

The Effects of Visual and Design Features on the Perception of Correlation in Scatterplots

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Abstract

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Lay abstract

This is lay abstract text.

Declaration of originality

I hereby confirm that no portion of the work referred to in the thesis has been submitted in support of an application for another degree or qualification of this or any other university or other institute of learning.

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Acknowledgements

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Chapter 1

Introduction

1.1 Research Motivation

1.2 Contributions

1.3 Included Publications

The research described in chapters 4, 5, 6, and 7 in this thesis is adapted from earlier publications, the last of which under review as of writing. To avoid repetition, information and discussion that would be repeated has been consolidated into the literature review and general methodology chapters. *Gabriel Strain* is the primary author of all included papers.

- *The Effects of Contrast on Correlation Perception in Scatterplots* [50] is reproduced in Chapter 4. Sections 4.5.2, 4.6.2, 4.5.3, 4.6.3, 4.5.4, 4.6.4, and 4.7 contain minimally altered parts of the published article.
- *Adjusting Point Size to Facilitate More Accurate Correlation Perception in Scatterplots* [49] is reproduced in Chapter 5. Sections 5.4.2, 5.4.3, 5.4.4, and 5.5 contain minimally altered parts of the published article.
- *Effects of Point Size and Opacity Adjustments in Scatterplots* [51] is reproduced in Chapter 6. Sections 6.4.2, 6.4.3, 6.4.4, and 6.5 contain minimally altered parts of the published article.
- *Effects of Alternative Scatterplot Designs on Belief (under review)* is reproduced in Chapter 7. Sections 7.4, 7.5.2, 7.5.3, 7.5.4, and 7.6 contain minimally altered parts of the published article.

1.4 Overview of Thesis

Chapter 2

Literature Review

2.1 Data Visualisation: A Brief History

2.2 Measuring Relatedness

2.3 Conceptions of Correlation

2.4 Visualising Correlation

2.4.1 History

2.4.2 Present Landscape

2.4.3 Scatterplots

2.5 Correlation Perception

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2.7 Underestimation: What's Really Going On?

2.8 Underestimation: Potential Consequences

2.9 Data Visualisation Literacy

2.10 Objectives and Contributions

Chapter 3

General Methodology

3.1 Introduction

In this chapter I describe our research methodologies. The experiments described in chapters 4, 5, and 6 share most aspects of experimental method, and are therefore described in full in this chapter. Chapter 7 features a different methodology, and is described therein. This chapter discusses experimental designs, the tools used to build and run the experiments, the approach to statistical analyses, and the computational methods and practices employed, particularly with regards to reproducibility and open science.

3.2 Experimental Methods

It is important to acknowledge that the way in which we conduct experiments influences what research questions we can ask and the conclusions that we may draw. The decisions that lead us to designing experiments in certain ways must be based not only on theory, but also on the practical constraints imposed by external factors on the research team. Concerns such as time, practicality, and cost must be addressed, and a compromise between research that is *valuable* and research that is *doable* must be reached.

We focused on pragmatism and impact throughout the course of this research project; happily, the research journey we embarked on resulted in methodologies that satisfied both principles. It is for this reason that we consider the framework we present to be a key contribution of this thesis.[a]

3.2.1 Experimental Design

All but the final experiment utilised within-participants designs. In such a design, each participant is exposed to each level of the intervention. This is in contrast with between-participants designs, where separate groups are exposed to only a single level of the intervention each. Where possible, within-participants designs are preferred. These designs do not rely on random allocation, and as each participant is able to provide as many data points as there are levels [15], offer a significant boost in statistical power over between-participant designs where each participant only provides a single data point. In experiments 1 to 3, each participant saw all experimental stimuli and provided a judgement of correlation using a sliding scale between 0 and 1 (see Figure 3.1). Experiment 1 featured a single factor

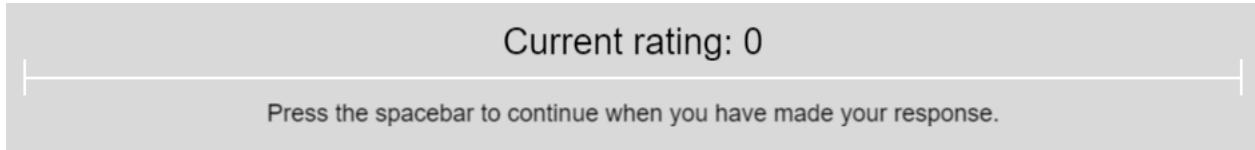


Figure 3.1. An example of the slider participants used to estimate correlation in experiments 1-4.

of global scatterplot point opacity with 4 levels (see [?@fig-exp1-examples](#)). Experiment 2 featured a single factor of scatterplot point design regarding opacity with 4 levels (see [?@fig-exp2-examples](#)). Experiment 3 featured a single factor of scatterplot point design regarding size with 4 levels (see [?@fig-exp3-examples](#)). Experiment 4 featured a factorial 2×2 design; IV1 was the scatterplot point opacity design used with 2 levels, and IV2 was the scatterplot point size design used with 2 levels (see [?@fig-exp4-examples](#)). Experiment 5 is a departure from the shared experimental paradigm of the previous experiments, and features a 1 factor, 2 level between-participants design.

3.2.2 Tools for Testing

However we design experiments, software plays a crucial role in allowing us to carry them out. Fortunately, there is a wealth of tools available to facilitate the testing of visualisations both in traditional lab-based tests and in online experiments. Following the principles of open and reproducible research [6], closed-source software, such as Gorilla [4] or E-prime [19] was discounted, as these rely on paid licences and do not allow for the sharing of code with future researchers. I settled on using PsychoPy [38] due to its open-source status, flexibility regarding graphical and code-based experimental design, and high level of timings accuracy [11]. Using such a open-source tool not only facilitated my own learning with regard to experiment building, but also enables the contribution of further examples of visualisation studies by hosting the resulting experiments online for use and modification by future researchers.

I elected to pursue online testing throughout this thesis. Doing so is much quicker than carrying out in-person lab-based testing, facilitating the collection of data from a much larger number of participants. This reduces the chances of detecting false positives during analysis and ensures adequate levels of power despite the potential for small effects sizes (see Section 3.2.3). Online testing also affords access to diverse groups of participants across our populations of interest, especially when compared to the relatively homogeneous student populations usually accessed by doctoral researchers. Research has identified online experimentation as producing reliable results that closely match those found in traditional lab-based experiments [5, 20, 42], especially with large sample sizes. Due to its integration with PsychoPy, Pavlovia was used to host all the experiments described in this thesis. Section 3.5.4 contains links to all experiments publicly hosted on Pavlovia's GitLab instance.

3.2.3 Recruitment & Participants

Recruitment of participants online is possible through a range of service providers, each with advantages and disadvantages. Research evaluating a number of these providers recently found that Prolific [43] and CloudResearch provide the highest quality data for the lowest cost [18]; I elected to use the

former due to my familiarity with the system. Despite these findings, there has also been evidence of low data quality and skewed demographics affecting even high quality platforms tailored towards academic research. On the 24th of July, 2021, the Prolific.co platform went viral on social media [14], leading to a participant pool heavily skewed towards young people identifying as female. At the time, Prolific did not manually balance the participants recruited for a study. This was addressed in the pilot study (see Section 4.2) by preventing participants who joined after this date from participating, in addition to manually requesting a 1:1 ratio of male to female participants. The demographic issues settled quickly, however the screened 1:1 ratio was maintained for the remainder of the experiments.

The first experiment conducted was a pilot study (see Section 4.2 for full details) investigating a very early iteration of the point opacity manipulation in combination with exploratory work around plot size and correlation estimation. At the time, I was relatively naive to the intricacies of recruiting research participants online, and thus experienced issues regarding participant engagement. Each experiment included attention check questions in which participants were instructed to ignore the stimulus and provide a specific answer. The advert for each experiment stated that failure of more than 2 attention check items would result in a submission being rejected. This pilot study suffered from a rejection rate of 57.5%, indicating very low levels of participant engagement. For the following studies, published guidelines [37] were followed to address these issues; specifically, it was required that participants:

- Had previously completed at least 100 studies on Prolific.
- Had an acceptance rate of at least 99% for those studies.¹

Following implementation of these pre-screen criteria, the rejection rate for the next experiment fell to ~5%. Rejection rates were similar for the remainder of experiments. Exact numbers of accepted and rejected participants can be found in the **Participants** sections of each experiment.

Each experiment recruited until 150 participants had completed successfully. Due to the novelty of this work, it was difficult to get a sense of the size of the effect that would be seen. I assumed a small effect size (Cohen's $d \sim 0.2$), and aimed to recruit enough participants that the experiments would be adequately powered [13]. NB: I did not conduct an *a priori* power analysis. A post-hoc power analysis of the first experiment revealed a power of 0.54. Effect sizes were larger in the subsequent experiments, however to facilitate comparison, it was decided that $n = 150$ would remain the target recruitment rate.

3.2.4 Creating Stimuli

All stimuli were created using ggplot2 in R. Specific versions are cited separately with regard to the specific visualisations produced for each experiment. Identical principles were followed regarding data visualisation design for each experiment bar the last, which is discussed *in situ*.

Experiments were designed with the intention of isolating and addressing a perceptual effect; the underestimation of correlation in positively correlated scatterplots. To achieve this, confounding extraneous design factors were removed, including axis labels, tick labels, grid lines, and titles. The axis

¹this is a more strict rate than the 95% recommended by Peer et al. [37].

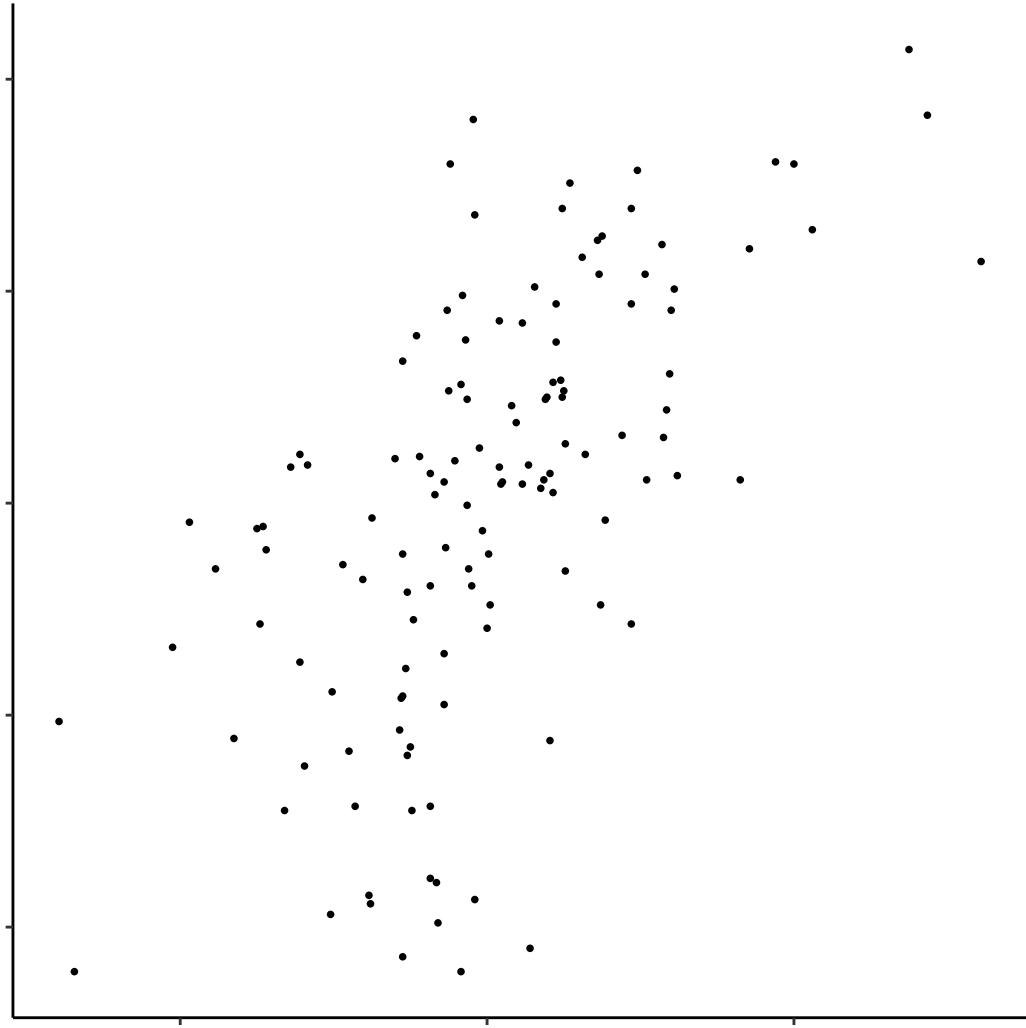


Figure 3.2. The basic design of scatterplots in experiments 1 to 4.

ticks themselves were preserved. Figure 3.2 demonstrates the basic design of the scatterplots used in experiments 1 to 4.

3.3 Analytical Methods

To investigate whether the experimental manipulations have actual effects on the interpretations participants provide, appropriate statistical testing must be employed. This involves taking into account the variability in responses that can be attributed to an experimental manipulation against the backdrop of other variability inherent in the dataset. Traditional analysis of the data collected throughout this thesis would involve the use of repeated measures analyses of variance (ANOVAs). This technique assesses whether there are significant differences in means of dependent variables between conditions. While these techniques are commonplace, they do not allow for comparisons of differences across the full range of individual participant responses, nor do they allow for simultaneous consideration of by-item and by-participant variance. It is for these reasons that linear mixed-effects models were used throughout. Linear mixed-effects modelling is a reliable approach that is resistant to a variety of distributional assumption violations [47], and facilitates the appreciation of the data story in a broader and more detailed fashion.

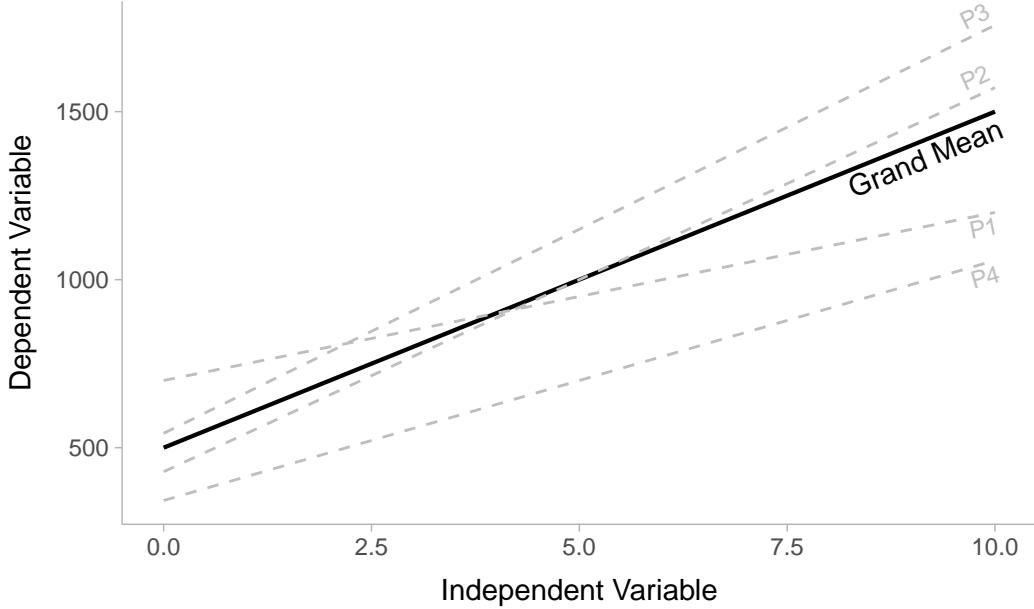


Figure 3.3. Visualising random intercepts and slopes for a theoretical experiment with 4 participants. The grand mean of the dependent variable is shown as a solid line, while each separate random intercept is drawn with dashed lines. Each line has a different gradient, representing different random slopes for each participant. This graphic was inspired by those featured in Brown, 2021 [12].

3.3.1 Linear Mixed-Effects Models

In a mixed-effects modelling paradigm, a distinction is made between variability that is thought to arise as a result of an experimental manipulation (fixed effects), and that which arises due to differences between, for example, participants or particular experimental items (random effects). When a variable is manipulated by a researcher in an experiment, each level of that variable is present, meaning it is appropriate to be modelled as a fixed effect. When only a *subset* of levels of a variable is present, such as a sample of all possible participants or experimental items, then this variable is appropriate for modelling as a random effect. Typically, mixed-effects models require the specification of *intercepts*; these are different baselines for each participant or item that reflect random deviations from the mean of the dependent variable. Mixed-effects models may also specify random *slopes*; these are differences in the magnitude of the difference between levels of the independent variable for each random effect [12]. Figure 3.3 visualises these concepts.

Throughout the course of this thesis, analyses attempt to model both random intercepts and slopes in order to capture the maximum amount of variability present in our datasets. In order to ascertain the goodness-of-fit of models, their ability to explain variance is compared to that of a nested null model [48]; such a model is identical bar the removal of the fixed effect of interest. The likelihood ratio test (LRT) is used here to assess goodness-of-fit. In cases where a model has in total more than two levels (here, all experiments bar experiment 5), the `emmeans` package [26] is used to calculate estimated marginal means between levels of fixed effects.

3.3.2 Ordinal Modelling

In experiment 5, participants used Likert scales to provide responses. These scales capture whether one rating is higher or lower than another, however they do not quantify the magnitude of the difference between levels of rating. Metric modelling, such as linear regression, treats the response options to a Likert scale as if they were numeric. Doing so assumes equal levels of difference between ratings, when in reality there is no theoretical reason to assume so. Metric modelling is therefore considered inappropriate for modelling responses to Likert scales [27]. In light of these issues, the `ordinal` package [16] in R was used to build cumulative link mixed effects models for the analysis of Likert scale data. This allows for the treatment of Likert responses as ordered factors as opposed to continuous response scales.

3.3.3 Model Construction

Choices are inherent in every type of statistical analysis, and can play a large role in the conclusions that are drawn from them. In linear mixed-effects modelling, deciding *what* is a fixed or random effect is straightforward; deciding *how to specify* random effects is a more complicated matter. Barr et al. [7] argue that for fully repeated measures designs, we should prefer a maximal model; one with random intercepts and slopes for each participant and experimental item. More recently, Bates et al. [8] have argued that attempting to specify maximal models for insufficiently rich datasets may lead to overfitting and unreliable conclusions. In light of this I sought a more systematic approach to selecting the random effects structure of a given model.

In an attempt to balance simplicity, explanatory power, and model convergence (whether or not a solution can be found), the `buildmer` package [54] in R was used to automate the selection of model specifications. Having been provided with a maximal model, `buildmer` uses stepwise regression to select the most complex model structure that successfully converges. Following this, random effects terms that fail to explain a significant amount of variance in the dataset are dropped; this stepwise elimination of terms is evaluated using successive likelihood ratio tests. This results in a model that captures the maximal amount of feasible variability while minimising redundancy. Note that `buildmer` was not relied upon as a modelling *panacea*; models are still based on theoretical underpinnings and are evaluated critically.

3.3.4 Effects Sizes

My approach to effects sizes evolved throughout the course of the research project due to reviewer feedback and a growing appreciation of the complexities of effect sizes when discussing linear mixed-effects models. Experiments 1, 2, and 3 featured a condition with no scatterplot manipulation present (henceforth referred to as a *baseline*); accordingly, the `EMAtools` package [23] was used to calculate equivalent Cohen's d effect sizes of manipulation-present conditions relative to the baseline. Experiment 4 did not feature a baseline condition, meaning Cohen's d was deemed inappropriate. The `r2glmm` package [22] was used instead to calculate semi-partial R^2 . In lieu of a traditional measure of

effect size, this demonstrated the unique variance in the dependent variable explained by each level of the independent [33]. Experiment 5 features a much simpler modelling situation, and returns to providing equivalent Cohen's d values for the pre- vs post- plot viewing conditions, this time calculated by converting odds ratios using the `effectsize` package [9]. More details on specific calculations, measures, and conclusions can be found *in situ*.

3.3.5 Reporting Analyses

Throughout this thesis, a broad approach to the reporting of statistical analyses was taken; while I consider our analytical methods and conclusions valid, I also present a range of statistics to allow the reader to draw their own conclusions should they wish. Statistical results are visualised where appropriate, and where visualisation aids understanding and interpretation. In addition, details about model structures and the issues we tackled when modelling are included for transparency [31].

3.4 Computational Methods

The approach to computational methods in this thesis sought to marry practicality, simplicity, and reproducibility. Often, this meant that what would otherwise be a makeshift script followed by copy-pasting of results into Overleaf ended up being an involved exercise in literate programming (knuth ref) and code wrangling. This involved effort and time, particularly in the early stages of the project, however has yielded a number of benefits. Many of the techniques developed early in the project proved to be instrumental later on, resulting in time-savings overall. Additionally, these techniques, principles, and practices are shared to enable future researchers to learn, where I struggled. In this section, we detail our approaches to computational methods, including how the idea of **executable papers** was utilised, and how containerised environments were used to capture a freeze-frame of the analyses.

3.4.1 Executable Reporting

Each paper published throughout this project, and this thesis, has been written to be executable. Packaging research in such a way means a lay person can follow simple instructions to recreate the work, while also facilitating and encouraging literate programming, or the close alignment of documentation and underlying code [41].

The use of a literate programming paradigm to generate reports (usually using LaTeX) has a rich history. This section focuses on this history as it pertains to the language used throughout this project, R.Sweave [25], written in 2002, allowed R code to be integrated into LaTeX documents. This was followed by Yihui Xie's knitr [56], which expanded Sweave functionality and improved integration with tools such as pandoc [29]. knitr uses Rmarkdown [57] to mix markdown-flavoured text with code chunks into a document that can be rendered into an appropriately-formatted conference or journal pdf; this workflow was used for the paper associated with experiments 1 and 2. Quarto [2], released

in 2022, further expands on Rmarkdown functionality, and removes reliance on R or Rstudio. Quarto was used for the remainder of the papers associated with this project, and for the present thesis.

Writing executable or dynamic documents allows results to be re-generated whenever the document is rendered. This includes any associated data visualisations and statistical modelling. Structuring documents like this effectively “open up” research by allowing others to view the code that performed the analysis and generated the data visualisations, in addition to guarding against accusations of questionable research practices through high levels of transparency [21]. This paradigm also allows for the caching of computationally expensive statistical models.

3.4.2 Containerised Environments

Providing the code associated with a project, even when that code is integrated into a literately programmed executable paper, is necessary, but not sufficient, for enabling adequate reproducibility. Previous work has found many instances where publicly-accessible code could not reproduce the results included in the corresponding document or failed to run entirely [17, 45, 53]. Poor programming practices accounted for a significant portion of these problems, highlighting the issue of researchers without technical backgrounds being expected to produce high quality technical documentation. Elsewhere, differences in computational environment, package versions, and operating systems have been identified as responsible for the non-replication of results. Large research projects, such as this, can include hundreds of functions from scores of packages, meaning that small changes can critically break code.

These issues were addressed using containers, specifically, those created by Docker [10, 30]. 1979 saw the development of chroot (change root), which is able to isolate an application’s file access to a ‘chroot jail’. Since then, we have seen the rapid development and uptake of containerisation software, mostly within the software development and security communities. Docker, released in 2014, is a popular, lightweight containerisation tool that enables a precise recreation of computational environments. Recording software versions and dependencies avoids the potential for broken code in the future, and publicly hosting papers as GitHub repositories that build into Docker containers ensures that future researchers can interact with code and data in the same computational environment used when carrying out the research.[b]

3.5 Reproducibility In This Thesis

Reproducibility is a broad spectrum [40] (see Figure 3.4). As discussed above, even when code and data are provided, results are often not replicable, and this is before issues around poor research practice, inappropriate analysis, and dishonest science even rear their heads. While for most, the reproducibility crisis [34] crystallised in the early 2010s [39], concerns had been voiced since at least the late 1960s [44]. Since coming into the wider academic conscious, numerous studies have identified reasons for the crisis, ranging from poor practice (e.g Potti et al., 2006 [1]) to outright deception and fabrication (e.g the Woo-Suk Hwang scandal [46]). These issues led this project to strive for a gold standard [40]

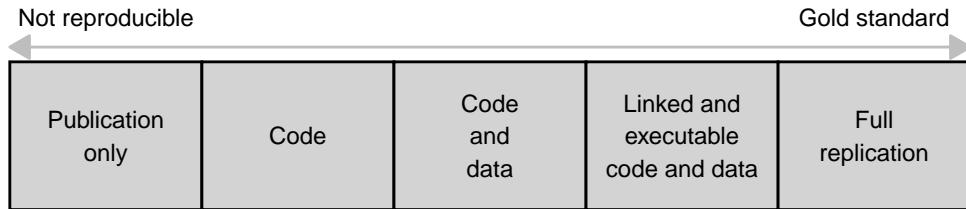


Figure 3.4. Peng’s (2011) Reproducibility Spectrum. This figure has been reproduced from Peng (2011) [40].

of reproducibility throughout. In this section, I detail how this was accomplished, and in doing so, expose my work to welcome critique.

3.5.1 Sharing Data and Code

The open and public sharing of data and code facilitates external assessment [3, 24], secondary use of data [52], and guards against reproducibility issues [32]. Quite aside from external motivating factors, I found that developing and embedding the reproducibility practices described here have resulted in longer term savings in time and effort. Favouring a gold-standard reproducible approach is also a way of “paying it forward”; having come from a non-technical background, I found previous work that adhered to the same standard critical to learning and development. GitHub is used to host both this thesis and the papers associated with the project; links to these repositories can be found throughout.[c]

3.5.2 Executable Papers and Docker Containers

As detailed above, Quarto and Docker were used to produce executable journal/conference papers for each of the published works this thesis describes. For simplicity, all analyses from these papers have been repeated using up to date packages here. Accordingly, a single implementation of Docker to is provided to reproduce this thesis. All statistics have been checked against those provided in the original analyses, and repositories for the corresponding papers are provided complete with separate Docker implementations.[d]

3.5.3 Pre-Registration of Hypotheses and Analysis Plans

Often touted as a low-cost entry point into reproducible research practices [28], pre-registration is the practice of clarifying hypotheses and analysis plans prior to data collection. While this may not be able to prevent research fraud and QRPs entirely, it does lend credibility to the researcher [36]. All hypotheses and analysis plans were pre-registered with the Open Science Framework [35]. Pre-registrations are embargoed[e], and deviations from registered analysis plans are detailed in the methods sections of the corresponding experiments.

3.5.4 Experimental Resources

Everything needed to run each experiment is included in the corresponding GitLab repository. Links to these repositories are also provided in the sections concerning each experiment.

Chapter 4

Experiment 1: https://gitlab.pavlovia.org/Strain/exp_uniform_adjustments

Experiment 2: https://gitlab.pavlovia.org/Strain/exp_spatially_dependent

Chapter 5

Experiment 3: https://gitlab.pavlovia.org/Strain/exp_size_only

Chapter 6

Experiment 4: https://gitlab.pavlovia.org/Strain/size_and_opacity_additive_exp

Chapter 7

Experiment 5 Pre-Study: https://gitlab.pavlovia.org/Strain/beliefs_scatterplots_pretest

Experiment 5 Main Study (Group A): https://gitlab.pavlovia.org/Strain/atypical_scatterplots_main_a

Experiment 5 Main Study (Group B): https://gitlab.pavlovia.org/Strain/atypical_scatterplots_main_t

3.6 Conclusion

In this chapter, I have established the broad methodological approach taken by this thesis. This project sought to investigate novel ways of visualising data and their effects on perception and cognition. I have provided justifications for the designs used, the methodological challenges faced, and how the use of a broad array of tools and techniques was able to overcome these challenges. Throughout, I have detailed how I have learnt from my mistakes. Open research and reproducibility is at the core of the work described here, and I hope this thesis can serve as an example for future work facing similar challenges and with similar commitments to open science. To this end, I have produced a template to facilitate future reproducible theses. We satisfy FAIR (Findable, Accessible, Interoperable, and Reusable) data principles [55] through public sharing of data and code, literate programming, and containerisation,

[a]I'm not sure this is needed [b]More about how Docker works would help here [c]sharing is no good without the appropriate license - maybe add a brief section of the different licenses here [d]do you talk about your Dockerfiles later? If not, this might be a good place to describe how a Dockerfile is constructed, and how yours are built - you can explain the critical lines that are common across all your Dockerfiles [e]are they always? for how long?

Chapter 4

Adjusting the Opacities of Scatterplot Points Can Affect Correlation Estimates

4.1 Abstract

4.2 Preface: Learning From an Early Pilot Study

4.3 Introduction

4.3.1 Overview

4.4 Related Work

4.4.1 Transparency, Contrast, Opacity, and Formal Definitions

4.4.2 Effects of Point Opacity on Correlation Estimation

4.5 Experiment 1: Uniform Opacity Adjustments

4.5.1 Introduction

4.5.2 Methods

4.5.3 Analysis

4.5.4 Discussion

4.6 Experiment 2: Spatially-Dependent Opacity Adjustments

4.6.1 Introduction

4.6.2 Methods

4.6.3 Analysis

Chapter 5

Adjusting the Sizes of Scatterplot Points Can Correct for a Historic Correlation Underestimation Bias

5.1 Abstract

5.2 Overview

5.3 Related Work

5.3.1 Size and Perception

5.3.2 Scatterplot Point Size and Correlation Perception

5.4 Experiment: Adjusting Point Size to Facilitate More Accurate Correlation Perception in Scatterplots

5.4.1 Introduction

5.4.2 Methods

5.4.3 Analysis

5.4.4 Discussion

5.5 General Discussion

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Interactions of Opacity and Size Adjustments

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6.2 Overview

6.3 Related Work

6.3.1 Size and Opacity

6.4 Experiment: Adjusting Point Size and Opacity Together

6.4.1 Introduction

6.4.2 Methods

6.4.3 Analysis

6.4.4 Discussion

6.5 General Discussion

Chapter 7

Visual Features Affecting Perceptual Estimates Also Affect Beliefs About Correlations

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7.2 Overview

7.3 Related Work

7.3.1 From Perception to Cognition

7.3.2 From Cognition to Belief

7.4 Pre-Study: Investigating Beliefs About Relatedness Statements

7.4.1 Introduction

7.4.2 Methods

7.4.3 Analysis

7.4.4 Discussion

7.5 Experiment: Potential for Belief Change Using Atypical Scatterplots

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7.5.2 Methods

7.5.3 Analysis

7.5.4 Discussion

Chapter 8

Conclusion

8.1 Main Findings

8.2 Relationship to Prior Work

8.3 Reproducibility

8.4 Contributions

8.5 Implications

8.5.1 For Design

8.5.2 For Society

8.6 Limitations

8.7 Future Directions

8.8 Closing Remarks

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Appendices

Appendix A

First appendix

A.1 Section in Appendix