580.422 System Bioengineering II: Neurosciences (Spring 2015)

Recitation #3 Review Questions

February 12th, 2015

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Question	
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Calcium ions are	removed from the c	ytoplasm b	V

- 1) Calcium channels
- 2) ATP-dependent active transport.
- 3) SERCA pumps into the endoplasmic reticulum.
- 4) All the above.
- 5) (1) and (2) above.
- 6) (2) and (3) above.

Question 2

Inhibitory synapses usually contain a chloride channel. However, sometimes synaptic activation can lead to inhibition or excitation through the gating of potassium by a metabotropic mechanism. Give a possible sequence of steps for such a mechanism. (4 pts)

Question 3

Part a)

To model bursting in neurons, we used a modified HH model in which a calcium-dependent potassium channel *KCa* was added to the system, giving the set of differential equations below.

$$C\frac{dV}{dt} = I_{ext} - G_K(V - E_K) - G_{KCa}(V - E_{KCa}) - G_{Ca}m_{\infty}(V)(V - E_{Ca}) - G_L(V - E_L)$$

$$\frac{dw}{dt} = \frac{w_{\infty}(V) - w}{\tau_w(V)}$$

$$G_K = \bar{G}_K w$$

$$\frac{dCa}{dt} = A\left(-\frac{ICa}{2F} - B * Ca\right)$$

$$G_{KCa} = \bar{G}_{KCa}\frac{Ca}{Ca+1}$$

In this model, bursting is terminated by the increase in the conductance of the *KCa* channel as *Ca* accumulates. There is some evidence that voltage or Ca-dependent inactivation of the calcium channel participates in burst termination. Suppose that there is no *KCa* channel in the system and bursting is terminated instead by voltage and Ca-dependent inactivation of the *Ca* channel. Rewrite the equations above to model this system. (Hint: this is easier than it sounds; delete a couple of things and add inactivation to the calcium current and an inactivation model.)

Part b)

There should be a function $h\infty(V,Ca)$ in your model above. Given that this is an inactivation function that should terminate bursting in response to depolarization and the rise in Ca during the burst, which of the following are possible $h\infty(V,Ca)$ functions, in the sense that the qualitative change (increase or decrease) in $h\infty(V,Ca)$ is correct as V and Ca increase from zero?

$$(1) h_{\infty}(V,Ca) = \frac{Ca(1-e^{-(V-E_{rest})})}{Ca+K_I}$$

$$(2) h_{\infty}(V,Ca) = \frac{2K_I}{(Ca+K_I)(1+e^{(V-E_{rest})})}$$

$$(3) h_{\infty}(V,Ca) = \frac{K_I(1-e^{-(V-E_{rest})})}{Ca+K_I}$$