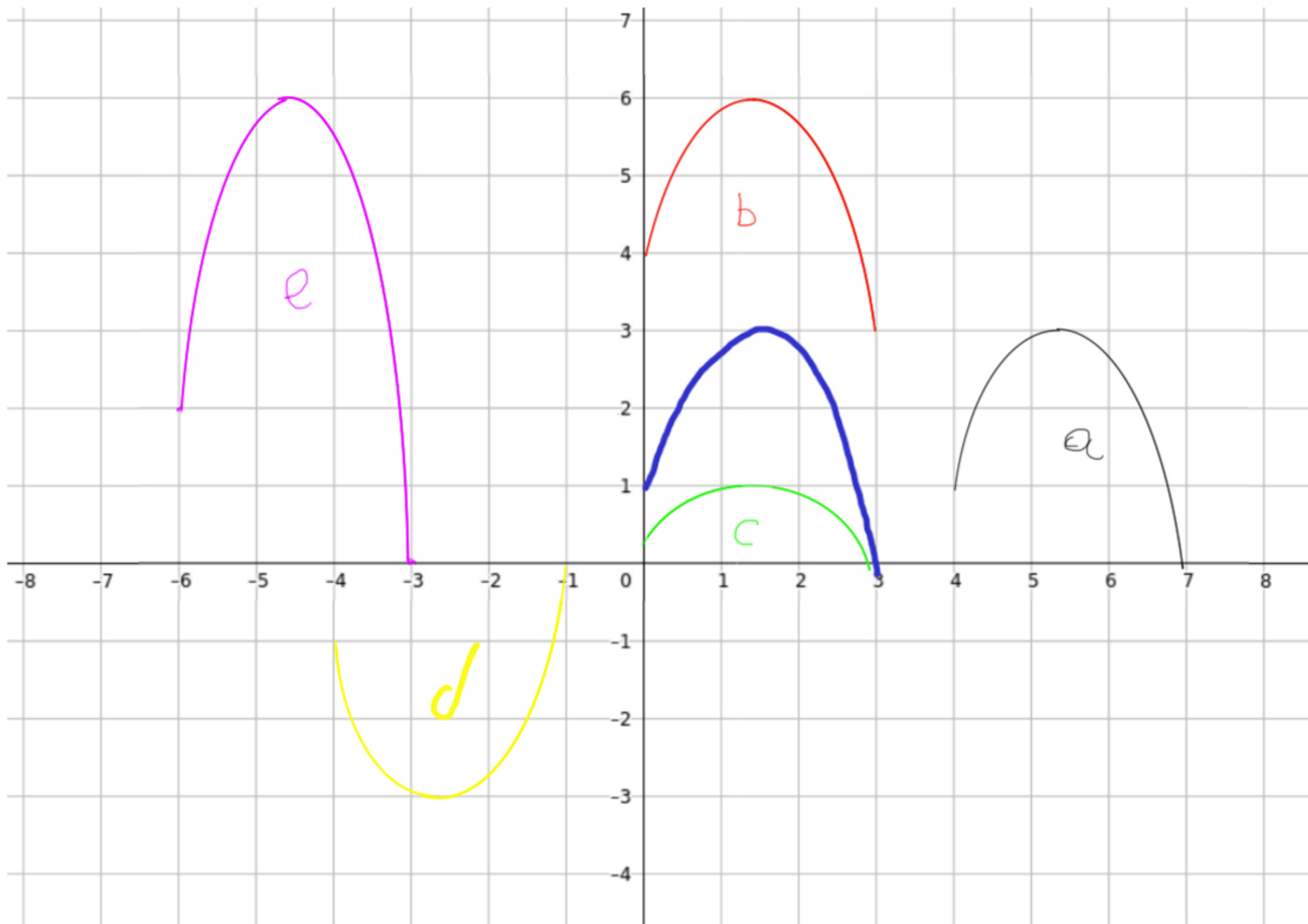


1-



$$2- \text{ a) } h(x) = 4x^2 + 4x + 1 + 6 = (2x+1)^2 + 6 \rightarrow g(x)$$

$$f(x) = x^2 + 6$$

$$\text{ b) } h(x) = 4x + 16 - 17 = 4(x+4) - 17 \rightarrow f(x)$$

$$g(x) = 4x - 17$$

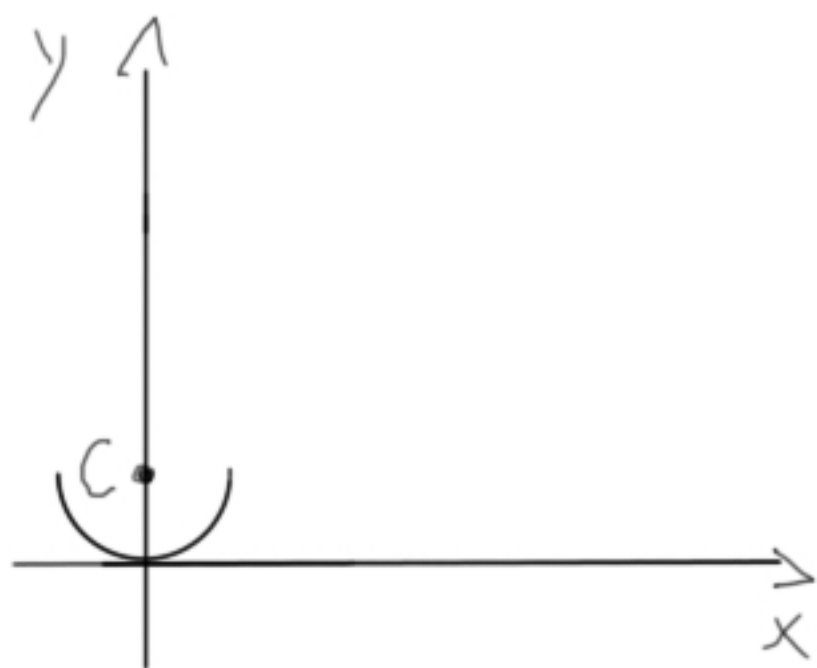
$$\text{ c) } y = \frac{2}{x} - 4 \xrightarrow[\text{inverse}]{\text{legendre}} x = \frac{2}{y} - 4 \rightarrow x+4 = \frac{2}{y} \rightarrow y = \frac{2}{(x+4)}$$

$$g(x) = \frac{2}{x+4}$$

3-

$$a) x^2 + (y-2)^2 = 4$$

centro é $C(0; 2)$ de raio 2



$$S = \{x \in \mathbb{R} \mid -2 \leq x \leq 2\}$$

$$(y-2)^2 = 4 - x^2$$

$$y-2 = \sqrt{4-x^2}$$

$$y = \pm \sqrt{4-x^2} + 2$$

porém, queremos só a metade inferior

$$y = -\sqrt{4-x^2} + 2$$

b)



$$A = \frac{l \cdot \sin 60^\circ \cdot l}{2} = \frac{\frac{\sqrt{3}}{2} \cdot l^2}{2} = \frac{l^2 \sqrt{3}}{4}$$

$$f(x) = \frac{x^2 \sqrt{3}}{4}$$

$$S = \{x \in \mathbb{R} \mid x > 0\}$$

c) primeira função: $y - y_0 = m \cdot (x - x_0)$ $y - 1 = -1 \cdot (x - (-3))$
 $1 - 2 = m \cdot (-3 - (-4))$ $y = -x - 2$
 $-1 = m \cdot 1$
 $m = -1$

segunda função:
 (circunferência) $(x^2 - 0) + (y^2 - 0) = 2^2$
 $y^2 = 4 - x^2$
 $y = \pm \sqrt{4 - x^2}$

terceira função: $3 - 0 = m \cdot (3 - 2)$ $y - 0 = 3 \cdot (x - 2)$
 $m = 3$ $y = 3x - 6$

$f: [-5, 3] \longrightarrow \mathbb{R}$, é dado por

$$f(x) = \begin{cases} y = -x - 2, & \text{para } -5 \leq x \leq -2 \\ y = \sqrt{4-x^2}, & \text{para } -2 \leq x \leq 2 \\ y = 3x - 6, & \text{para } 2 \leq x \leq 3 \end{cases}$$

$$4 - \frac{1}{|3x-8|} > 20$$

$$\text{case } 3x-8 > 0$$

$$\frac{1}{3x-8} > 20 \Rightarrow 1 > 60x - 160$$

$$161 > 60x$$

$$\frac{161}{60} > x$$

$$S: \left\{ x \in \mathbb{R} \mid \right] \frac{53}{20} ; \frac{8}{3} [\cup \left] \frac{8}{3} ; \frac{161}{60} [$$

$$\text{case } 3x-8 < 0$$

$$-\frac{1}{(3x-8)} > 20 \Rightarrow \frac{1}{-3x+8} > 20 \Rightarrow 1 > -60x + 160$$

$$-159 > -60x$$

$$159 < 60x \Rightarrow \frac{159}{60} < x \Rightarrow \frac{53}{20} < x$$

$$x \neq \frac{8}{3}$$