Defu: Set

A set is a collection of objects.

 $\{x, S = \{1, 2, 3\}$

N = {1,2,3,4,...} "natural numbers"

Q = { m/n: m, n are integers and n + 0}

Defn: Set Membership

We say that "x is in S" clensted

 $\chi \in S$

if S contains X as an element.

Ex. 5 e N

2/3 € Ø

2/3 & N _ read: not in

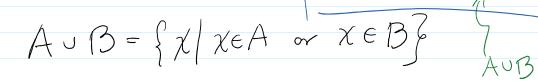
Defu! Containment

We say "A is a subset of B" denoted

We say it is a susset of U denoted
ACB
if x e A implies X e B.
Ex. 51,2,33 CN
QCR reduiser
N \$ 51,2,3) not a subsect
Defn: Set Equality
We say "A is equal to B" if
ACB and BCA
we write $A = B$.
Set Operations
Defn: Union
The union of A and B denoted
AUB

Lecture Notes Page 2

is defined as



$$\{ \underline{X}, A = N, B = \{ \pm 1, \pm 2, \pm 3, \dots \} \}$$

$$A \cup B = \{ \pm 1, \pm 2, \pm 3, \dots \}$$

$$EX$$
, $QUR = R$
 $b/c QCR$

Fact! If ACB then AUB = B.

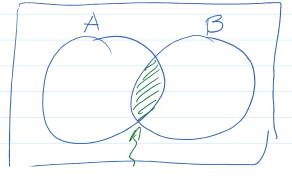
Fact! AUA = A

Defu: Intersection

The intersection of A and B cheroted

ANB or AB

is defined as



is defined as AB = {X | X EA and X EB} Ex, A = N $B = \{-1, -2, -3, \dots\}$ then AB = 8 Enoty set Ex. ON = IN b/c MCQ Fact: If ACB then AB = A. Fact: AA = A Defn: Set Difference We say the difference between A and B is defined as

A-B= {X/XEA and X \ B}

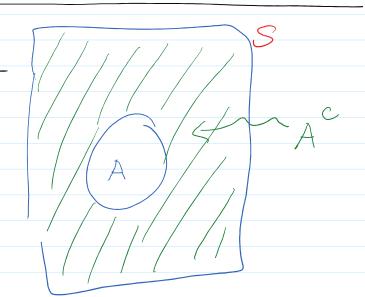
$$\frac{e_{X}}{B} = \{1, 2, 3\}$$

$$B = \{3, 4, 5\}$$
Here $A \setminus B = \{1, 2\}, B \setminus A = \{4, 5\}$

Defu: Complement

$$\frac{\text{Want:}}{A^{c} = \{ \chi | \chi \notin A \}}$$

Need: universe set S



ther
$$A^{c} = \{x \in S \mid x \notin A\} = S \setminus A$$

$$E_X$$
, $A = 51,23$, $S = N$
Nen $A^c = 53,4,5,6,...3$

Basic Theorems

- 2) Associativity , Au (Buc) = (AUB) UC A(BC) = (AB)C
- 3 Distributivity: A(BUC) = ABUAC AU(BC) = (AUB)(AUC)
- (2) (AB) = ACUBC

Countably Infinite Set Operations

Let A, Az, Az, ... be subsets of S

notation: (Ai) =

Defu! Countable Union

 $\bigcup_{i=1}^{\infty} A_i = \left\{ x \in S \mid x \in A_i \text{ for some } i \right\}$

$$ex$$
, let $S = (0, 1]$
and let $A_i = [/i, 1]$
 $A_i = [i], A_2 = [/2, 1], A_3 = [/3, 1]$

$$\bigcirc A_i = (0, 1]$$

Defu: Cantable Intersection

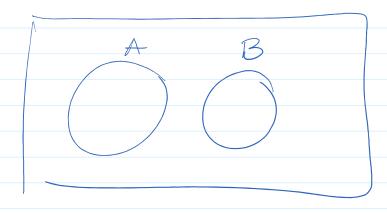
$$\bigcap_{i=1}^{\infty} A_i = \frac{2}{3} x \in S | x \in A_i \forall i$$

Ex, continue from above

$$\bigcap_{i=1}^{\infty} A_i = \{1\}$$

Defn: Disjoint

we say A and B are disjoint if AB=Ø



Defu: Pairwise Disjoint

A seg (Ai) is pairwise disjoint if

$$A_i A_j = \emptyset \quad \forall i \neq j$$

$$\mathcal{E}_{X}$$
 (f $A_i = [i, i+1)$
then $A_i A_j = \emptyset$

Defu: Partition

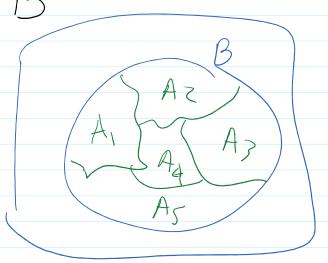
We say a seg (Ai) where Ai CB

L

are a partition of B

1) the Ai are disjoint

(2) UA; = B



Defu: Power Set

The permer set of a set A is the Collection of all subsets of A.

notation: P(A) or 2

Ex, A = \$1,23 then

$$2^{A} = \{\{1\}, \{2\}, A, \emptyset\}$$

Fact: |2 A = 2 |A|