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Classical Ciphers and Frequency Analysis Examples

The following are some examples of classical ciphers and letter frequency analysis used in my course on [Security and Cryptography](#) at SIIT.

Caesar Cipher and Brute Force Attack

Lets start with some ciphertext obtained using a Caesar cipher:

```
dvvkzeczssprkkve
```

There are 26 possible keys with a Caesar cipher and so a brute force attack is easy. The following uses the [crypto](#) script in a for loop, decrypting the ciphertext with each different key. The key and corresponding plaintext is printed.

```
$ for i in `seq 0 25`; do echo -n "$i "; crypto caesar dec dvvkzeczssprkkve
$i ; done ;
0 dvvkzeczssprkkve
1 cuujydberroqjjud
2 bttixcadqqnpiitc
3 asshwbzcppmohhsb
4 zrrgvayboolnggra
5 yqqfuzxannkmffqz
6 xppetywzmmjleepy
7 woodsxvyllikddox
8 vnncrwuxkkhjccnw
9 ummbqvtwjgibbmV
10 tllapusviifhaalu
11 skkzotruhhegzckt
12 rjjynstggdfyyjs
13 qiixmrpsffcexxir
14 phhwlqoreebdwhhQ
15 oggvkpnqddacvvgp
16 nffujompcczbuufo
17 meetinlobbyatten
18 lddshmknaxzssdm
19 kccrgljmzzwyrrcl
20 jbbqfkilyyvxxqbk
21 iaapejhxuwxppaj
22 hzzodigjwvtvoozi
23 gyynchfivvsunnyh
24 fxxmbgehuurtmmxg
25 ewwlaafdgttqslwlf
```

Which plaintext makes sense? "meet in lobby at ten" (I've inserted the spaces for readability). The 25 other plaintexts look like random collections of English characters - they don't form known English words/phrases. Hence if we can recognise valid plaintext, the brute force attack works.

Just to confirm, lets decrypt using key 17 (and to demonstrate the crypto script, also encrypt):

```
$ crypto caesar dec dvvkzeczssprkkve 17
meetinlobbyatten
$ crypto caesar enc meetinlobbyatten 17
dvvkzeczssprkkve
```

Letter Frequency Analysis

An alternative to a brute force attack is to be more intelligent. Apply cryptanalysis. We've already assumed the plaintext is English text. English text (and in fact text in any language) has structure. A simple measure of the structure is the frequency at which certain letters occur, e.g. letter 'e' occurs much more frequently on average than the letter 'q'. To demonstrate this lets take an English [book](#) and count the occurrences of each letter. Of the 447,145 letters in the book, the following shows the percentage that the top 15 letters make up:

```
$ crypto count letters book1.txt percentsort
447145
12.29 e
 9.06 t
 8.08 a
 7.80 o
 6.99 i
 6.65 n
 6.62 h
 6.25 s
 5.74 r
 4.27 d
 3.94 l
 3.05 u
 2.72 m
 2.58 w
 2.48 c
```

The letter 'e' is the most frequent (about 12% of all letters in the book), followed by 't', and so on. If similar analysis is performed on other English books, similar statistics can be obtained. There are other statistics about expected plaintext that can be obtained as well. For example, the frequency of digrams (pairs of letters) and trigrams (triples of letters). From the same book:

```
$ crypto count digrams book1.txt percentsort
338145
 3.87 th
 3.59 he
 2.36 in
 2.18 er
 2.03 an
 1.74 ha
 1.73 re
 1.72 ou
```

```

1.55 nd
1.51 at
1.38 on
1.33 ed
1.32 en
1.27 it
1.25 hi
$ crypto count trigrams book1.txt percentsort
235545
3.39 the
1.55 and
1.21 ing
0.96 hat
0.91 you
0.88 her
0.83 tha
0.74 his
0.68 ere
0.61 was
0.54 ver
0.54 for
0.51 thi
0.51 ave
0.48 ter

```

'th' is the most frequency digram and 'the' the most frequent trigram. These statistics aid in the cryptanalysis of a ciphertext. Consider the general Caesar cipher. The letter 'a' in plaintext always maps to the same letter in ciphertext (the actual letter depends on the key). Similar with all other letters in plaintext. Therefore in plaintext we expect the letter 'e' to be most common (about 12%). If we look at the most common letter in the ciphertext then we may try assuming that that ciphertext letter maps to the letter 'e' in plaintext. Similar with the 2nd most common letter. After several attempts (normally one or two, but much less than all 26 used with brute force) it's easy to find the key.

Below is an example [ciphertext](#) obtained by encrypting a paragraph of English text with a Caesar cipher.

```

$ cat phrase1-caesar1.txt
ymnxhtzwxjfnrxytuwtanijdtzbnymijyfnqjipstbqjiljtknrutwyfsyyjhmstqtlnjxfsifuuq
nh
fyntsymfyfwjzxjinsymjnsyjwsjyizjytmjgwtfisfyzwjtkymnxknjqiyjmhtzwxjhtajwxtsq
dx
jqjhyjiytunhxkthzxxnslknwxytsxtrjfiafshjiytunhxnsnsyjsjyyjhmstqtlnjxjlnwjqq
xx
qfsxrtgnqjnsyjsjyrzqynhfxyfsiymjsfxjqjhyntstkhzwwjsyfsisjcyljsjwfyntsfsuqnfhf
yn
tsxfsixjwanhxxjluunuyaatanudtzbnnqqjfwsmtbymjnsyjsjybtwpxfsimtbxjwanhxxfsifuu
qn
hfyntsfwjuwtanijiytzxjwxtkymjnsyjsjyymnxpstbqjiljbnqqmqjqudtz

```

And the statistics about frequencies of letters from this ciphertext:

```
$ crypto count letters phrasel-caesar1.txt percentsort
552
13.41 j
9.78 y
9.24 s
8.33 t
8.33 n
6.52 x
6.34 f
5.07 w
4.71 q
4.35 i
3.80 h
3.62 u
3.08 m
2.54 z
1.99 b
```

In the ciphertext the letter 'j' is most common. But we expect letter 'e' to be most common in the plaintext. If we assumed plaintext 'e' mapped to ciphertext 'j' then that implies a key of 5. Lets try to decrypt the entire ciphertext with the key:

```
$ crypto caesar dec phrasel-caesar1.txt 5 file
thiscourseaimstoprovideyouwithdetailedknowledgeofimportanttechnologiesandappl
ic
ationthatareusedintheinternetduetothebroadnatureofthisfieldthecoursecoversonl
ys
electedtopicsfocussingfirstonsomeadvancedtopicsininternettechnologiesegwirele
ss
lansmobileinternetmulticastandthenaselectionofcurrentandnextgenerationapplica
ti
onsandservicesegpptvvoipyowilllearnhowtheinternetworksandhowservicesandapp
li
cationsareprovidedtousersoftheinternetthisknowledgewillhelpyouinthedesignandm
an
agementofcomputernetworksaswellasdevelopmentandexecutionofinternetapplication
s
```

We've found the [plaintext](#) after just 1 decryption! If using key 5 did NOT produce readable plaintext then we could have guessed the key based on the second most common letter and so on.

Frequency Analysis of Monoalphabetic Cipher

The Caesar cipher is subject to both brute force and a frequency analysis attack. But what about ciphers with larger key spaces? A monoalphabetic cipher using 26 English characters has 26! possible keys (that is, more than 10^{26}). A brute force attack is no longer feasible. Lets see how frequency analysis still makes breaking a monoalphabetic cipher easy.

Below is the [ciphertext](#) output from a monoalphabetic cipher:

```
$ cat phrase3-mono1.txt
ziolegxkltqodlzgofzkgrxetngxzgzihtkofeohstlqfrzteifojxtlgyltexkofuegdhxztklqf
regd
hxztkftzvvgkalvoziygexlgfzfztkftzltexkoznzitegxkltolttytezoctsnlhsozofzgzvghqk
zlyo
klzofzkgrxeofuzitzitgkngyeknhzgukqhinoxfesxrofuigvdqfnesqlloeqsqfrhghxsqkqsugk
ozid
lvgkaturtlklqrouozqsloufqzxktlqfrltegfrhkgcorofurtzqoslgyktqsofztkftzltexkozn
hkgz
geglqsugkoqidlqfrziktqzltuohltecokxltlyoktvqsslitfetngxvossstqkfwgzizitgktzo
eqsq
lhtezlgyegdhxztkqfrftzvvgkaltextkoznqlvtssqligvziqzzitgknolqhhsotrofzitoftztkftz
ziol
afgvstrutvossitshngxofrtloufofuqfrtctsghofultexktqhhsoeqzogflqfrftzvvgkahkgzg
egsl
qlvtssqlwxosrofultextktftzvvgkal
```

Lets count the frequency of letters and digrams of the ciphertext:

```
$ crypto count letters phrase3-mono1.txt percentsort
597
10.39 t
8.88 z
8.38 o
7.87 l
7.71 g
7.04 k
7.04 f
5.86 q
5.36 s
4.86 e
3.85 x
3.69 h
3.52 r
3.52 i
2.68 u
$ crypto count digrams phrase3-mono1.txt percentsort
596
2.85 of
2.52 zi
2.18 lt
2.01 te
1.68 tz
1.68 gk
1.68 fr
1.51 xk
```

1.51 qf
 1.51 lq
 1.51 it
 1.34 oz
 1.34 eg
 1.17 zt
 1.17 qs

Now compare to the most frequent letters and digrams from the example English book [above](#). (In the following I will write the plaintext letters in UPPERCASE)

Looking at the four most frequent letters, in the ciphertext we have t, z, o and l while we expect E, T, A and O. In the ciphertext the letter t occurs about 2% more frequently than the second most frequent. So initially lets assume plaintext E maps to ciphertext t, or in short E-->t. Now lets look at the ciphertext, but replacing each occurrence of t with E:

```
ziolegxklEqodl zgofz kgrxeEngxzgziEhkofeohsElqfrzEeifojxElgylEexkofuegdhxxEklqf
regd
hxzEkfEzvgkalvoziygexlgf ofzEkfEzlEexkoznziEegxklEolEyyEezocEsnlhsozofzgzvghqk
zlyo
klzofz kgrxeofuziEziEgkngyeknhzgukqhino fesxrofuigvdqfnesqlloeqsqfrhghxsqkqsugk
ozid
lvgkaEurElklqrouozqsloufqzxkElqfrlEegfrhkgcorofurEzqoslgykEqsofzEkfEzlEexkozn
hkgz
gegslqsugko zidlqfrzikEqzlEuohlEecokxlElyokEvqssliEfeEngxvosssEqkfwgziziEgkEzo
eqsq
lhEezlgyegdhxxEklqfrfEzvgkalEexkoznqlvEssqligvziqzziEgknolqhhsoErofziEofzEkfEz
ziol
afgvsEruEvossiEshngxofrElouf ofuqfr rEcEsghofulEexkEqhhsoeqzogflqfrfEzvgkahkgzg
egsl
qlvEssqlwxosrofulEexkEfEzvgkal
```

That doesn't help much - it is impossible to make out any English words yet. Lets continue with the second most frequent letter and assume T-->z.

```
TiolegxklEqodlTgofTkgrxeEngxTgTiEhkofeohsElqfrTEeifojxElgylEexkofuegdhxTEklqf
regd
hxTEkfETvgkalvoTiygexlgf ofTEkfETlEexkoTnTiEegxklEolEyyEeTocEsnlhsoTofTgTvghqk
Tlyo
klTofTkgrxeofuTiETiEgkngyeknhTgukqhino fesxrofuigvdqfnesqlloeqsqfrhghxsqkqsugk
oTid
lvgkaEurElklqrouoTqsloufqTxkElqfrlEegfrhkgcorofurETqoslgykEqsofTEkfETlEexkoTn
hkgT
gegslqsugkoTidlqfrTikEqTlEuohlEecokxlElyokEvqssliEfeEngxvosssEqkfwgTiTiEgkETo
eqsq
lhEeTlgyegdhxTEklqfrfETvgkalEexkoTnqlvEssqligvTiQTiEgknolqhhsoErofTiEofTEkfET
Tiol
afgvsEruEvossiEshngxofrElouf ofuqfr rEcEsghofulEexkEqhhsoeqTogflqfrfETvgkahkgTg
egsl
```

```
qlvEssqlwxosrofulEexkEfETvgkal
```

Still difficult to identify words. Lets try the two most frequent digrams. In the ciphertext we have 'of' and 'zi' while we expect 'IN' and 'TH'. We already have assumed t-->Z, so no lets also try: o-->I, f-->N and i-->H.

```
THIlegxklEqIdlTgINTkgrxeEngxTgTHEhkINeIhsElqNrTEeHNIjxElgylEexkINuegdhxTEklqN
regd
hxTEkNETvgkalvITHygexlgNINTEkNETlEexkITnTHEegxkleIIEyyEeTICesnhsITINTgTvghqk
TlyI
kLTINTkgrxeINuTHETHEgkngyeknhTgukqhHnINesxrINuHgvdqNnesqlleqsqNrghghxsqkqsugk
ITHd
lvgkaEurElklqrIuITqslIuNqTxkElqNrIEegNrhhkgcIrINurETqIslgykEqsINTEkNETlEexkITn
hkgT
gegsLqsugkITHdlqNrTHkEqTlEuIhlEecIkxlElyIkEvqsslHENeEngxvIsssEqkNwgTHTHEgkETI
eqsq
lhEeTlgyegdhxTEkqNrNETvgkalEexkITnqlvEssqlHgvTHqTTHEgknIlqhhsIErINTHEINTEkNET
THIl
aNgvsEruEvIssHEshngxINrElIuNINuqNrrEcEsghINulEexkEqhhsIeqTIgNlqNrNETvgkahkgTg
egsl
qlvEssqlwxIsrINulEexkENETvgkal
```

Can we make out any words? On the second line (and elsewhere) INTEkNET suggests k-->R (giving INTERNET). The first word is THl... Possibly THIS? Lets also try l-->S.

```
THISegxRSEqIdSTgINTRgrxeEngxTgTHEhRINeIhsESqNrTEeHNIjxEsGySEexRINuegdhxTERSqN
regd
hxTERNETvgRaSvITHygexSgNINTERNETSEexRITnTHEegxRSEISEyyEeTICesnShsITINTgTvghqR
TSyI
RSTINTRgrxeINuTHETHEgRngyeRnhTguRqhHnINesxrINuHgvdqNnesqSSIEqsqNrghghxsqRqsugR
ITHd
SvgrRaEurESRSqrIuITqssIuNqTxRESqNrSEegNrhhRgcIrINurETqIsSgyREqsINTERNETSEexRITn
hRgT
gegsSqsugRITHdSqNrTHREqTSEuIhSEecIRxSESyIREvqssSHENeEngxvIsssEqkNwgTHTHEgRETI
eqsq
ShEeTSgyegdhxTERqNrNETvgRaSEexRITnqSvEssqSHgvTHqTTHEgRnISqhhsIErINTHEINTERNET
THIS
aNgvsEruEvIssHEshngxINrESIuNINuqNrrEcEsghINuSEexREqhhsIeqTIgNSqNrNETvgRahRgTg
egsS
qSvEssqSwxIsrINuSEexRENETvgRaS
```

Now returning to the most frequent letters. We have already covered E, T, I, N and H. The other two frequency letters are A and O. In the ciphertext we have covered t, z, o, f and i. So its likely that A and O map to one of l, g, or k. Try different combinations in the text so far and see if any words make sense. Eventually I tried g-->O.

```
THISe0xRSEqIdST0INTROrxeEn0xT0THEhRINeIhsESqNrTEeHNIjxEs0ySEexRINue0dhxTERSqN
re0d
hxTERNETv0RaSvITHy0exSONINTERNETSEexRITnTHEe0xRSEISEyyEeTICesnShsITINT0Tv0hqR
```

TSyI
 RSTINTROrxeINuTHETHEORnOyeRnhT0uRqhHnINesxrINuH0vdqNnesqSSIEqsqNrh0hxsqRqsuOR
 ITHd
 Sv0RaEurESRSqrIuITqsSIuNqTxRESqNrSEeONrhR0cIrINurETqIsS0yREqsINTERNETSEexRITn
 hROT
 0e0sSqsuORITHdSqNrTHREqTSEuIhSEecIRxSESyIREvqssSHENeEn0xvIsssEqRNw0THTHEORETI
 eqsq
 ShEeTS0ye0dhxTERqNrNETv0RaSEexRITnqSvEssqSH0vTHqTTHEORnISqhhsIErINTHEINTERNET
 THIS
 aN0vsEruEvIssHEshn0xINrESIuNINuqNrrEcEs0hINuSEexREqhhsIeqTIONSqNrNETv0RahR0TO
 e0sS
 qSvEssqSwxIsrINuSEexRENETv0RaS

Near the start we have INTROrxe. That suggests INTRODUC... (as in introduction, introduce, introducing). Now lets assume
 r-->D, x-->U and e-->C.

THISCOURSEqIdSTOINTRODUCEnOUTOTHEhRINCIhsESqNDTECHNIjUES0ySECURINuC0dhUTERSqN
 DC0d
 hUTERNETv0RaSvITHy0CUSONINTERNETSECURITnTHECOURSEISEyyECTIcEsnShsITINT0Tv0hqR
 TSyI
 RSTINTRODUCINuTHETHEORnOyCRnhT0uRqhHnINCsUDINuH0vdqNnCsqSSICqsqNDh0hUsqRqsuOR
 ITHd
 Sv0RaEuDESRSqDIuITqsSIuNqTURESqNDSECONdhR0cIDINuDETqIsS0yREqsINTERNETSECURITn
 hROT
 0C0sSqsuORITHdSqNDTHREqTSEuIhSECCIRUSESyIREvqssSHENCEn0UvIsssEqRNw0THTHEORETI
 Cqsq
 ShECTS0yC0dhUTERqNDNETv0RaSECURITnqSvEssqSH0vTHqTTHEORnISqhhsIEDINTHEINTERNET
 THIS
 aN0vsEDuEvIssHEshn0UINDESIuNINuqNDDEcEs0hINuSECUREqhhsICqTIONSqNDNETv0RahR0TO
 C0sS
 qSvEssqSwUIsDINuSECURENETv0RaS

THIS COURSE qIdSTO INTRODUCE nOU TO THE hRINCIhsES Try n-->Y, h-->P and s-->L.

THISCOURSEqIdSTOINTRODUCEYOUTOTHEPRINCIPLESqNDTECHNIjUES0ySECURINuC0dPUTERSqN
 DC0d
 PUTERNETv0RaSvITHy0CUSONINTERNETSECURITYTHECOURSEISEyyECTIcELYSPPLITINT0Tv0PqR
 TSyI
 RSTINTRODUCINuTHETHEORY0yCRYPT0uRqPHYINCLUDINuH0vdqNYCLqSSICqLqNDPOPULqRqLuOR
 ITHd
 Sv0RaEuDESRSqDIuITqLSIuNqTURESqNDSECONdPR0cIDINuDETqILS0yREqLINTERNETSECURITY
 PROT
 0COLSqLuORITHdSqNDTHREqTSEuIPSECCIRUSESyIREvqLLSHENCEY0UvILLLEqRNw0THTHEORETI
 CqLq
 SPECTS0yC0dPUTERqNDNETv0RaSECURITYqSvELLqSH0vTHqTTHEORYISqPPLIEDINTHEINTERNET
 THIS
 aN0vLEDuEvILLHELPHYOUINDESIuNINuqNDDEcELOPINuSECUREqPPLICqTIONSqNDNETv0RaPROTO

COLS

qSvELLqSwUILDINuSECURENETv0RaS

THIS COURSE qIdS TO INTRODUCE YOU TO THE PRINCIPLES qND TECHNIjUES Oy SECURINu CodPUTERS ...

With a few more steps it is easy to find the remaining letters and the resulting plaintext:

THISCOURSEAIMSTOINTRODUCEYOUTOTHEPRINCIPLESANDTECHNIQUESOFSECURINGCOMPUTERSAND
DCOM
PUTERNETWORKSWITHFOCUSONINTERNETSECURITYTHECOURSEISEFFECTIVELYSPLITINTOTWOPAR
TSFI
RSTINTRODUCINGTHETHEORYOFCRYPTOGRAPHYINCLUDINGHOWMANYCLASSICALANDPOPULARALGOR
ITHM
SWORKEGDESRSADIGITALSIGNATURESANDSECONDPROVIDINGDETAILSOFFREALINTERNETSECURITY
PROT
OCOLSALGORITHMSANDTHREATSEGIPSECVIRUSESFIREWALLSHENCEYOUWILLLEARNBOTHTHEORETI
CALA
SPECTSOFCOMPUTERANDNETWORKSECURITYASWELLASHOWTHATTHEORYISAPPLIEDINTHEINTERNET
THIS
KNOWLEDGEWILLHELPLYOUINDESIGNINGANDDEVELOPINGSECUREAPPLICATIONSANDNETWORKPROTO
COLS
ASWELLASBUILDINGSECURENETWORKS

So we have demonstrated that this monoalphabetic cipher has too many keys to apply a brute force attack ($> 10^{26}$), with frequency analysis and some trial-and-error we could manually break the cipher and obtain the [plaintext](#) in less than 1 hour. In fact these steps can be automated and solved almost instantly with a computer.

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