

# CARNET- Carbon Neutral Evaluation Tool

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## 1 Introduction

Baltimore County (BC) requires an interactive decision support tool, wherein decision makers can alter input parameters, to identify and evaluate various feasible (and ideally optimal) conversion roadmaps for the transformation of the current BC vehicle fleet to a low-carbon, renewable energy vehicle fleet in order to achieve a percentage reduction in greenhouse gas emissions from a baseline year by a target date. The current goal is to reduce emissions by 40% of 2006 levels by 2037.

## 2 Dataset

BC has a fleet of 1400+ vehicles which are a combination of buses, trucks and sedans. All of them are run on gas engines (ICEs).

## 3 Model Formulation

### 3.1 Variables

- **Planning horizon:** Let  $T = \{0, 1, 2, 3...20\}$  indicate the total planning horizon in years and  $t \in T$ .
- **Vehicle:** Let  $V_i^t$  be the set of all vehicles in the portfolio at a given time  $t$  with  $n_t$  being the total number of vehicles.
- **Fuel:** Let  $F_i^t$  be the fuel/consumable cost of vehicle  $i$  in the portfolio in the time  $t$ . This is calculated based on  $FE_t$  (with a deterioration factor  $DF_t$ ), the fuel economy of the vehicle measured in miles per gallon and  $VMT_t$ , the Vehicle Miles travelled-  $F_i = \left[ \frac{FE_t}{DF_t} \times VMT_t \right] \times c_t$  where  $c_t$  is the cost in \$ for fuel. We denote the first component in the above equation as  $f_i^t$  or the fuel consumed.
- **Emission Cost:**  $E_i^t$  be the emission cost of vehicle  $V_i^t$  at time  $t$  and  $E_t$  be the total emission cost of the portfolio of vehicles in year  $t$ . This is

calculated based on the fuel consumed  $f_i^t$  and the emission factor  $EF$  and the environmental damage cost of emission  $C_{CO2}$  as follows.

$$E_i = f_i^t \times EF \times C_{CO2}$$

We will assume the damage cost of emission  $C_{CO2}$  to be \$120 per ton (based on literature).

- **Purchase Costs:** Let  $P_i^t$  be the salvage adjusted purchase cost the corresponding infrastructure set up cost of the replacement vehicle  $i$  in the year  $t$  and  $P_t$  be the total cost purchase and setting up of all new vehicles and in time  $t$ .  $P_T$  is the total purchase cost over the time horizon.

$$P_T = \sum_{t=0}^{max(T)} P_t$$

- **Maintenance Costs:** Let  $M_i^t$  be the cost of maintenance and repair of vehicle  $V_i^t$  in the portfolio in the year  $t$ .  $M_t$  be the total cost of maintenance and repair in year  $t$  and  $M_T$  is the total maintenance cost over the time horizon.

$$M_T = \sum_{t=0}^{max(T)} M_t$$

- **Total Cost:** Let  $C_i^t$  be the total cost incurred in year  $t$ . It is computed as-

$$C_i^t = E_i^t + M_i^t + F_i^t$$

and  $C_T$  is the total cost incurred over the entire time horizon  $T$  across all the vehicles.

$$C_T = E_T + M_T + F_T$$

### 3.2 Decision

The decision that needs to be made is either 'Keep' ( $K$ ) or 'Replace' ( $R$ ) a vehicle  $V_i$  in a given year  $t$ . An optimal decision is a matrix of size  $n \times T$  of  $K$ s and  $R$ s.

### 3.3 Stage

Since there is one decision per year it makes sense to keep every  $t \in T$  as the stage.

### 3.4 Recursion equation and constraints

We write down the recursion equation of minimizing the total cost of the Replacement problem as below.

$$g(t) = \min_x \{C_t + g(x)\}$$

Where  $g(t)$  is the minimum cost incurred from time  $t$  till time  $\max(T)$  and  $x$  satisfies the inequality  $t + 1 \leq x \leq \max(T)$ . *This equation will have to be applied to each of the  $i$  vehicles individually.(To discuss).*

### 3.5 Constraints

- **Purchase Budget-** The annual purchase and set-up cost cannot exceed  $B_t$ . i.e

$$P_t \leq B_t$$

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- **Mileage threshold-** Vehicle  $V_i$  can only be replaced if it has travelled a threshold miles  $A$ . i.e

$$VMT_i \geq A$$

if decision is replace( $R$ ).