

Yijia Liu Assignment 1

1.

a.

$$T \sim N(2.5, 0.37^2)$$

$$P(T > 3) = 1 - F(3) = 1 - \text{pnorm}(3, \text{mean}=2.5, \text{sd}=0.37) = 0.08829$$

The probability is 8.829%.

b.

$$P(T \leq 2.5) = F(2.5) = \text{pnorm}(2.5, \text{mean}=2.5, \text{sd}=0.37) = 0.5$$

The probability is 50%.

c.

$$P(T \leq 2) = F(2) = \text{pnorm}(2, \text{mean}=2.5, \text{sd}=0.37) = 0.08829$$

The probability is 8.829%.

d.

$$P(T \leq x) = 0.99$$

$$\text{qnorm}(0.99, \text{mean}=2.5, \text{sd}=0.37) = 3.3607$$

The baseball game begins at 2 p.m., so it would end at 5:22 p.m. (approximately)

e.

$$LB = 2.5 - 1.96 * 0.37 = 1.7748$$

$$UB = 2.5 + 1.96 * 0.37 = 3.2252$$

The baseball game will end between 3:46 p.m. and 5:13 p.m. (approximately)

2.

a.

	Did Not Restate Earnings (Y=0)	Restate Earnings (Y=1)	Total
No IFE on board (X=0)	0.58	0.12	0.7
IFE on board (X=1)	0.27	0.03	0.3
Total	0.85	0.15	1.00

b.

X and Y are both discrete random variables and their distributions are Bernoulli.

c.

$$E(Y) = 0.85 \cdot 0 + 0.15 \cdot 1 = \underline{0.15}$$

It means the possibility that a firm restates its earnings is 15%.

d.

$$E(X) = 0 \cdot 0.7 + 1 \cdot 0.3 = \underline{0.3}$$

It means the possibility that a firm has IFE on board is 30%.

e.

For $E(Y|X=0)$:

$$P(Y=0|X=0) = P(Y=0, X=0)/P(X=0) = 0.58/0.7 = 0.828571429$$

$$P(Y=1|X=0) = P(Y=1, X=0)/P(X=0) = 0.12/0.7 = 0.171428571$$

$$E(Y|X=0) = 0 \cdot 0.828571429 + 1 \cdot 0.171428571 = \underline{0.17}$$

Meaning: If the firm has no IFE on board, the possibility of restating earnings is 17%.

For $E(Y|X=1)$:

$$P(Y=0|X=1) = P(Y=0, X=1)/P(X=1) = 0.27/0.3 = 0.9$$

$$P(Y=1|X=1) = P(Y=1, X=1)/P(X=1) = 0.03/0.3 = 0.1$$

$$E(Y|X=1) = 0 \cdot 0.9 + 1 \cdot 0.1 = \underline{0.1}$$

Meaning: If the firm has IFE on board, the possibility of restating earnings is 10%.

Having IFEs on board will make a firm less likely to restate earnings than having no IFEs.

f.

$$E(X=1|Y=1) = P(X=1, Y=1)/P(Y=1) = 0.03/0.15 = 0.2$$

The probability that it has an IFE on its board is 0.2.

$$E(X=1) = 0.3$$

If I did not know whether or not it had to restate its earnings, the probability will be 30%.

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g.

No, they are not independent.

$$P(X=1, Y=1) = 0.03$$

$$P(X=1) * P(Y=1) = 0.3 * 0.15 = 0.045$$

Because $P(X=1, Y=1)$ does not equal to $P(X=1) * P(Y=1)$, so they are not independent.