```
In [1]: # This notebook prepares the dataframes for analysis and runs
         # the VAR on the combined model (economic and sentiment features) and
         # the economic (only) model.
In [2]: | import warnings
         warnings.filterwarnings('ignore')
In [3]: import numpy as np
         import pandas as pd
         import matplotlib.pyplot as plt
         from statsmodels.tsa.vector_ar.var_model import VAR
         from sklearn.metrics import r2 score
         from statsmodels.stats.stattools import durbin watson
         from scipy.stats.distributions import chi2
         import warnings
         warnings.filterwarnings('ignore')
In [4]: import warnings
         warnings.filterwarnings('ignore')
In [5]: # Quick look at the first two lines of the econ CSV
         with open('data/econ vars.csv') as f:
             print(f.readline())
             next(f)
             print(f.readline())
         \verb|month_date,ur,pi_gr,nyse_gr,gdp_log_diff,tb_sqrt_diff,ics_log_diff,pce_gr_diff|
         2011-01-01,9.1,0.002028679786119758,0.016528644263536174,-
         0.004803188602163777
In [6]: # Set data types for the econ features
         dts = {"month date": str, "ur": np.float64
               "pi_gr": np.float64, "nyse_gr": np.float64
             , "gdp_log_diff": np.float64, "tb_sqrt_diff": np.float64
, "ics_log_diff": np.float64, "pce_gr_diff": np.float64}
In [7]: # Import econ data
         data raw = pd.read csv("data/econ vars.csv"
                            , sep=","
                            , skiprows=0
                            , dtype=dts)
In [8]: # Check the shape of the raw econ data
         data raw.shape
Out[8]: (91, 8)
In [9]: # Copy raw data
         data = data_raw.copy()
In [10]: # Sort descending and reset index
         data.sort index(ascending=False, inplace=True)
         data.reset index(drop=True, inplace=True)
```

```
In [11]: # Check the dataframe
    data.head()
```

Out[11]:

| | month_date | ur | pi_gr | nyse_gr | gdp_log_diff | tb_sqrt_diff | ics_log_diff | pce_gr_diff |
|---|------------|-----|-----------|-----------|--------------|--------------|--------------|-------------|
| 0 | 2018-06-01 | 4.0 | 0.003863 | -0.001827 | 0.000000 | 0.014587 | 0.002039 | -0.001110 |
| 1 | 2018-05-01 | 3.8 | 0.003728 | 0.000941 | 0.010188 | 0.037168 | -0.008130 | 0.008168 |
| 2 | 2018-04-01 | 3.9 | -0.004827 | -0.002903 | 0.010188 | 0.022809 | -0.025975 | -0.008891 |
| 3 | 2018-03-01 | 4.1 | 0.003938 | -0.015846 | 0.000000 | 0.050844 | 0.016907 | 0.007407 |
| 4 | 2018-02-01 | 4.1 | 0.003282 | -0.053517 | 0.005479 | 0.065562 | 0.040947 | 0.001663 |

```
In [12]: # Quick look at the first two lines of the sentiment CSV
with open('data/rev_means_vars_stationary.csv') as f:
    print(f.readline())
    next(f)
    print(f.readline())
```

date,perc_pos_rev_weighted,perc_neg_rev_weighted,perc_uncert_rev_weighted,perc_l itig_rev_weighted,perc_modal_wk_rev_weighted,perc_modal_mod_rev_weighted,perc_co nstrain rev weighted,perc modal str rev weighted diff

2011-03-01, 1.9607048390000001, 0.979452392, 0.957424913, 0.073102265, 0.387478896, 0.560045154, 0.142131806, -0.0495581759999999

```
In [14]: # Check the sentiment data types sent_raw.dtypes
```

```
Out[14]: date
                                                object
         perc_pos_rev_weighted
                                               float64
         perc_neg_rev_weighted
                                               float64
         {\tt perc\_uncert\_rev\_weighted}
                                               float64
         perc_litig_rev_weighted
                                               float64
                                               float64
         perc_modal_wk_rev_weighted
         perc_modal_mod_rev_weighted
                                               float64
                                               float64
         perc constrain rev weighted
         perc modal str rev weighted diff
                                               float64
         dtype: object
```

In [15]: # Drop any observations with Nan sent_raw.dropna(inplace=True)

```
In [16]: #sort and reset the index
    sent_raw.sort_values(by='date', ascending=False, inplace=True)
    sent_raw.reset_index(drop=True, inplace=True)
```

In [17]: # Confirm the shape of the dataframe
 sent_raw.shape

Out[17]: (89, 9)

In [18]: # Check the dataframe
sent_raw.head()

Out[18]:

| | date | perc_pos_rev_weighted | perc_neg_rev_weighted | perc_uncert_rev_weighted | perc_litig |
|---|------------|-----------------------|-----------------------|--------------------------|------------|
| 0 | 2018-06-01 | 2.043836 | 0.890239 | 0.815790 | 0.094844 |
| 1 | 2018-05-01 | 1.915107 | 1.074677 | 0.803269 | 0.082565 |
| 2 | 2018-04-01 | 1.926137 | 1.068873 | 0.777739 | 0.095691 |
| 3 | 2018-03-01 | 2.016781 | 0.979256 | 0.800769 | 0.102810 |
| 4 | 2018-02-01 | 2.004129 | 0.963727 | 0.815629 | 0.098500 |

In [19]: # Copy sentiment data
sent = sent_raw.copy()

In [21]: # Combine the econ and sentiment dataframes
data = pd.concat([data,sent], axis=1)

In [23]: # Drop the month_date column and the gdp column
data = data.drop(data.columns[[0,4]], axis=1)

In [24]: # Check the dataframe
data.head()

Out[24]:

| | ur | pi_gr | nyse_gr | tb_sqrt_diff | ics_log_diff | pce_gr_diff | perc_pos_rev_weighted | ķ |
|------------|-----|-----------|-----------|--------------|--------------|-------------|-----------------------|---|
| date | | | | | | | | |
| 2018-06-01 | 4.0 | 0.003863 | -0.001827 | 0.014587 | 0.002039 | -0.001110 | 2.043836 | C |
| 2018-05-01 | 3.8 | 0.003728 | 0.000941 | 0.037168 | -0.008130 | 0.008168 | 1.915107 | 1 |
| 2018-04-01 | 3.9 | -0.004827 | -0.002903 | 0.022809 | -0.025975 | -0.008891 | 1.926137 | 1 |
| 2018-03-01 | 4.1 | 0.003938 | -0.015846 | 0.050844 | 0.016907 | 0.007407 | 2.016781 | C |
| 2018-02-01 | 4.1 | 0.003282 | -0.053517 | 0.065562 | 0.040947 | 0.001663 | 2.004129 | C |

In [25]: # Copy econ features to econ dataframe and drop all sentiment variables econ = data.drop(data.columns[[6,7,8,9,10,11,12,13]], axis=1)

In [26]: # Check the dataframe
econ.head()

Out[26]:

| | ur | pi_gr | nyse_gr | tb_sqrt_diff | ics_log_diff | pce_gr_diff |
|------------|-----|-----------|-----------|--------------|--------------|-------------|
| date | | | | | | |
| 2018-06-01 | 4.0 | 0.003863 | -0.001827 | 0.014587 | 0.002039 | -0.001110 |
| 2018-05-01 | 3.8 | 0.003728 | 0.000941 | 0.037168 | -0.008130 | 0.008168 |
| 2018-04-01 | 3.9 | -0.004827 | -0.002903 | 0.022809 | -0.025975 | -0.008891 |
| 2018-03-01 | 4.1 | 0.003938 | -0.015846 | 0.050844 | 0.016907 | 0.007407 |
| 2018-02-01 | 4.1 | 0.003282 | -0.053517 | 0.065562 | 0.040947 | 0.001663 |

In [28]: # Fit the model to the combined variables
 comb_fitted = comb_model.fit(maxlags=2, ic='bic', verbose=True, trend='c')

| VAR | Order | Selection | |
|-----|-------|-----------|--|
|-----|-------|-----------|--|

| ==== | | | | |
|------|-----------------|-----------------|------------|---------|
| | aic | bic | fpe | hqic |
| 0 | -91 . 97 | -91 . 57 | 1.141e-40 | -91.81 |
| 1 | -99.89* | -93.94* | 4.360e-44* | -97.49* |
| 2 | -98.88 | -87.37 | 1.649e-43 | -94.25 |
| | | | | |

^{*} Minimum

Using 1 based on bic criterion $\,$

In [29]: # Print a summary of the models
comb_fitted.summary()

| Model: | VAR | | |
|------------------------|--|---|------------|
| Method: | OLS | | |
| Date: Time: | Tue, 18, Jun, 2019 17:21:51 | | |
| | | | |
| No. of Equation | | | -93.7304 |
| Nobs: | 88.0000 | | -97.2605 |
| | od: 2846.13 | | |
| AIC: | -99 . 6422 | <pre>Det(Omega_mle):</pre> | |
| Results for 6 | | | |
| | | ======================================= | ========= |
| | | coefficient | std. error |
| t-stat | prob | | |
| | | | |
| const -1.755 | 0.083 | -0.827841 | 0.471726 |
| L1.ur | 0.000 | 1.011513 | 0.011859 |
| 85.292 | 0.000 | | |
| L1.pi_gr 0.845 | 0.401 | 1.511155 | 1.787599 |
| L1.nyse_gr | | 0.130882 | 0.435033 |
| 0.301 | | | |
| L1.tb_sqrt_di 0.896 | | 0.289768 | 0.323562 |
| L1.ics_log_di | | 1.056703 | 0.304881 |
| 3.466 | 0.001 | | |
| L1.pce_gr_dif -0.550 | Ef 0.584 | -1.561460 | 2.838331 |
| L1.perc_pos_1 | | 0.085887 | 0.103277 |
| 0.832 | 0.408 | 0 105055 | |
| L1.perc_neg_n 0.852 | | 0.197955 | 0.232477 |
| | rt_rev_weighted | 0.367334 | 0.491891 |
| 0.747 | | 0.000160 | 0.002406 |
| 0.082 | g_rev_weighted 0.935 | 0.080162 | 0.983426 |
| L1.perc_modal | l_wk_rev_weighted | -0.371585 | 0.736801 |
| -0.504 | 0.616 | 0 420772 | 0 461000 |
| 1.perc_modal | L_mod_rev_weighted 0.344 | 0.439772 | 0.461822 |
| L1.perc_const | train_rev_weighted | -0.172817 | 0.992679 |
| -0.174 | 0.862 L str rev weighted diff | -0.557680 | 0.349682 |
| -1.595 | 0.115 | -0.33/660 | 0.349082 |
| | | | |
| Deguli - C | | | |
| | equation pi_gr ==================================== | ======================================= | |
| | ======= | 6-1-1 | |
| + c+>+ | nroh | coefficient | std. error |
| t-stat | prob | | |
| | | | |
| const 0.799 | 0.427 | 0.023636 | 0.029573 |
| L1.ur | V.12, | -0.000248 | 0.000743 |
| -0.333 | 0.740 | | |
| L1.pi_gr | | -0.191584 | 0.112067 |

```
In [30]: # Calculate the combined r squared
y_true = data['pce_gr_diff'].iloc[1:89]
y_pred = comb_fitted.resid['pce_gr_diff'] + y_true
print ("Combined model R^2: {}".format(r2_score(y_true, y_pred)))

Combined model R^2: 0.3033409524231241
```

In [31]: # Calculate the mean squared error of the combined model
 comb_mse = np.mean(comb_fitted.resid['pce_gr_diff']**2)
 print ("Combined model MSE: {}".format(comb_mse))

Combined model MSE: 1.746804553927309e-05

Combined model Durbin-Watson test: 2.5328634408873234

In [33]: # Instantiate the VAR model using the econ variables
 econ_model = VAR(econ)

In [34]: # Fit the model to the econ data
 econ_fitted = econ_model.fit(maxlags=2, ic='bic', verbose=True, trend='c')

| VAR | Order | Selection |
|-----|-------|-----------|
|-----|-------|-----------|

| ==== | | | | ======== |
|------|---------|---------|------------|----------|
| | aic | bic | fpe | hqic |
| | | | | |
| 0 | -38.34 | -38.17 | 2.228e-17 | -38.27 |
| 1 | -43.66 | -42.47* | 1.100e-19 | -43.18 |
| 2 | -44.13* | -41.92 | 6.936e-20* | -43.24* |
| ==== | | | | |

^{*} Minimum

Using 1 based on bic criterion

In [35]: # Print a summary of the models
 econ_fitted.summary()

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| Model: Method: | VAR OLS | | | |
|---|---|--|--|------|
| | ue, 18, Jun, 2019 | | | |
| Time: | 17:21:51 | | | |
| No. of Equations: | 6.00000 | BIC: | -42.4596 | |
| Nobs: | 88.0000 | | -43.1656 | |
| Log likelihood: | 1213.05 | FPE: | 1.11537e-19 | |
| AIC: | -43.6420 | Det(Omega_mle): | 7.04649e-20 | |
| Results for equat: | ion ur | | | ==== |
| == | | | | |
| ob | | std. error | | |
| const | 0.009825 | 0.056289 | 0.175 | |
| 0.862 | 1 00000 | 0.000555 | 117 (11 | |
| L1.ur 0.000 | 1.006361 | 0.008557 | 117.611 | |
| L1.pi_gr 0.477 | 1.210979 | 1.696079 | 0.714 | |
| L1.nyse_gr 0.749 | 0.131370 | 0.409557 | 0.321 | |
| L1.tb_sqrt_diff 0.494 | | | 0.687 | |
| L1.ics_log_diff 0.001 | | 0.287296 | 3.343 | |
| Ll.pce_gr_diff 0.602 | -1.438920 | 2.749622 | -0.523 | |
| Results for equat: | | ======== | ======== | ==== |
| ob | coefficient | std. error | t-stat | |
| | | | | |
| | | | | |
| const 0.203 | 0.004612 | 0.003593 | 1.284 | |
| | 0.004612 -0.000387 | | 1.284 | |
| const 0.203 L1.ur | | 0.000546 0.108260 | | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 | -0.000387 -0.138910 0.009626 | 0.000546 0.108260 0.026142 | -0.708 -1.283 0.368 | |
| <pre>const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495</pre> | -0.000387 -0.138910 0.009626 -0.012863 | 0.000546 0.108260 0.026142 0.018753 | -0.708 -1.283 0.368 -0.686 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 | 0.000546 0.108260 0.026142 0.018753 0.018338 | -0.708 -1.283 0.368 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 L1.pce_gr_diff 0.146 | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 -0.257348 | 0.000546 0.108260 0.026142 0.018753 0.018338 0.175507 | -0.708 -1.283 0.368 -0.686 -1.254 -1.466 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 L1.pce_gr_diff 0.146 | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 -0.257348 | 0.000546 0.108260 0.026142 0.018753 0.018338 | -0.708 -1.283 0.368 -0.686 -1.254 -1.466 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 L1.pce_gr_diff 0.146 ==================================== | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 -0.257348 | 0.000546 0.108260 0.026142 0.018753 0.018338 0.175507 | -0.708 -1.283 0.368 -0.686 -1.254 -1.466 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 L1.pce_gr_diff 0.146 ==================================== | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 -0.257348 | 0.000546 0.108260 0.026142 0.018753 0.018338 0.175507 | -0.708 -1.283 0.368 -0.686 -1.254 -1.466 | |
| const 0.203 L1.ur 0.481 L1.pi_gr 0.203 L1.nyse_gr 0.714 L1.tb_sqrt_diff 0.495 L1.ics_log_diff 0.213 L1.pce_gr_diff 0.146 ==================================== | -0.000387 -0.138910 0.009626 -0.012863 -0.022995 -0.257348 | 0.000546 0.108260 0.026142 0.018753 0.018338 0.175507 | -0.708 -1.283 0.368 -0.686 -1.254 -1.466 | |

```
In [36]: # Calculate the combined r squared
         y_true = econ['pce_gr_diff'].iloc[1:89]
         y_pred = econ_fitted.resid['pce_gr_diff'] + y_true
         print ("Economic model R^2: {}".format(r2_score(y_true, y_pred)))
         Economic model R^2: 0.28749324079974536
In [37]: # Calculate the mean squared error of the econ model
         econ_mse = np.mean(econ_fitted.resid['pce_gr_diff']**2)
         print ("Economic model MSE: {}".format(econ_mse))
         Economic model MSE: 1.7865411437689707e-05
In [38]: # Run the Durbin Watson test
         print ("Economic model Durbin-Watson test: {}".format (durbin watson(econ fitted.r
         esid['pce gr diff'])))
         Economic model Durbin-Watson test: 2.5575996229732354
In [39]: # View the log likelihood values
         print ("Combined model Log Likelihood: {}".format(comb fitted.llf))
         print ("Economic model Log Likelihood: {}".format(econ_fitted.llf))
         Combined model Log Likelihood: 2846.125874607882
         Economic model Log Likelihood: 1213.0463632573587
In [40]: # Create a function that calculates the likelihood ratio test
         def likelihood ratio(11 model 1, 11 model 2): # Model 1 is the more restrictive e
         con model
             return (2*(ll model 2 - ll model 1))
In [41]: import math
         # Calculate the likelihood ratio and run the likelihood ratio test on a chi square
         distribution
         LR = likelihood_ratio(econ_fitted.llf, comb_fitted.llf)
         pval = chi2.sf(LR, 8) # Combined model +8 variables 8 d.f.
         print ("Log Likelihood Ratio test p-value: {:4.03f}".format((pval)))
```

Log Likelihood Ratio test p-value: 0.000