# Anamorphic Signatures

Secrecy From a Dictator Who Only Permits Authentication!

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Joint work with Miroslaw Kutyłowski, Duong Hieu Phan, Moti Yung, Marcin Zawada

### Privacy as a Human Right

UDHR, Article 12: (1948)

No one shall be subjected to arbitrary interference with his privacy, family, home or correspondence,...

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#### End to End Encryption

- Cryptography has been very successful in providing tools for encrypting communication
  - ► The Signal protocol and app



### The receiver-privacy assumption

Encryption guarantees message confidentiality only with respect to parties that do not have access to the receiver's private key

The receiver-privacy assumption

The receiver keeps his secret key in a private location

### Receiver privacy

- Realistic for "normal" settings
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  - with no explicit mention

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### Receiver privacy

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  - with no explicit mention
- In a dictatorship, instead
  - No receiver privacy: citizens might be invited to surrender their private keys



# Democracies attempt to regulate encryption

### The Clipper Chip

Presently, anyone can obtain encryption devices for voice or data transmissions. [...] if criminals can use advanced encryption technology in their transmissions, electronic surveillance techniques could be rendered useless because of law enforcement's inability to decode the message.

Howard S. Dakoff

The Clipper Chip Proposal, J. Marshall L. Rev., 29, 1996.

### Ban of E2E encryption

In our country, do we want to allow a means of communication between people which even in extremis, with a signed warrant from the Home Secretary personally, that we cannot read?

> David Cameron UK Prime Minister January 2015

# Crypto Wars

#### Arguments against restricting encryptions:

- the bad guys can utilize other encryption systems
- all other encryption schemes must be declared illegal
  - what qualifies as an encryption scheme? e.g., chaffing and winnowing
- it creates a natural weak system security point
  - ► Frankel and Yung showed how to frame legitimate users in the Clipper Chip [Crypto 95]

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#### indirect and non-technical



#### A Dictator's Paradise

#### A thought experiment

- Let us have it the Dictator's way
  - Encryption still allowed
  - Users must surrender the secret keys associated with their public keys
- Did the dictator achieve their goal?
  - Access to all communication

# **Enter Anamorphic Encryption**

[P, Phan, Yung - Eurocrypt 22]

#### The anamorphic approach

- A ciphertext is associated with two secret keys sk, dkey
- share dkey with your friend
- A ciphertext ct carries two plaintexts  $m_0, m_1$ , one for each key
  - $m_0 = \text{Dec}(ct, sk)$ , the regular decryption algorithm
  - $m_1 = aDec(ct, dkey)$ , the anamorphic decryption algorithm
- ...and there is no second key
  - at least, that's what the dictator thinks
  - when dictator asks for keys, give him sk because there is only one key...

### The anamorphic thesis

#### The anamorphic thesis

#### Regulating/crippling encryption is technically futile

- Because Anamorphic Encryption exists
  - ► Feasibility of Anamorphic Encryption [P, Phan, Yung EC22]
    - \* The Naor-Yung CCA encryption scheme
- Because Anamorphic Encryption is being used
  - Prevalence of Anamorphic Encryption [Kutilowski, P, Phan, Yung,
    Zawada PETS 23]
    - \* Paillier, RSA-OAEP, Goldwasser-Micali
    - \* ElGamal, Cramer-Shoup, Smooth Projective Hash Functions

### Resistance is futile



### A Frequent Objection

The dictator can hit you with the wrench until you surrender the **second** key

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Rather to tell democracies how low they must go to effectively control private communication

and then ask if it is worth it

### Futile, you said?

### Encryption is declared illegal

 the dictator mandates that all communication happens through a central hub

- messages can only be digitally signed
  - so that we know whom we are talking to

### Futile, you said?

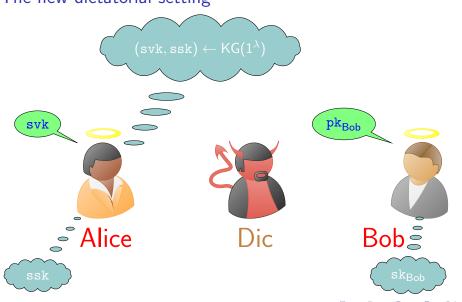
### Encryption is declared illegal

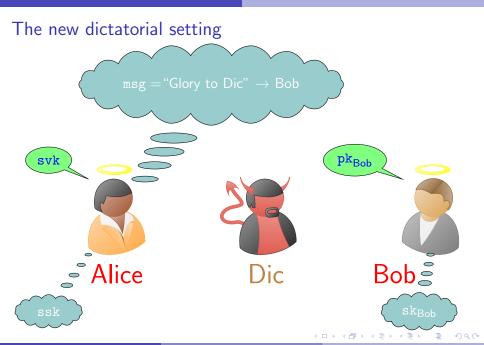
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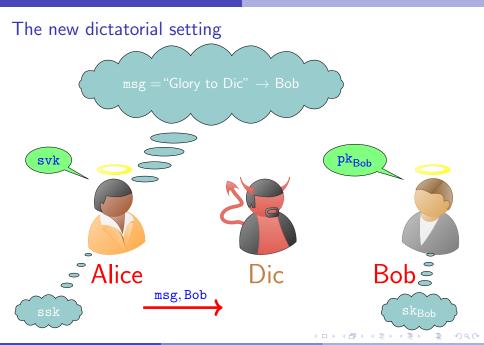
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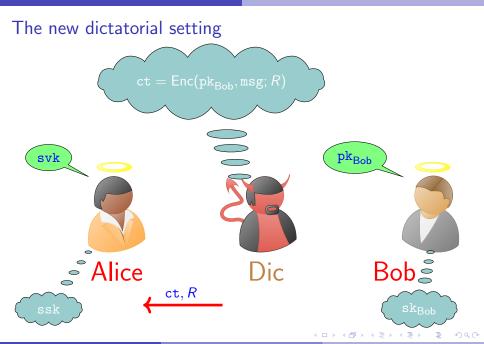
#### Do not annoy your dictator!

# The new dictatorial setting

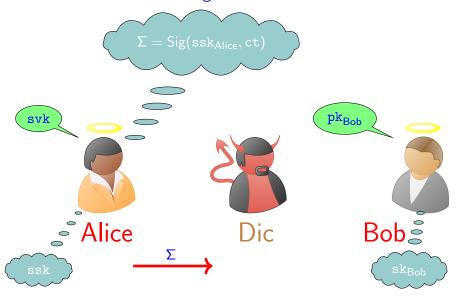






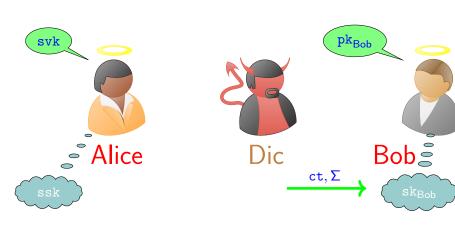


# The new dictatorial setting



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# The new dictatorial setting

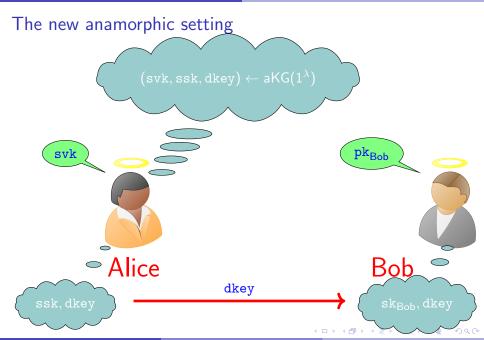


# Dictator's thinking

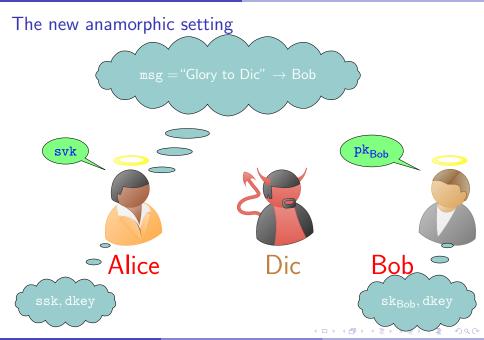
- Every user has a private channel to the Dic
- Every user has a public and secret encryption key
- Every user has a verification and signing key
- Dic is the only allowed to use encryption on a public channel

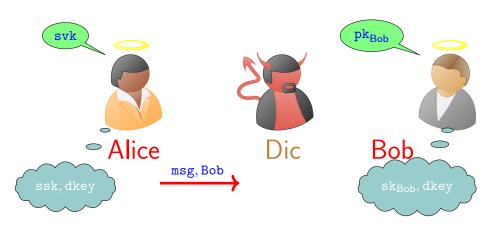


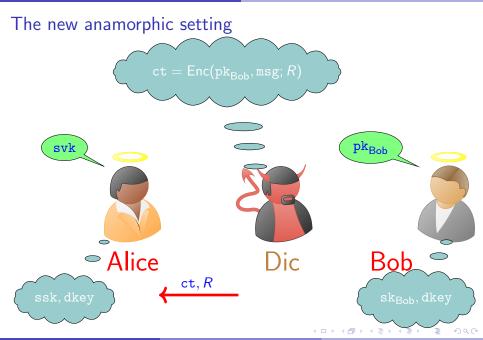


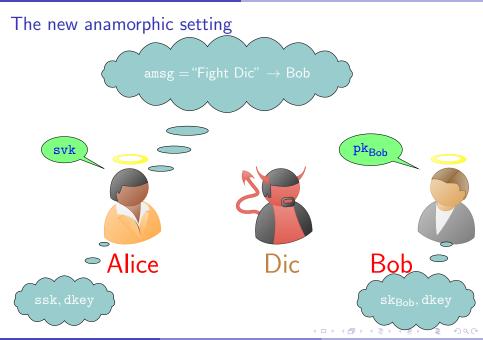


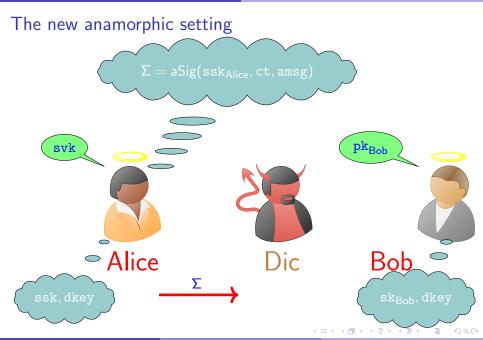


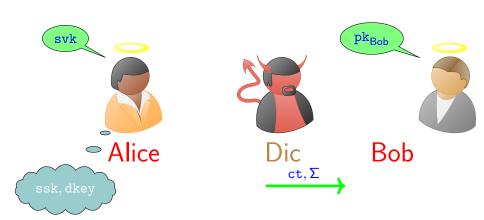














#### Signature Schemes

- ullet the *key-generation* algorithm  $\mathsf{KG}(1^\lambda)$ 
  - (svk, ssk), a public verification key and secret signing key;
- the signing algorithm Sig(msg, ssk)
  - ightharpoonup signature  $\Sigma$ ;
- the *verification* algorithm  $Verify(\Sigma, msg, svk)$ 
  - ightharpoonup accepts or rejects  $\Sigma$  as a signature of msg.

#### Anamorphic Triplet

- the anamorphic key-generation algorithm  $\mathsf{aKG}(1^\lambda)$ 
  - (svk, ssk, dkey), a public verification key, a secret signing key, and a double key;
- the anamorphic signing algorithm aSig(msg, amsg, ssk, dkey)
  - $\triangleright$  anamorphic signature  $\Sigma$ ;
- the anamorphic decryption algorithm aDec(Σ, svk, dkey)
  - amsg.

# Security Notion for Anamorphic Signatures

# $\mathsf{RealG}_{\mathsf{S},\mathcal{D}}(\lambda)$

- e return  $\mathcal{D}^{Os(\cdot,\cdot,ssk)}(svk,ssk)$ , where Os(msg,amsg,ssk) = Sig(msg,ssk).

#### Anamorphic $G_{T,\mathcal{D}}(\lambda)$

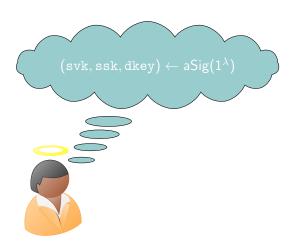
- e return  $\mathcal{D}^{Oa(\cdot,\cdot,assk,dkey)}(asvk,assk)$ , where Oa(msg,amsg,assk,dkey) = aSig(msg,amsg,assk,dkey).

# **Anamorphic Channels**

 dkey can be used to establish an anamorphic channel between signers and verifiers that have access to dkey

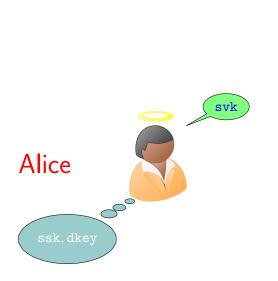
- The channel can be One-to-Many
  - dkey does not give you the ability to sign
  - ▶ only the signer can send anamorphic messages

- The channel can be Many-to-Many
  - dkey does give you the ability to sign
  - everybody is a signer and can send anamorphic messages



Alice







 $\mathsf{Bob}_1$ 



 $\mathsf{Bob}_2$ 

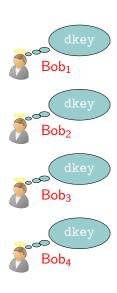


Bob<sub>3</sub>

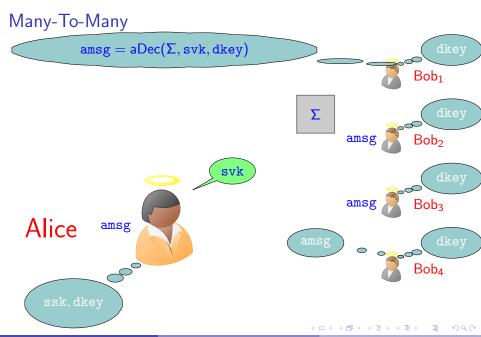


 $\mathsf{Bob}_4$ 





# Many-To-Many Bob<sub>1</sub> Σ Bob<sub>2</sub> svk Bob<sub>3</sub> **Alice** $\Sigma = aSig(msg, amsg, dkey)$





**Alice** 













 $\Sigma = aSig(msg, amsg, ssk, dkey)$ 



Σ







# One-To-Many $amsg = aDec(\Sigma, svk, dkey)$ Bob<sub>1</sub> svk Alice

# One-to-Many Anamorphic Signatures

# $\mathsf{DsigG}^{\mathcal{A}}_{\mathsf{S},\mathsf{T}}(\lambda)$

- $(\text{msg}, \Sigma) \leftarrow \mathcal{A}^{\text{Os}(\cdot, \text{assk})}(\text{asvk}, \text{dkey}),$ where Os(m, assk) = (m, Sig(m, assk));
- ③ if  $Verify(\Sigma, msg, asvk) = 1$  and  $(msg, \Sigma)$  has not been returned by Os then return 1; else return 0.

### A General Technique

- dkey includes the key K of a symmetric encryption scheme
- A two step procedure
  - ▶ identify *extractable* randomness from the signature
  - ► replace randomness with ciphertext encrypted using *K*

ciphertexts must be indistinguishable from random

# Symmetric Encryption with PseudoRandom Ciphertexts

prEnc returns  $\ell(\lambda)$ -bit ciphertexts for encrypting  $n(\ell)$ -bit messages with a key with security parameter  $\lambda$ 

```
\mathsf{PRCtG}^{\beta}_{\mathsf{prE},\mathcal{A}}(\lambda)
```

- **Q** Return  $\mathcal{A}^{\mathsf{OPr}^{\beta}(K,\cdot)}()$ , where, for  $n(\lambda)$ -bit plaintext msg,  $\mathsf{OPr}^{0}(K,\mathsf{msg})$  returns a randomly selected  $\ell(\lambda)$ -bit string;  $\mathsf{OPr}^{1}(K,\mathsf{msg}) = \mathsf{prEnc}(K,\mathsf{msg})$ .

# The Boneh-Boyen signature scheme

- The Key Generation algorithm  $bbKG(1^{\lambda})$ 
  - $(G_1, G_2, G_T, e, p) \leftarrow \mathcal{G}(1^{\lambda})$
  - ▶ Generators  $g_1 \in G_1, g_2 \in G_2$
  - $\triangleright$   $x, y \leftarrow \mathbb{Z}_p$
  - $ightharpoonup z = e(g_1, g_2), u = g_2^x, v = g_2^y.$
  - $svk = (g_1, g_2, u, v, z)$  and  $ssk = (g_1, x, y)$ .
- The Signing algorithm  $\mathsf{bbSig}(\mathsf{ssk} = (g_1, x, y), \mathsf{msg} \in \mathbb{Z}_p)$ 
  - ▶ randomly selects  $r \leftarrow \mathbb{Z}_p$ .
  - ▶ If r = -(x + msg)/y then  $\bot$ .
  - return  $(r, \sigma = g_1^{1/(x+msg+yr)})$ .
- The Verification algorithm bbVerify( $\Sigma = (r, \sigma)$ )
  - ▶ check

$$e(\sigma, u \cdot g_2^m \cdot v^r) = z.$$



# Anamorphic Triplet for BB

- ullet The anamorphic key generation algorithm  $\mathsf{abbKG}(1^\lambda)$ 
  - $(svk, ssk) \leftarrow bbKG(1^{\lambda})$
  - $K \leftarrow \operatorname{prKG}(1^{\lambda})$ .
  - ▶ return
    - ★ anamorphic verification key asvk := svk,
    - ★ anamorphic signing key assk := ssk,
    - ★ double key dkey := K
- The anamorphic signing algorithm abbSig(msg, amsg, ssk, dkey)
  - ▶ act = prEnc(K, amsg)
  - ▶  $r = \text{act and if } r = -(x + m)/y \text{ then } \bot$
  - return  $a\Sigma = (r, \sigma = g_1^{1/(x+m+yr)})$ .
- The anamorphic decryption algorithm  $aDec(a\Sigma = (r, \sigma), dkey = K)$ 
  - ▶ return amsg = prDec(K, r).

#### The Fiat-Shamir Heuristics

# The Schnorr Signature Scheme

- The Key Generation algorithm  $ScKG(1^{\lambda})$ 
  - $\blacktriangleright$   $\mathbb{G}$ , a cyclic group of prime order q
  - ▶ a generator  $g \in \mathbb{G}$
  - ▶ hash function  $H: \{0,1\}^* \times \mathbb{G} \to \mathbb{Z}_q$ .
  - $\triangleright$   $x \leftarrow \mathbb{Z}_q$  and sets  $y = g^x$

$$ssk := (\mathbb{G}, g, H, x) \text{ and } svk := (\mathbb{G}, g, H, y).$$

- The Signing algorithm ScSig(ssk, msg)
  - $ightharpoonup \kappa \leftarrow \mathbb{Z}_q$ ,
  - $ightharpoonup r = g^{\kappa}$ , c = H(msg, r) and  $s = \kappa + c \cdot x$
  - ▶ Return  $\Sigma = (r, s)$ .
- The Verification algorithm ScVerify(Σ, msg, svk)
  - checks that

$$r = g^s \cdot y^{-H(msg,r)}$$



# Anamorphic Schnorr

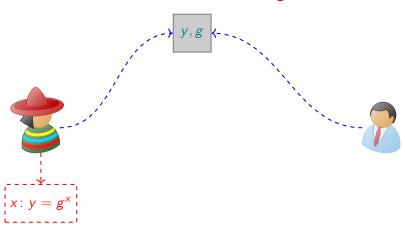
- The Signing algorithm ScSig(ssk, msg)
  - $ightharpoonup \kappa \leftarrow \mathbb{Z}_a$ ,
  - $r = g^{\kappa}$ , c = H(msg, r) and  $s = \kappa + c \cdot x$
  - ▶ Return  $\Sigma = (r, s)$

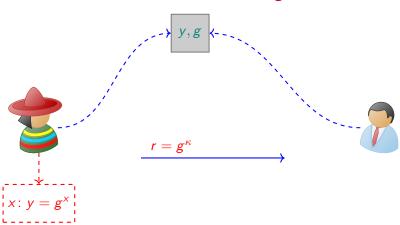
# Anamorphic Schnorr

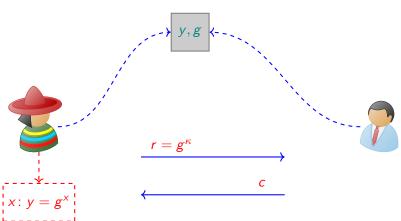
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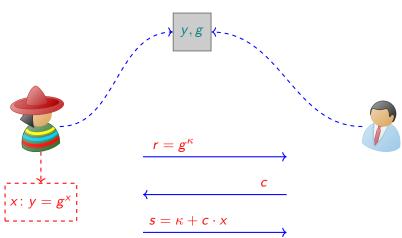
#### Fishing for randomness

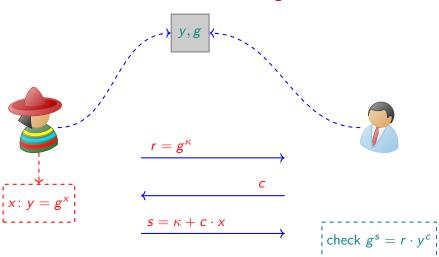
- Set  $r = \operatorname{prEnc}(K, \operatorname{amsg})$ 
  - ightharpoonup need  $\kappa$  to compute s
- Set  $\kappa = \operatorname{prEnc}(K, \operatorname{amsg})$ 
  - ightharpoonup cannot recover  $\kappa$  during verification
    - \* add x to dkey
    - \* a many-to-many anamorphic channel

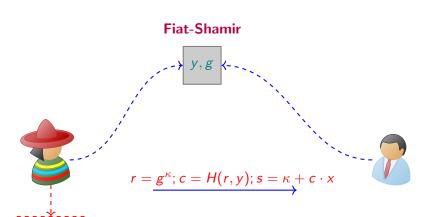




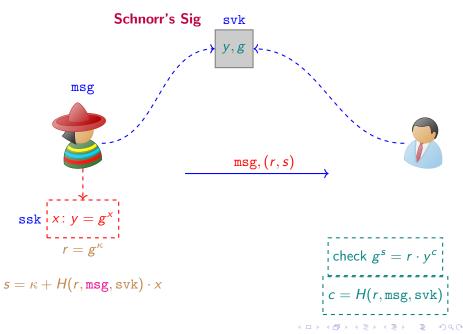


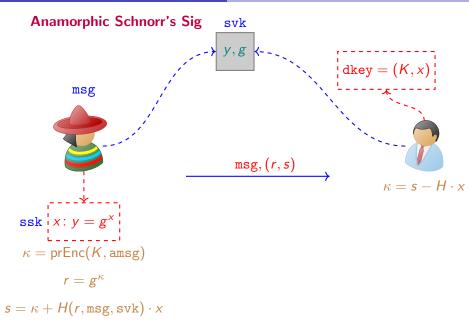


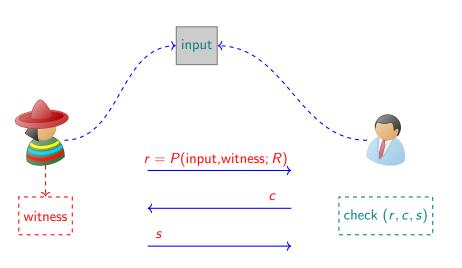




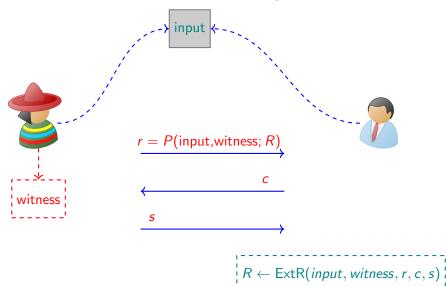
 $x: y = g^x$ 







#### **Sufficient condition for Anamorphism**



# Fiat-Shamir preserves Anamorphism

#### Fiat-Shamir Heuristics

How to construct a signature scheme from a 3-round interactive proof

#### Fiat-Shamir preserves Anamorphism

If 3-round interactive proof is anamorphic the resulting signature scheme is also anamorphic

## The Naor-Yung Transformation

## Lamport's Tagging Scheme [1979]

- ullet Key Generation algorithm LKG $(1^\lambda,1^\ell)$ 
  - ► for  $j = 1, ..., \ell$ . ★  $x_{0,j}, x_{1,j} \leftarrow \{0, 1\}^{\lambda}$ 
    - \*  $y_{0,j} = f(x_{0,j})$  and  $y_{1,j} = f(x_{1,j})$

$$\mathsf{Lvk} = ((y_{0,j}, y_{1,j}))_{j=1}^\ell \text{ and } \mathsf{Lsk} = ((x_{0,j}, x_{1,j}))_{j=1}^\ell.$$

- Signing algorithm LSig $(m_1, \ldots, m_\ell, Lsk)$ 
  - $\Sigma = (x_{m_j,j})_{j=1}^{\ell}.$
- Verification algorithm LVerify $(\Sigma, m_1, \dots, m_\ell, Lvk)$ 
  - ▶ check  $f(s_i) = y_{m_i,j}$  for  $j = 1, ..., \ell$ .



### We have a problem

- Signing is deterministic
  - no randomness to be extracted by the verifier
- There is randomness in the verification key: the  $x_{b,j}$ 's
- We can embed the anamorphic message amsg as  $x_{0,1} = \text{prEnc}(K, \text{amsg})$  and  $x_{1,1} = \text{prEnc}(K, \text{amsg})$ 
  - ▶ anamorphic message to be determined at key generation time
  - weakly anamorphic
- It is a one-time signature
- We are going to be fine
  - for one-time signatures key generation time "coincides" with signing time

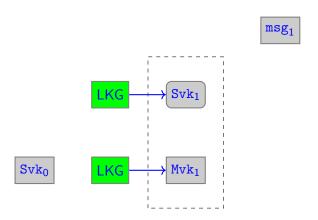
#### **NY Lifting**

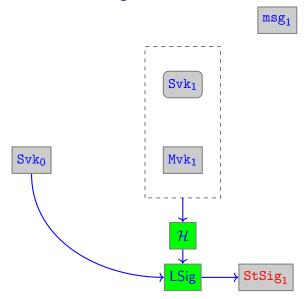
one-time to multi-time signature

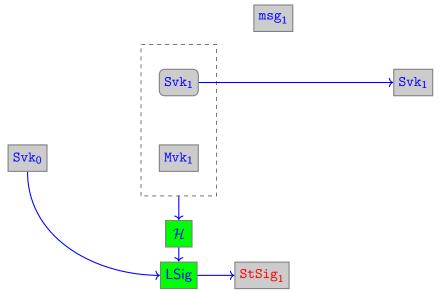
• weakly anamorphic to fully anamorphic

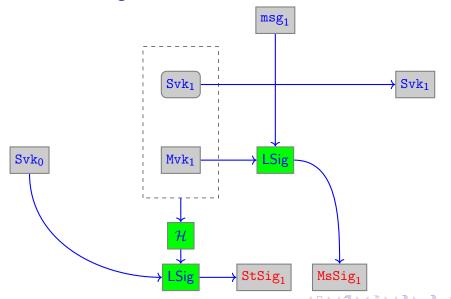
 $msg_1$ 

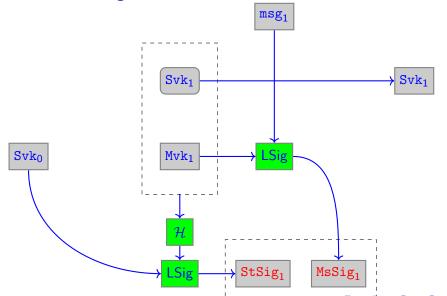
 $\mathtt{Svk}_0$ 







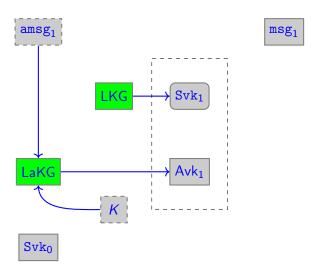


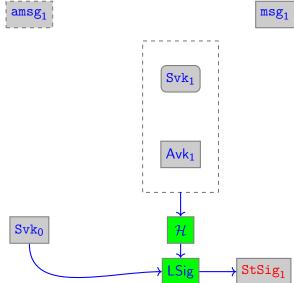


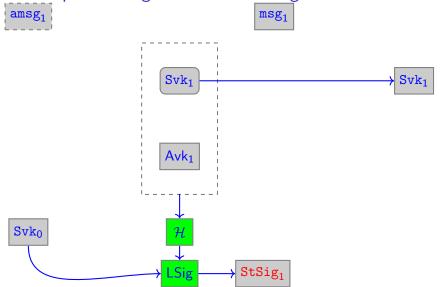


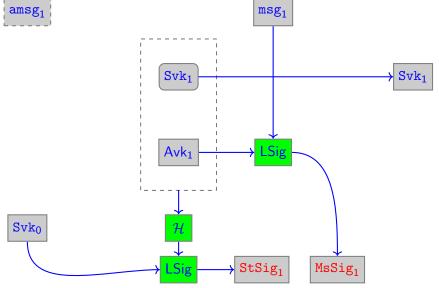


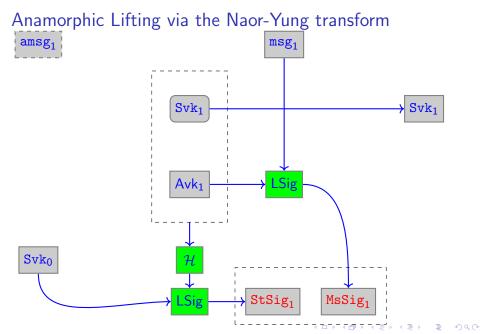
Svk<sub>0</sub>











## Anamorphism of NY

#### Lifting

If universal one-way hash functions exist, any weakly anamorphic one-time signature can be lifted to a fully anamorphic multi-time signature.

#### Naor-Yung-Lamport-Rompel

If one-functions exist then there exists a fully anamorphic multi-time signature scheme.

## One-to-Many Anamorphism of NY

### Separability of K

- K and (Svk<sub>0</sub>, Ssk<sub>0</sub>) are independent
- only need K to extract amsg
- K will not help produce signatures

### Technical summary

- the new notion of anamorphic signature
- theoretical properties
- two flavors:
  - one-to-many anamorphic communication
    - ★ dkey allows decryption but not signature
  - many-to-many anamorphic communication
    - ★ dkey allows decryption and signature
- one general technique
  - extract randomness and replace with ciphertext

## **Technical Summary**

- two design paradigms for signatures preserve anamorphism
  - ► Fiat-Shamir turns 3-round protocols into signatures in the ROM
    - If prover randomness can be extracted, then resulting signature is anamorphic
    - Schnorr, [Beth 88], [Guillou+Quisquater90], [Ong+Schnorr90, [Brickell+McCurley91], [Girault91], [Okamoto93], [Pointcheval95], [Stern94]
    - ★ Need the witness to extract (i.e., the signing key).
    - ★ Many-to-Many Anamorphism
  - Naor-Yung turns one-time signatures into many-time signatures in the standard model (assume one-way functions)
    - ★ If one-time signature eenjoys a weak form of anamorphism, resulting many-time is fully anamorphic
    - ★ Lamport, BC, HORS
    - **★** One-to-Many Anamorphism
- Applications to schemes using digital signatures
  - ► Canetti-Halevi-Katz CCA encryptions scheme uses a signature scheme
  - ▶ the transformation preserves anamorphism

#### Conclusions

- disallowing encryption is not sufficient
- must disallow message authentication too
  - complete disruption of communication
  - not clear who is talking to whom
- or disallow randomized signatures
  - ▶ more to come about this...
- dictator will not care
  - ▶ just give me dkey or else...
  - ▶ if no dkey then can't surrender it...
- technical evidence that a democracy cannot actually control communication
  - unless, that is, it ceases to be a democracy



- Giuseppe Persiano, Duong Hieu Phan, Moti Yung: Anamorphic Encryption: Private Communication against a Dictator. IACR Cryptol. ePrint Arch. 2022: 639 (2022). Eurocrypt '22
- Mirek Kutylowski, Giuseppe Persiano, Duong Hieu Phan, Moti Yung, Marcin Zawada: The Self-Anti-Censorship Nature of Encryption: On the Prevalence of Anamorphic Cryptography. IACR Cryptol. ePrint Arch. 2023: 434 (2023). PETS '23
- Mirek Kutylowski, Giuseppe Persiano, Duong Hieu Phan, Moti Yung, Marcin Zawada: Anamorphic Signatures: Secrecy From a Dictator Who Only Permits Authentication! IACR Cryptol. ePrint Arch. 2023: 356 (2023). CRYPTO '23