Lecture 6: More Evaluation

Two reasons to evaluate:

1. get a measure of gen. perf.
2. model selection:
   e.g. choosing a tuning parameter
   → k in kNN
   → which covariates to include

Q: Can we use a test/train split (or X-validation) to do (2)?

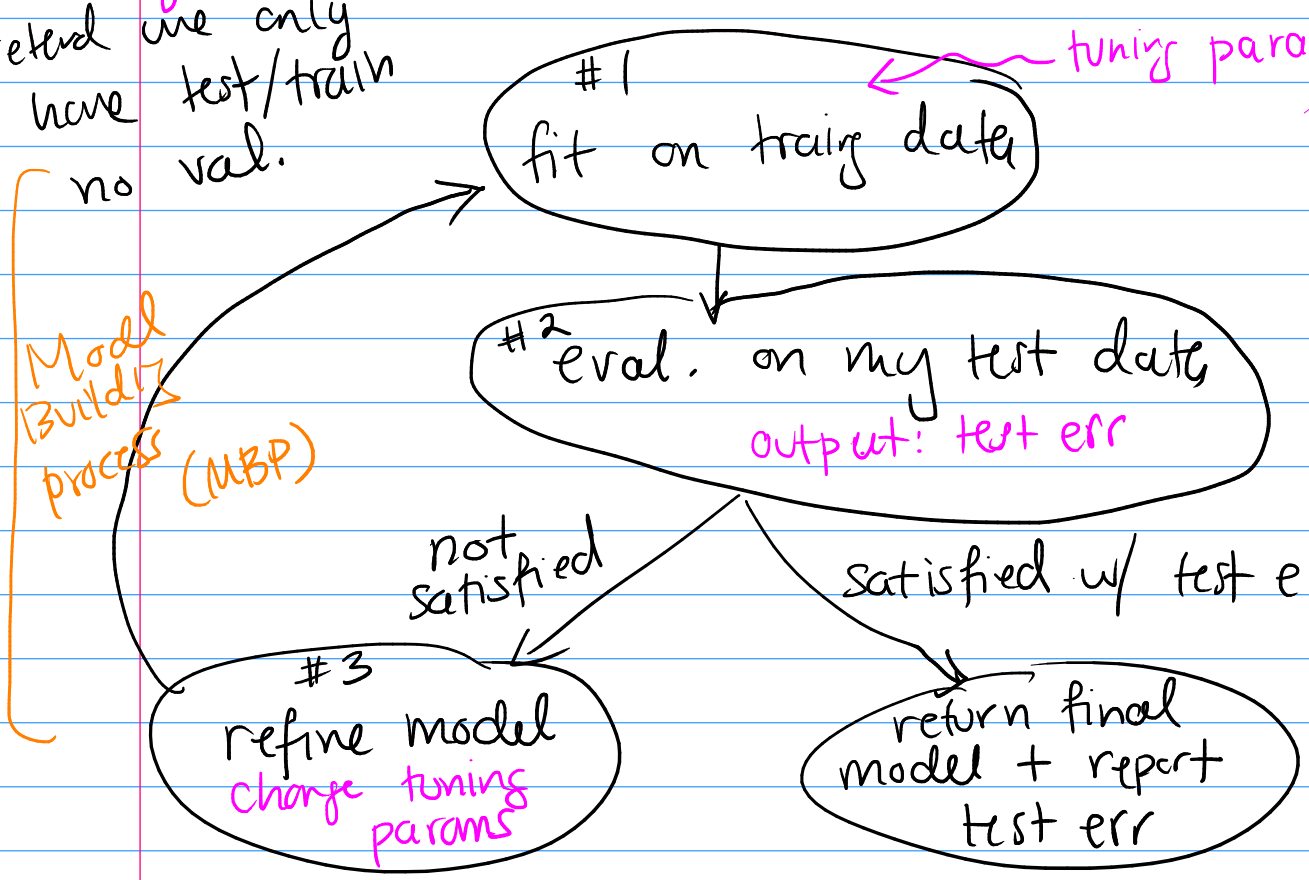
A: Yes, but we need to be careful.

Proper way to do this: split data into 3 datasets

1. training used to directly fit the model (e.g. min RSS)
2. validation used to select among my models (e.g. Choose k)
3. test to estimate gen. perf. of my final chosen model.

Why do we need sep. val/test?

Pretend we only have test/train no val.



Cardinal Sin: can't let my ML algo see the test data

Q: Did my model see the test data? After all, my algo only fit using the train data.

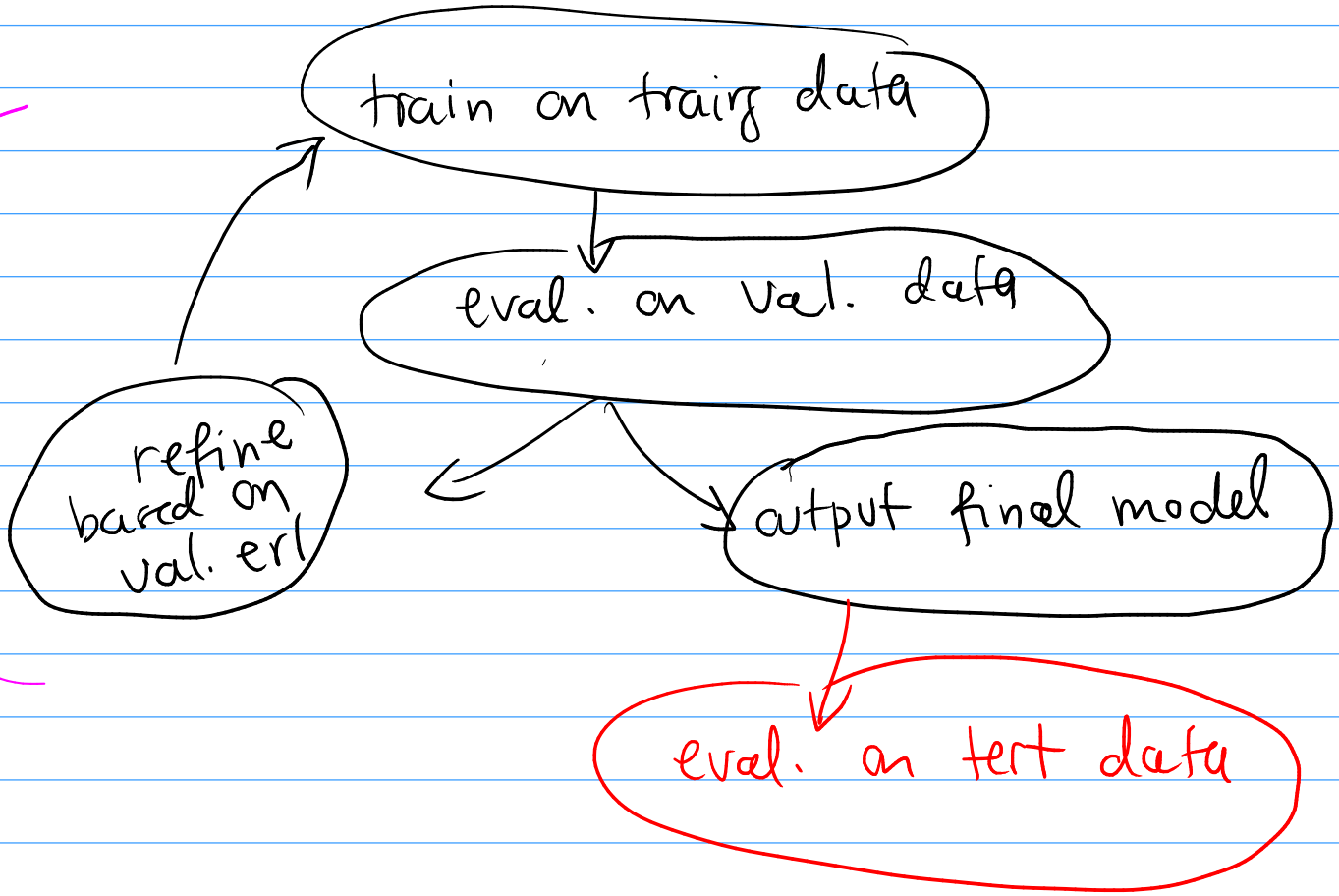
A: Yeah, kinda. By iteratively refing model based on test err. – the test data has influenced the MBP.

Still need a true "hold-out" dataset to est. gen. perf.

Consequently, we split into 3 datasets

1. train
2. val.
3. test

} used to build/choose model.



Ex. Choosing k for kNN

Split data into train val., test

MBP

For k in seq of ks

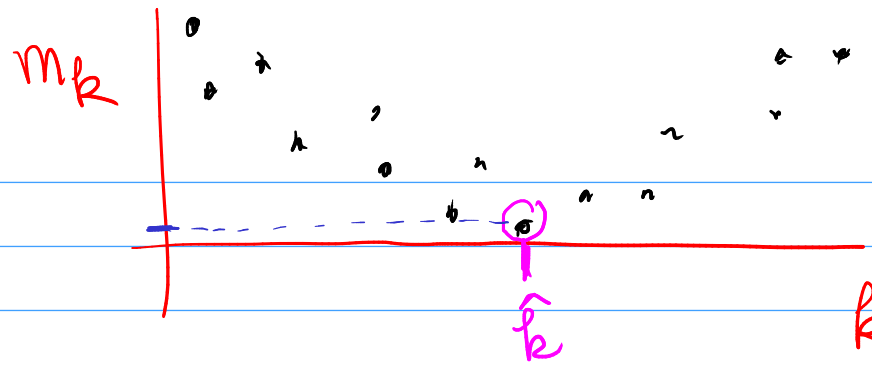
→ train on training data using k neighbors

→ eval. on val. data

m_k = RMSE of val. preds

END FOR

$\hat{k} = \underset{k}{\text{argmin}}\ m_k$ = i.e. val. of k that produces min m_k



THEN to est. my gen. perf. I fit kNN using $\hat{k}$ neighbors on combined train/val

and then eval. on my testing data.

Can we do this in a x-validated way?

Called: nested cross validation

Split data into I folds

For $i = 1, \ldots, I$

→ hold out fold i for testing

→ use other folds for train-val

→ split train-val into J folds

For $j = 1, \ldots, J$

→ hold out fold j as val. data

→ use other folds as traing data

For k in seq of ks

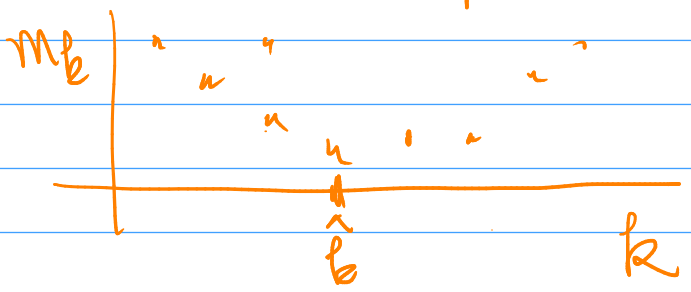
→ fit kNN usig train and k neighbors

→ evd on val

$m_k^{(j)}$ = RMSE on val.

→ $m_k = \text{mean}(m_k^{(j)})$

→ choose $\hat{k} = \underset{k}{\text{argmin}}\ m_k$



→ fit model w/ $\hat{k}$ on train-val

→ eval ony my test data

M_i = RMSE of $\hat{k}$ model on test

So after all of this I have

$M_1, \ldots, M_I$

So e.g. gen. perf. might be mean(M_i)