

SBE II: Homework 4

Experiment-4:

Given that we know the following:

$$\tilde{V}(x, s) = \frac{2I_0\lambda r_i}{s\sqrt{s+1}} \cosh\left(\sqrt{s+1} \frac{x}{\lambda}\right)$$

We are asked to derive the equation of V for steady state (i.e. $t \rightarrow \infty$). This can be accomplished by applying the final value theorem.

$$\begin{aligned} V(s, t \rightarrow \infty) &= \lim_{s \rightarrow 0} s \tilde{V}(x, s) \\ &= \lim_{s \rightarrow 0} \frac{2I_0\lambda r_i}{\sqrt{s+1}} \cosh\left(\sqrt{s+1} \frac{x}{\lambda}\right) \\ V(x, t \rightarrow \infty) &= 2I_0r_i\lambda \cosh\left(\frac{x}{\lambda}\right) \end{aligned}$$