Introduction to Machine Learning feat. TensorFlow



Peter Goldsborough

July 10, 2016

July 10, 2016

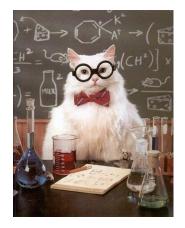
Table of Catents

Table of Catents



Theory

Table of Catents



Theory



Practice

CS Student @ TUM

- CS Student @ TUM
- ► Google & Bloomberg Intern

- CS Student @ TUM
- ► Google & Bloomberg Intern
- ► I like cats

- CS Student @ TUM
- ► Google & Bloomberg Intern
- I like cats

Seminar Topic: Deep Learning With TensorFlow github.com/peter-can-write/tensorflow-paper

github.com/peter-can-talk/python-meetup-munich-2016

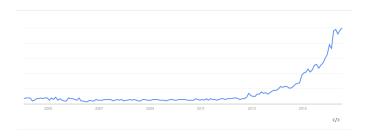
Time to go Deeper

What if the meaning of life is to spend your time thinking about the meaning of life?

The why

The why, the what

The why, the what and the ugly



Basic Definition

ightharpoonup Let ${\cal L}$ denote the number of hidden layers in a neural network

- lackbox Let ${\mathcal L}$ denote the number of hidden layers in a neural network
- ▶ Then we call neural network *deep*, if

- ightharpoonup Let $\mathcal L$ denote the number of hidden layers in a neural network
- Then we call neural network deep, if
 - 1. It is trained at more than 10,000m below sea level, or

- ightharpoonup Let $\mathcal L$ denote the number of hidden layers in a neural network
- Then we call neural network deep, if
 - 1. It is trained at more than 10,000m below sea level, or
 - 2. L > 1

- ightharpoonup Let $\mathcal L$ denote the number of hidden layers in a neural network
- Then we call neural network deep, if
 - 1. It is trained at more than 10,000m below sea level, or
 - 2. L > 1
- ► To really understand why many layers are a good idea, we must understand why few layers might be a bad idea

▶ Theoretically, a single layer is just enough

- ▶ Theoretically, a single layer is just enough
- However, we would need exponentially many units for discrete functions

- ▶ Theoretically, a single layer is just enough
- However, we would need exponentially many units for discrete functions
- And infinitely many for continuous functions

- ▶ Theoretically, a single layer is just enough
- However, we would need exponentially many units for discrete functions
- And infinitely many for continuous functions
- Just use an infinitely sized hash table

► The number of possible outputs scales exponentially with the dimensionality of our dataset

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



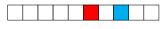
1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



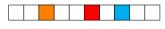
1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



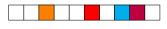
1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



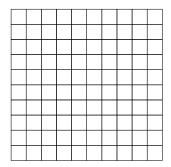
1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



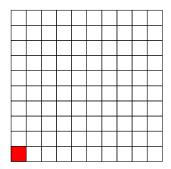
1 feature = 10 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



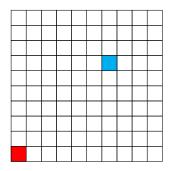
2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



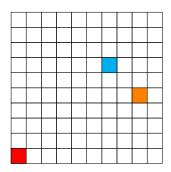
2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



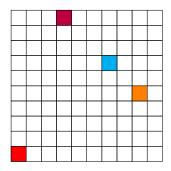
2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



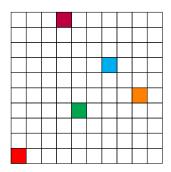
2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



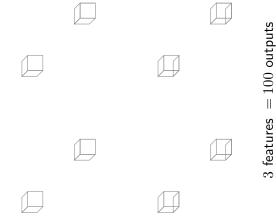
2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



2 features = 100 outputs

- ► The number of possible outputs scales exponentially with the dimensionality of our dataset
- Assume our features have 10 possible values



Why is this a problem?

- Why is this a problem?
- ▶ To predict an output, we must have seen at least one example

- Why is this a problem?
- ▶ To predict an output, we must have seen at least one example
- In high dimensions, an algorithm cannot possibly be trained on all possible output

- Why is this a problem?
- ▶ To predict an output, we must have seen at least one example
- In high dimensions, an algorithm cannot possibly be trained on all possible output, unless

- Why is this a problem?
- ▶ To predict an output, we must have seen at least one example
- In high dimensions, an algorithm cannot possibly be trained on all possible output, unless

We make assumptions about our data

Assumptions either

- Assumptions either
 - Explicitly reduce the output space, or

- Assumptions either
 - Explicitly reduce the output space, or
 - Create dependencies between outputs

- Assumptions either
 - Explicitly reduce the output space, or
 - ► Create dependencies between outputs
- Local constancy assumption (prior)

$$f^{\star}(\mathbf{x}) \approx f^{\star}(\mathbf{x} + \varepsilon)$$

- Assumptions either
 - Explicitly reduce the output space, or
 - ► Create dependencies between outputs
- Local constancy assumption (prior)

$$f^{\star}(\mathbf{x}) \approx f^{\star}(\mathbf{x} + \varepsilon)$$



- Assumptions either
 - Explicitly reduce the output space, or
 - ► Create dependencies between outputs
- Local constancy assumption (prior)

$$f^{\star}(\mathbf{x}) \approx f^{\star}(\mathbf{x} + \varepsilon)$$



- Assumptions either
 - Explicitly reduce the output space, or
 - Create dependencies between outputs
- Local constancy assumption (prior)

$$f^{\star}(\mathbf{x}) \approx f^{\star}(\mathbf{x} + \varepsilon)$$

Don't need as much data any more!



Deep Learning assumes that data is structured

Deep Learning assumes that data is structured hierarchically

Deep Learning assumes that data is structured

hierarchically

Note:

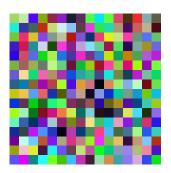
According to the No Free Lunch Theorem it is just as bad as flipping a coin.

 Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition

- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- ▶ They assume their input are images



- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- ▶ They assume their input are images



- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- ► They assume their input are images



- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- They assume their input are images

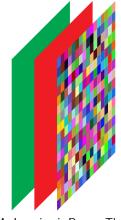


- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- They assume their input are images



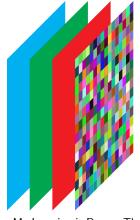
My Learning is Deeper Than Yours

- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- They assume their input are images



My Learning is Deeper Than Yours

- Convolutional Neural Networks (CNNs; ConvNets) are used in image recognition
- They assume their input are images



My Learning is Deeper Than Yours

 \blacktriangleright We want to classify images into one of k classes

- \blacktriangleright We want to classify images into one of k classes
- ▶ The model should learn to extract features

- \blacktriangleright We want to classify images into one of k classes
- ▶ The model should learn to extract features
- We expect it to exploit the hierarchical nature of the data

- We want to classify images into one of k classes
- ▶ The model should learn to extract features
- We expect it to exploit the hierarchical nature of the data
 - 1. Lines and edges
 - 2. Corners and contours
 - 3. Abstract components (e.g. noses, ears, feet)
 - 4. Entire objects (e.g. faces, spaceship)

- ▶ We want to classify images into one of *k* classes
- ▶ The model should learn to extract features
- We expect it to exploit the hierarchical nature of the data
 - Lines and edges
 - 2. Corners and contours
 - 3. Abstract components (e.g. noses, ears, feet)
 - 4. Entire objects (e.g. faces, spaceship)
- First idea: just feed the pixels into a neural network

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

concatenate (R.flatten, G.flatten, B.flatten)

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

$$R. flatten = \begin{bmatrix} 116 & 80 & 170 & 194 \end{bmatrix}$$

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

$$R. {\tt flatten} = \begin{bmatrix} 116 & 80 & 170 & 194 \end{bmatrix}$$
 $G. {\tt flatten} = \begin{bmatrix} 82 & 78 & 5 & 236 \end{bmatrix}$

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

$$R. {\tt flatten} = \begin{bmatrix} 116 & 80 & 170 & 194 \end{bmatrix}$$
 $G. {\tt flatten} = \begin{bmatrix} 82 & 78 & 5 & 236 \end{bmatrix}$ $B. {\tt flatten} = \begin{bmatrix} 76 & 139 & 245 & 236 \end{bmatrix}$

$$\begin{bmatrix} 116 & 80 \\ 170 & 194 \end{bmatrix} \quad \begin{bmatrix} 82 & 78 \\ 5 & 236 \end{bmatrix} \quad \begin{bmatrix} 76 & 139 \\ 245 & 236 \end{bmatrix}$$

$$R \qquad \qquad G \qquad \qquad B$$

$$\begin{split} R. \texttt{flatten} &= \begin{bmatrix} 116 & 80 & 170 & 194 \end{bmatrix} \\ G. \texttt{flatten} &= \begin{bmatrix} 82 & 78 & 5 & 236 \end{bmatrix} \\ B. \texttt{flatten} &= \begin{bmatrix} 76 & 139 & 245 & 236 \end{bmatrix} \end{split}$$

$$\mathbf{x} = [116, 80, 170, 194, 82, 78, 5, 236, 76, 139, 245, 236]$$

▶ Why is this a bad idea?

- Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images

- ▶ Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images
 - \triangleright 200 × 200 × 3 = 120,000 features

- ▶ Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images
 - \triangleright 200 × 200 × 3 = 120,000 features
 - With 100 hidden units: $100 \times 120,000 = 12,000,000$

- Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images
 - \triangleright 200 × 200 × 3 = 120,000 features
 - With 100 hidden units: $100 \times 120,000 = 12,000,000$
 - ▶ With 5 layers: $12,000,000 \times 5 = 60,000,000$ weights

- ▶ Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images
 - \triangleright 200 × 200 × 3 = 120,000 features
 - With 100 hidden units: $100 \times 120,000 = 12,000,000$
 - ▶ With 5 layers: $12,000,000 \times 5 = 60,000,000$ weights
 - ▶ $1000 \times 1000 \rightarrow 1,500,000,000$ weights

- Why is this a bad idea?
 - 1. Fully connected NNs scale badly for images
 - \triangleright 200 × 200 × 3 = 120,000 features
 - With 100 hidden units: $100 \times 120,000 = 12,000,000$
 - ▶ With 5 layers: $12,000,000 \times 5 = 60,000,000$ weights
 - ► $1000 \times 1000 \rightarrow 1,500,000,000$ weights
 - 2. It assumes every pixel has entirely new information



This is a cat ♥



Still a cat ♥♥



Half cat / half salad ♥♥♥



Minecraft cat ♥♥♥♥

▶ Our network learns to detect a feature in one part of the image

- Our network learns to detect a feature in one part of the image
- Wouldn't it make sense to reuse that information?

- Our network learns to detect a feature in one part of the image
- Wouldn't it make sense to reuse that information?
- Yes!

Weight Sharing

Recipe for a Convolutional Neural Network

Ingredients

- Ingredients
 - 1. Image I with dimension $w \times h \times d$

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking

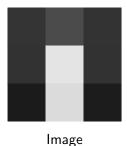
- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking
 - Put the image into the oven at 150°C

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking
 - Don't put the image into the oven at 150°C

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking
 - ▶ Don't put the image into the oven at 150°C
 - Slide the kernel across the image

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking
 - ▶ Don't put the image into the oven at 150°C
 - Slide the kernel across the image
 - ► Compute the "dot product" for each configuration

- Ingredients
 - 1. Image I with dimension $w \times h \times d$
 - 2. A kernel (filter) K of size $k \times k \times d$
- Cooking
 - Don't put the image into the oven at 150°C
 - Slide the kernel across the image
 - Compute the "dot product" for each configuration
 - ▶ (This is a convolution I * K)



0.4	0.9	0.1
0.7	0.2	0.6
0.8	0.3	0.5

Image

0.4	0.9	0.1
0.7	0.2	0.6
0.8	0.3	0.5

Image

Kernel

$5.7 \cdot 0.4$	$2.4 \cdot 0.9$	0.1
$3.1 \cdot 0.7$	$0.9 \cdot 0.2$	0.6
0.8	0.3	0.5

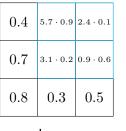
Image

$5.7 \cdot 0.4$	$2.4 \cdot 0.9$	0.1
$3.1 \cdot 0.7$	$0.9 \cdot 0.2$	0.6
0.8	0.3	0.5

6.79

Image

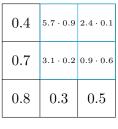
Output



Image

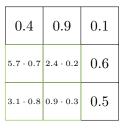
Output

6.79



6.79 6.53

Image



6.79 6.53

Image



6.79 6.53 7.67

Image

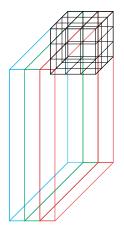


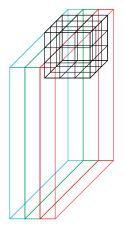
6.79 6.53 7.67

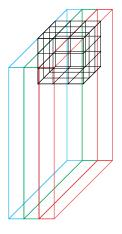
Image

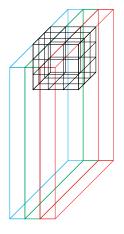


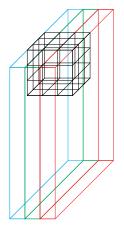
Image

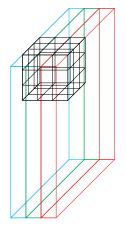


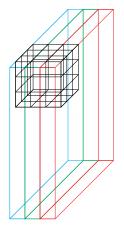


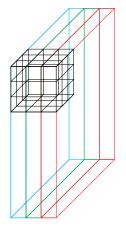


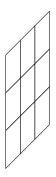


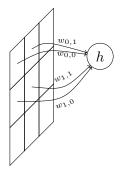


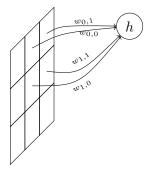


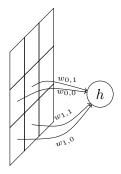


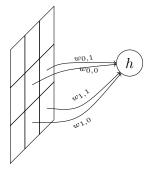












Convolutional Neural Networks have three hyperparameters

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)



- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)



- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)



- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)

0	0	0	0	0	0
0					0
0					0
0					0
0					0
0	0	0	0	0	0

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)

0	0	0	0	0	0
0	×				0
0					0
0					0
0					0
0	0	0	0	0	0

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)

0	0	0	0	0	0
0		×			0
0					0
0					0
0					0
0	0	0	0	0	0

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)

0	0	0	0	0	0
0			×		0
0					0
0					0
0					0
0	0	0	0	0	0

- Convolutional Neural Networks have three hyperparameters
 - 1. Kernel size
 - 2. Kernel stride
 - 3. Padding (valid or same)

0	0	0	0	0	0
0				X	0
0					0
0					0
0					0
0	0	0	0	0	0

▶ Pooling achieves translational invariance

- Pooling achieves translational invariance
- A form of downsampling

- Pooling achieves translational invariance
- A form of downsampling
- ► The maximum stays the maximum

66	2
6	32

- Pooling achieves translational invariance
- A form of downsampling
- ► The maximum stays the maximum

6	2
66	32

- Pooling achieves translational invariance
- A form of downsampling
- ► The maximum stays the maximum

2	66
6	32

- Pooling achieves translational invariance
- A form of downsampling
- ► The maximum stays the maximum

32	6
2	66

Convolutional Neural Network: Architecture

[?]

► Each layer of a ConvNet learns to detect features

- ► Each layer of a ConvNet learns to detect features
- Later layers combine features of earlier layers

- ► Each layer of a ConvNet learns to detect features
- Later layers combine features of earlier layers
- ► For early layers, we can still gain an intuition of what they do

What's in a kernel?

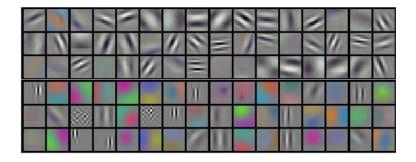
0	1	0
0	1	0
0	1	0

Patterns

What's in a kernel?

0	0	0
-1	1	0
0	0	0

Features



Recurrent Neural Networks

LSTMs

▶ Why the recent success of deep learning?

- ▶ Why the recent success of deep learning?
- ► Three reasons

- ▶ Why the recent success of deep learning?
- ► Three reasons
 - 1. Better hardware

- ▶ Why the recent success of deep learning?
- ► Three reasons
 - 1. Better hardware
 - 2. More data

- ▶ Why the recent success of deep learning?
- ► Three reasons
 - 1. Better hardware
 - 2. More data
 - 3. Better methods

The Ugly

References