

# Presentation at L3S Research Seminar

DALE: Differential Accumulated Local Effects for efficient and accurate global explanations

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# Who we are

- **Vasilis Gkolemis:**
  - ▶ Research Assistant at ATHENA Research Center ([ATHENA RC](#))
  - ▶ First-year PhD at Harokopio University of Athens ([HUA](#))
  - ▶ Main focus: Explainability under uncertainty
- Supervisors:
  - ▶ [Christos Diou](#) (HUA) → Generalization under few-shot
  - ▶ [Eirini Ntoutsi](#) (UniBw-M) → Explainability, Fairness
  - ▶ [Theodore Dalamagas](#) (ATHENA) → Databases, data semantics
- Paper I will present
  - ▶ [DALE: Differential Accumulated Local Effects for efficient and accurate global explanations](#)
  - ▶ Accepted at [Asian Conference Machine Learning \(ACML\) 2022](#)

# eXplainable AI (XAI)

- Black-box model  $f(\cdot) : \mathcal{X} \rightarrow \mathcal{Y}$ , trained on  $\mathcal{D}$
- XAI extracts interpretable properties:
  - Tabular data - Which features favor a prediction?
  - Computer Vision - Which image areas confuse the model?
  - NLP - Which words classified the comment as offensive?
- Categories:
  - Global vs local
  - Model-agnostic vs Model-specific
  - Output? number, plot, instance etc.

Feature Effect: global, model-agnostic, outputs plot

# Feature Effect

$y = f(x_s) \rightarrow$  plot showing the effect of  $x_s$  on the output  $y$

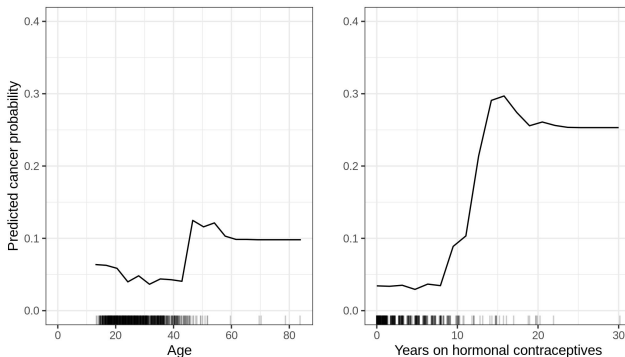


Figure: Image taken from Interpretable ML book (Molnar, 2022)

Feature Effect is simple and intuitive.

# Feature Effect Methods

- $x_s \rightarrow$  feature of interest,  $\mathbf{x}_c \rightarrow$  other features
- Isolating the effect of  $x_s$  is a difficult task:
  - ▶ features are correlated
  - ▶  $f$  has learned complex interactions
- Three well-known methods:
  - ▶ Partial Dependence Plots (PDP)
  - ▶ M-Plots
  - ▶ Accumulated Local Effects (ALE)

# Partial Dependence Plots (PDP)

- Proposed by J. Friedman on 2001<sup>1</sup> and is the marginal **effect** of a feature to the model output:

$$f_s(x_s) = \mathbb{E}_{\mathbf{x}_c} [f(x_s, \mathbf{x}_c)] = \int f(x_s, \mathbf{x}_c) p(\mathbf{x}_c) d\mathbf{x}_c$$

where:

- $x_s$  is the feature whose effect we wish to compute
  - $\mathbf{x}_c$  are the rest of the features
- Approximation:

$$\hat{f}_s(x_s) = \frac{1}{n} \sum_{i=1}^n f(x_s, \mathbf{x}_c^{(i)})$$

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<sup>1</sup>J. Friedman. "Greedy function approximation: A gradient boosting machine." Annals of statistics (2001): 1189-1232

# Issues with PDPs

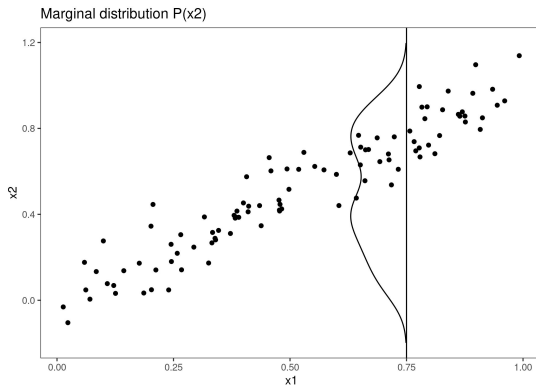


Figure: C. Molnar, IML book

- Correlated features

- ▶ Example:  $\text{price} = f(\text{num\_rooms}, \text{area})$
- ▶ To compute the effect of  $x_{\text{age}} = 20$  on the output (cancer probability) it will integrate over all  $x_{\text{years\_contraceptives}}$  values
- ▶  $f$  can have weird behaviour when  $x_{\text{age}} = 20, x_{\text{years\_contraceptives}} = 20$  (out of distribution)
- ▶ As a result, we have a wrong estimation of the feature effect



- We use the value of  $x_s$  as a condition, so we integrate over  $\mathbf{x}_c | x_s$

$$f(x_s) = \mathbb{E}_{\mathbf{x}_c | x_s} [f(x_s, \mathbf{x}_c)] = \int f(x_s, \mathbf{x}_c) p(\mathbf{x}_c | x_s) d\mathbf{x}_c$$

where:

- ▶  $x_s$  is the feature whose effect we wish to compute
- ▶  $\mathbf{x}_c$  the rest of the features
- Computation:

$$f_s(x_s) = \frac{1}{n} \sum_{i: x_s^{(i)} \approx x_s} f(x_s, \mathbf{x}_c^{(i)})$$

In the previous example

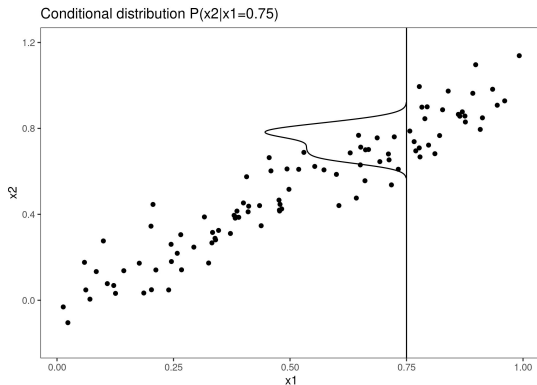


Figure: C. Molnar, IML book

# Issues with M-Plots

- Aggregated effect symptom  $\rightarrow$  the calculated effects result from the combination of all (correlated) features
- Real effect:
  - ▶  $x_{\text{age}} = 50 \rightarrow 10$
  - ▶  $x_{\text{years_contraceptives}} = 20 \rightarrow 10$
  - ▶ aggregated effect close to 20
- Because  $x_{\text{age}}, x_{\text{years_contraceptives}}$  are correlated, MPlot may assign:
  - ▶  $x_{\text{age}} = 50 \rightarrow 17 \approx$  aggregated effect
  - ▶  $x_{\text{years_contraceptives}} = 20 \rightarrow 17 \approx$  aggregated effect

# Accumulated Local Effects (ALE)<sup>2</sup>

- Resolves problems that result from the feature correlation by computing differences over a (small) window

$$f(x_s) = \int_{x_{min}}^{x_s} \underbrace{\mathbb{E}_{\mathbf{x}_c|z}}_{\text{realistic}} \underbrace{\left[ \frac{\partial f}{\partial x_s}(z, \mathbf{x}_c) \right]}_{\text{isolates}} \partial z$$

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<sup>2</sup>D. Apley and J. Zhu. “Visualizing the effects of predictor variables in black box supervised learning models.” *Journal of the Royal Statistical Society: Series B (Statistical Methodology)* 82.4 (2020): 1059-1086.

# ALE approximation

ALE definition:  $f(x_s) = \int_{x_{s,min}}^{x_s} \mathbb{E}_{\mathbf{x}_c|z} \left[ \frac{\partial f}{\partial x_s}(z, \mathbf{x}_c) \right] \partial z$

ALE approximation:  $f(x_s) = \underbrace{\sum_k^{k_x} \frac{1}{|S_k|} \sum_{i: \mathbf{x}^i \in S_k} \underbrace{[f(z_k, \mathbf{x}_c^i) - f(z_{k-1}, \mathbf{x}_c^i)]}_{\text{point effect}}}_{\text{bin effect}}$

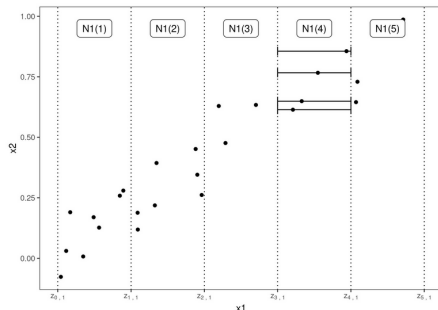


Figure: Image taken from Interpretable ML book (Molnar, 2022)

# ALE approximation - weaknesses

$$f(x_s) = \sum_k^{k_x} \underbrace{\frac{1}{|S_k|} \sum_{i: \mathbf{x}^i \in S_k} \underbrace{[f(z_k, \mathbf{x}_c^i) - f(z_{k-1}, \mathbf{x}_c^i)]}_{\text{point effect}}}_{\text{bin effect}}$$

- Point Effect  $\Rightarrow$  evaluation **at bin limits**
  - ▶ 2 evaluations of  $f$  per point  $\rightarrow$  slow
  - ▶ change bin limits, pay again  $2 * N$  evaluations of  $f \rightarrow$  restrictive
  - ▶ broad bins may create out of distribution (OOD) samples  $\rightarrow$  not-robust in wide bins

ALE approximation has some weaknesses

# Our proposal: Differential ALE

$$f(x_s) = \Delta x \sum_k^{k_x} \frac{1}{|S_k|} \sum_{i: x^i \in S_k} \underbrace{\left[ \frac{\partial f}{\partial x_s}(x_s^i, x_c^i) \right]}_{\text{point effect}}$$

bin effect

- Point Effect  $\Rightarrow$  evaluation **on instances**
  - ▶ Fast  $\rightarrow$  use of auto-differentiation, all derivatives in a single pass
  - ▶ Versatile  $\rightarrow$  point effects computed once, change bins without cost
  - ▶ Secure  $\rightarrow$  does not create artificial instances

For **differentiable** models, DALE resolves ALE weaknesses

# DALE is faster and versatile - theory

$$f(x_s) = \underbrace{\Delta x \sum_k \frac{1}{|S_k|} \sum_{i: \mathbf{x}^i \in S_k}}_{\text{bin effect}} \underbrace{\left[ \frac{\partial f}{\partial x_s}(\mathbf{x}_s^i, \mathbf{x}_c^i) \right]}_{\text{point effect}}$$

- Faster
  - ▶ gradients wrt all features  $\nabla_{\mathbf{x}} f(\mathbf{x}^i)$  in a single pass
  - ▶ auto-differentiation must be available (deep learning)
- Versatile
  - ▶ Change bin limits, with near zero computational cost

DALE is faster and allows redefining bin-limits



# DALE is faster and versatile - Experiments

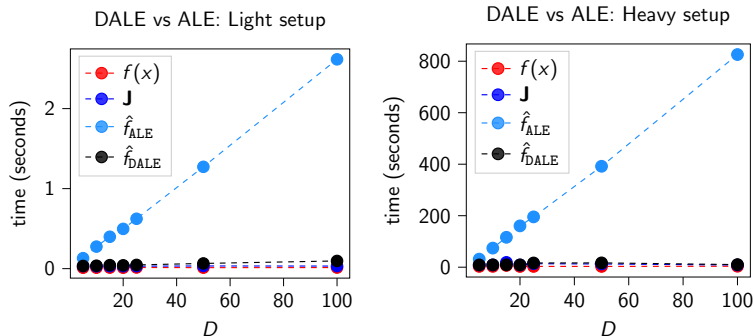


Figure: Light setup; small dataset ( $N = 10^2$  instances), light  $f$ . Heavy setup; big dataset ( $N = 10^5$  instances), heavy  $f$

DALE considerably accelerates the estimation

# DALE uses on-distribution samples - Theory

$$f(x_s) = \underbrace{\sum_k \frac{1}{|\mathcal{S}_k|} \sum_{i: \mathbf{x}^i \in \mathcal{S}_k} \underbrace{\left[ \frac{\partial f}{\partial x_s}(\mathbf{x}_s^i, \mathbf{x}_c^i) \right]}_{\text{point effect}}}_{\text{bin effect}}$$

- point effect **independent** of bin limits
  - ▶  $\frac{\partial f}{\partial x_s}(\mathbf{x}_s^i, \mathbf{x}_c^i)$  computed on real instances  $\mathbf{x}^i = (\mathbf{x}_s^i, \mathbf{x}_c^i)$
- bin limits affect only the **resolution** of the plot
  - ▶ wide bins  $\rightarrow$  low resolution plot, bin estimation from more points
  - ▶ narrow bins  $\rightarrow$  high resolution plot, bin estimation from less points

DALE enables wide bins without creating out of distribution instances

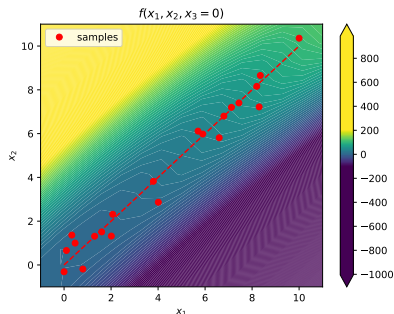
# DALE uses on-distribution samples - Experiments

$$f(x_1, x_2, x_3) = x_1 x_2 + x_1 x_3 \pm g(x)$$

$$x_1 \in [0, 10], x_2 \sim x_1 + \epsilon, x_3 \sim \mathcal{N}(0, \sigma^2)$$

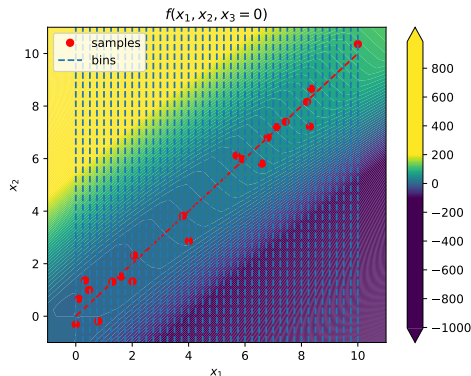
$$f_{\text{ALE}}(x_1) = \frac{x_1^2}{2}$$

- point effects affected by  $(x_1 x_3)$   
( $\sigma$  is large)
- bin estimation is noisy (samples are few)



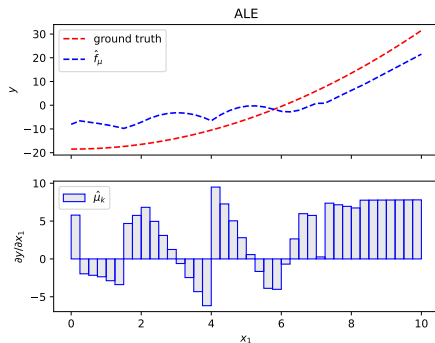
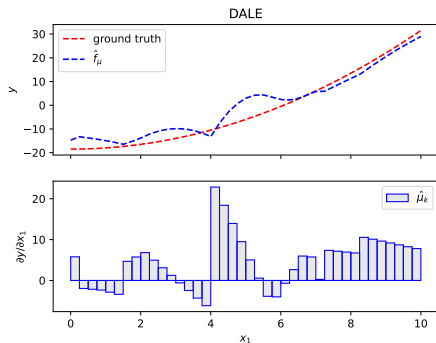
Intuition: we need wider bins (more samples per bin)

# DALE vs ALE - 40 Bins



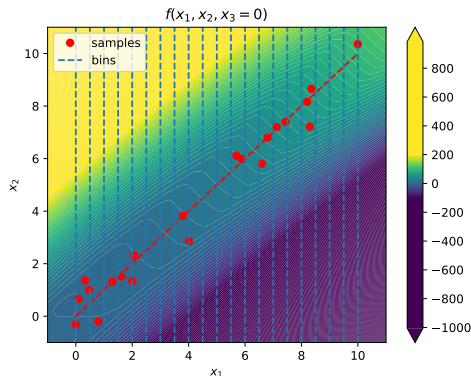
- DALE: on-distribution, noisy bin effect  $\rightarrow$  poor estimation
- ALE: on-distribution, noisy bin effect  $\rightarrow$  poor estimation

# DALE vs ALE - 40 Bins



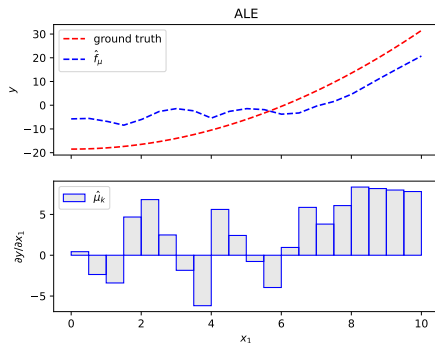
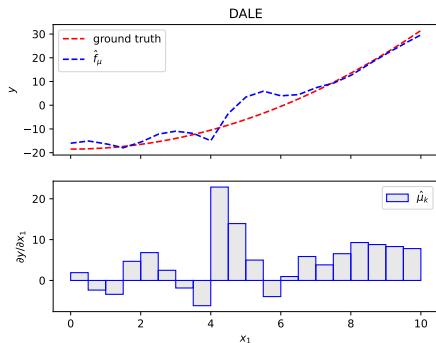
- DALE: on-distribution, noisy bin effect → poor estimation
- ALE: on-distribution, noisy bin effect → poor estimation

# DALE vs ALE - 20 Bins



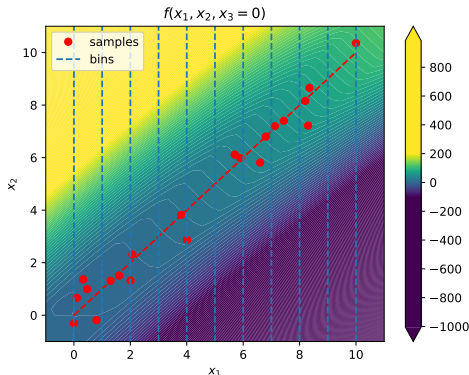
- DALE: on-distribution, noisy bin effect → poor estimation
- ALE: on-distribution, noisy bin effect → poor estimation

# DALE vs ALE - 20 Bins



- DALE: on-distribution, noisy bin effect → poor estimation
- ALE: on-distribution, noisy bin effect → poor estimation

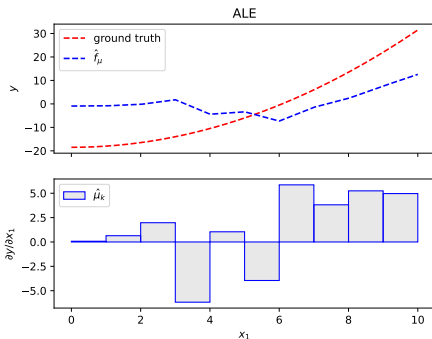
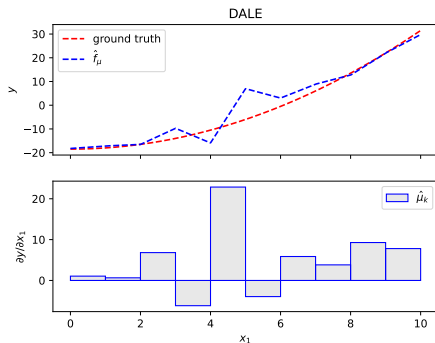
# DALE vs ALE - 10 Bins



- DALE: on-distribution, noisy bin effect → poor estimation
- ALE: starts being OOD, noisy bin effect → poor estimation

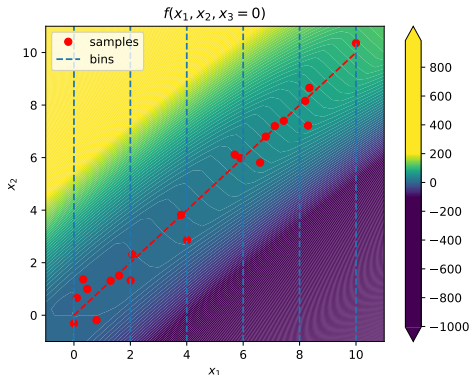


# DALE vs ALE - 10 Bins



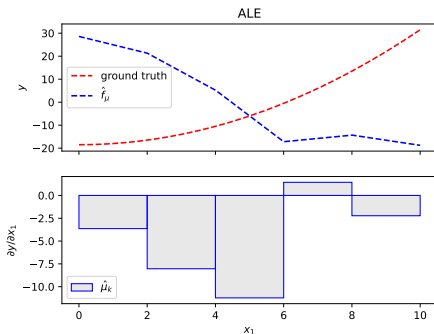
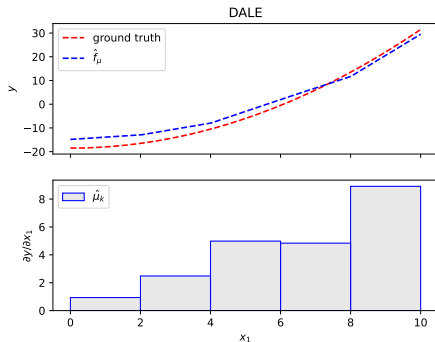
- DALE: on-distribution, noisy bin effect → poor estimation
- ALE: starts being OOD, noisy bin effect → poor estimation

# DALE vs ALE - 5 Bins



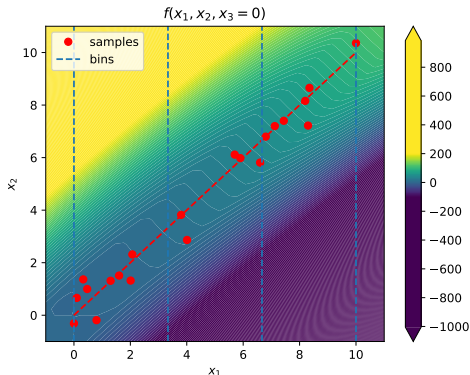
- DALE: on-distribution, robust bin effect → good estimation
- ALE: completely OOD, robust bin effect → poor estimation

# DALE vs ALE - 5 Bins



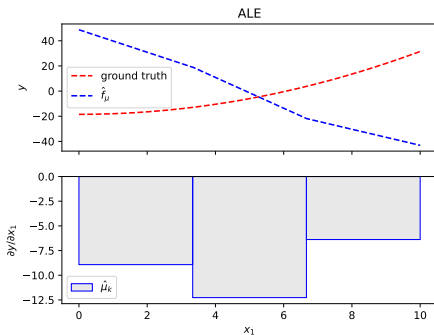
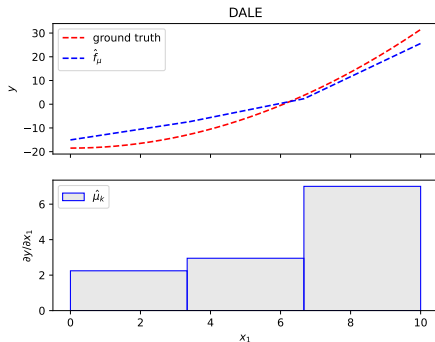
- DALE: on-distribution, robust bin effect → good estimation
- ALE: completely OOD, robust bin effect → poor estimation

# DALE vs ALE - 3 Bins



- DALE: on-distribution, robust bin effect → good estimation
- ALE: completely OOD, robust bin effect → poor estimation

# DALE vs ALE - 3 Bins



- DALE: on-distribution, robust bin effect → good estimation
- ALE: completely OOD, robust bin effect → poor estimation

# Real Dataset Experiments - Efficiency

- Bike-sharing dataset(Fanaee-T and Gama, 2013)
- $y \rightarrow$  daily bike rentals
- $x$  : 10 features, most of them characteristics of the weather

Efficiency on Bike-Sharing Dataset (Execution Times in seconds)

	Number of Features										
	1	2	3	4	5	6	7	8	9	10	11
DALE	1.17	<b>1.19</b>	<b>1.22</b>	<b>1.24</b>	<b>1.27</b>	<b>1.30</b>	<b>1.36</b>	<b>1.32</b>	<b>1.33</b>	<b>1.37</b>	<b>1.39</b>
ALE	<b>0.85</b>	1.78	2.69	3.66	4.64	5.64	6.85	7.73	8.86	9.9	10.9

DALE requires almost same time for all features

# Real Dataset Experiments - Accuracy

- Difficult to compare in real world datasets
- We do not know the ground-truth effect
- In most features, DALE and ALE agree.
- Only  $X_{\text{hour}}$  is an interesting feature

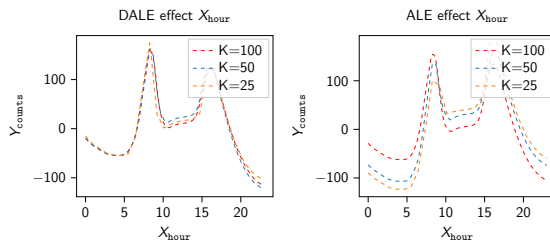


Figure: (Left) DALE (Left) and ALE (Right) plots for  $K = \{25, 50, 100\}$

# What next?

- Could we automatically decide the optimal bin sizes?
  - ▶ Sometimes narrow bins are ok
  - ▶ Sometimes wide bins are needed
- What about variable size bins?
- Model the uncertainty of the estimation?





DALE can be a driver for future work



# Thank you

- Questions?

# References I

-  Apley, Daniel W. and Jingyu Zhu (2020). “Visualizing the effects of predictor variables in black box supervised learning models”. In: *Journal of the Royal Statistical Society. Series B: Statistical Methodology* 82.4, pp. 1059–1086. ISSN: 14679868. DOI: [10.1111/rssb.12377](https://doi.org/10.1111/rssb.12377). arXiv: [1612.08468](https://arxiv.org/abs/1612.08468).
-  Fanaee-T, Hadi and Joao Gama (2013). “Event labeling combining ensemble detectors and background knowledge”. In: *Progress in Artificial Intelligence*, pp. 1–15. ISSN: 2192-6352. DOI: [10.1007/s13748-013-0040-3](https://doi.org/10.1007/s13748-013-0040-3). URL: [\[WebLink\]](#).
-  Friedman, Jerome H. (2001). “Greedy function approximation: A gradient boosting machine”. In: *Annals of Statistics* 29.5, pp. 1189–1232. ISSN: 00905364. DOI: [10.1214/aos/1013203451](https://doi.org/10.1214/aos/1013203451).
-  Molnar, Christoph (2022). *Interpretable Machine Learning. A Guide for Making Black Box Models Explainable*. 2nd ed. URL: <https://christophm.github.io/interpretable-ml-book>.