Numerical Uncertainty in Analytical Pipelines Lead to Impactful Variability in Brain Networks

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Abstract

The analysis of brain-imaging data requires complex processing pipelines to support findings on brain function or pathologies. Recent work has shown that variability in analytical decisions, small amounts of noise, or computational environments can lead to substantial differences in the results, endangering the trust in conclusions¹⁻⁷. We explored the instability of results by instrumenting a connectome estimation pipeline with Monte Carlo Arithmetic^{8,9} to introduce random noise throughout. We evaluated the reliability of the connectomes, their features 10,11, and the impact on analysis 12,13. The stability of results was found to range from perfectly stable to highly unstable. This paper highlights the potential of leveraging induced variance in estimates of brain connectivity to reduce the bias in networks alongside increasing the robustness of their applications in the classification of individual differences. We demonstrate that stability evaluations are necessary for understanding error inherent to brain imaging experiments, and how numerical analysis can be applied to typical analytical workflows both in brain imaging and other domains of computational science. Overall, while the extreme variability in results due to analytical instabilities could severely hamper our understanding of brain organization, it also leads to an increase in the reliability of datasets.

Keywords

Stability — Reproducibility — Network Neuroscience — Neuroimaging

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The modelling of brain networks, called connectomics, 9 but potentially pave the way for therapeutics 19-23. ² has shaped our understanding of the structure and function 3 of the brain across a variety of organisms and scales over 4 the last decade 11, 14-18. In humans, these wiring diagrams are 6 and show promise towards identifying biomarkers of disease. 7 This can not only improve understanding of so-called "connec-

However, the analysis of brain imaging data relies on complex computational methods and software. Tools are trusted to ₁₂ perform everything from pre-processing tasks to downstream 5 obtained in vivo through Magnetic Resonance Imaging (MRI), 13 statistical evaluation. While these tools undoubtedly undergo 14 rigorous evaluation on bespoke datasets, in the absence of 15 ground-truth this is often evaluated through measures of re-8 topathies", such as Alzheimer's Disease and Schizophrenia, 16 liability^{24–27}, proxy outcome statistics, or agreement with

17 existing theory. Importantly, this means that tools are not 53 sampled into two components, resulting in four samples per 24 and it is likely that software instabilities played a role.

29 cations of the observed instabilities on downstream analyses 30 were quantified. We accomplished this through the use of 31 Monte Carlo Arithmetic (MCA)⁸, a technique which enables 32 characterization of the sensitivity of a system to small nu-33 merical perturbations. This is importantly distinct from data 34 perturbation experiments where the underlying datasets are 35 manipulated or pathologies may be simulated, and allows 36 for the evaluation of experimental uncertainty in real-world 37 settings. We explored the impact of numerical perturbations 38 through the direct comparision of structural connectomes, the 39 consistency of their features, and their eventual application 40 in a neuroscience study. We also characterized the conse-41 quences of instability in these pipelines on the reliability of 42 derived datasets, and discuss how the induced variability may 43 be harnessed to increase the discriminability of datasets, in 44 an approach akin to ensemble learning. Finally, we make 45 recommendations for the roles perturbation analyses may play 46 in brain imaging research and beyond.

47 Graphs Vary Widely With Perturbations

49 understanding of the induced variability was required. A sub- 86 tinct, connectomes generated with sparse perturbations show 50 set of the Nathan Kline Institute Rockland Sample (NKIRS) 87 considerable variability, often reaching deviations equal to 51 dataset²⁹ was randomly selected to contain 25 individuals 88 or greater than those observed across individuals or sessions 52 with two sessions of imaging data, each of which was sub- 89 (Figure 1A; right). Interpretting these results with respect to

18 necessarily of known or consistent quality, and it is not un- 54 individual and 100 samples total ($25 \times 2 \times 2$ samples). Struc-19 common that equivalent experiments may lead to diverging 55 tural connectomes were generated with canonical determinis-20 conclusions^{1,5–7}. While many scientific disciplines suffer 56 tic and probabilistic pipelines^{30,31} which were instrumented 21 from a lack of reproducibility²⁸, this was recently explored 57 with MCA, replicating computational noise either sparsely 22 in brain imaging by a 70 team consortium which performed 58 or densely throughout the pipelines^{4,9}. In the sparse case, a 23 equivalent analyses and found widely inconsistent results¹, 59 small subset of the libraries were instrumented with MCA, al-60 lowing for the evaluation of the cascading effects of numerical The present study approached evaluating reproducibility 61 instabilities that may arise. In the dense case, operations are 26 from a computational perspective in which a series of brain 62 more uniformly perturbed and thus the law of large numbers 27 imaging studies were numerically perturbed in such a way 63 suggests that perturbations will quickly offset one-another and 28 that the plausibility of results was not affected, and the impli- 64 only dramatic local instabilities will have propagating effects. 65 Importantly, the perturbations resulting from the sparse setting 66 represent a strict subset of the possible outcomes of the dense ₆₇ implementation. The random perturbations are statistically 68 independent from one another across both settings and sim-69 ulations. Instrumenting pipelines with MCA increases their 70 computation time, in this case by multiplication factors of $_{71}$ 1.2× and 7× for the sparse and dense settings, respectively⁴. 72 The results obtained were compared to unperturbed (e.g. ref-73 erence) connectomes in both cases. The connectomes were 74 sampled 20 times per sample and once without perturbations, 75 resulting in a total of 8,400 connectomes. Two versions of 76 the unperturbed connectomes were generated and compared 77 such that the absence of variability aside from that induced 78 via MCA could be confirmed.

The stability of connectomes was evaluated through the 80 normalized percent deviation from reference⁴ and the num-81 ber of significant digits (Figure 1). The comparisons were 82 grouped according to differences across simulations, subsam-83 pling of data, sessions of acquisition, or subjects, and accord-84 ingly sorted from most to least similar. While the similarity 48 Prior to exploring the analytic impact of instabilities, a direct 85 of connectomes decreases as the collections become more dis-

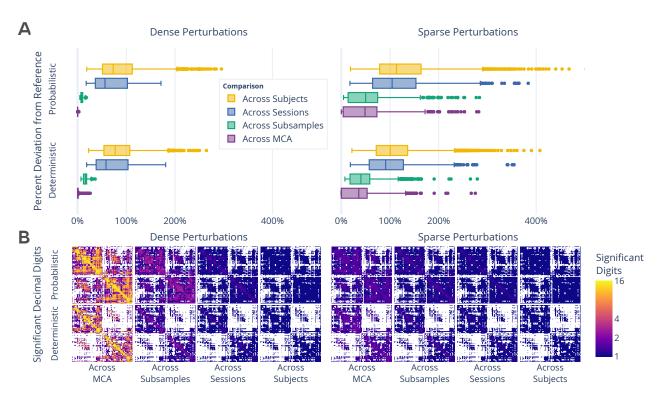


Figure 1. Exploration of perturbation-induced deviations from reference connectomes. (**A**) The absolute deviations between connectomes, in the form of normalized percent deviation from reference. The difference in MCA-perturbed connectomes is shown as the across MCA series, and is presented relative to the variability observed across subsamples, sessions, and subjects. (**B**) The number of significant decimal digits in each set of connectomes as obtained by evaluating the complete distribution of networks. In the case of 16, values can be fully relied upon, whereas in the case of 1 only the first digit of a value can be trusted. Dense and sparse perturbations are shown on the left and right, respectively.

the distinct MCA environments used suggests that the tested the description of the distinct MCA environments used suggests that the tested the pipelines may not suffer from single dominant sources of the pipelines may not suffer from single dominant sources of the pipelines instability, but that nevertheless there exist minor local interest that instabilities which may the propagate throughout the pipeline. The preference of the pipelines that instabilities inherent the pipelines, the pipelines may mask session or individual differences, the pipelines may mask session or individual differences, the pipelines when comparing networks across subsamplings to these pipelines show similar performance, the probabilistic that the pipeline was more stable in the face of dense perturbations the deterministic was more stable to sparse perturbations the deterministic was more stable to sparse perturbations the normalized percent deviation, the stability of correlations the normalized percent deviation, the stability of correlations the normalized percent deviation, the stability of correlations the propagate throughout the pipeline was make the determinant of the pipeline was more stable to sparse perturbations that the normalized percent deviation, the stability of correlations the pipeline that the normalized percent deviation, the stability of correlations that the normalized percent deviation is supplemental Section S1. The purpless of significant digits across individuals did not exceed the propagate throughout the propagate throughout the pipeline that the tested to the decrease across of the pipeline with the decrease along similarity between comparison of connectomes along similarity between comparison of connectomes along similarity between comparison of connectomes along similarity between comparison of connectomes. While the decrease along similarity between comparison of connectomes (Figure 1998) and the decrease al

118 average connectomes can be trusted. The combination of 154 indicating a dominant session-dependent signal for all indi-119 these results with those presented in Figure 1A suggests that 155 viduals despite no intended biological differences. However, 120 while specific edge weights are largely affected by instabili- 156 while still significant relative to chance (score: 0.85 and 0.88; ties, macro-scale network structure is stable.

122 Sparse Perturbations Reduce Off-Target Signal

125 the similarity of samples across sessions were compared to 126 distinct samples in the dataset (Table 1, with additional ex- 163 143 context-agnostic method for dataset augmentation.

While the discriminability of individuals is essential for 181 145 the identification of individual brain networks, it is similarly 182 ability to discriminate networks on the basis of meaningful bi-146 reliant on network similarity – or lack of discriminability – 183 ological signal alongside a reduction in discriminability due to 147 across equivalent acquisitions (Hypothesis 2). In this case, 184 of off-target signal in the sparse perturbation setting. This re-148 connectomes were grouped based upon session, rather than 185 sult appears strikingly like a manifestation of the well-known subject, and the ability to distinguish one session from an- 186 bias-variance tradeoff³² in machine learning, a concept which 150 other based on subsamples was computed within-individual 187 observes a decrease in bias as variance is favoured by a model. 151 and aggregated. Both the unperturbed and dense perturbation 188 In particular, this highlights that numerical perturbations can 152 settings perfectly preserved differences between sessions with 169 be used to not only evaluate the stability of pipelines, but that

p < 0.005 for both), sparse perturbations lead to significantly lower discriminability of the dataset (p < 0.005 for all). This 159 reduction of the difference between sessions suggests that We assessed the reproducibility of the dataset through mimick- 160 the added variance due to perturbations reduces the relative ing and extending a typical test-retest experiment²⁶ in which impact of non-biological acquisition-dependent bias inherent 162 in the networks.

Though the previous sets of experiments inextricably evalperiments and explanation of the measure and its scaling 164 uate the interaction between data acquisition and tool, the 128 in Supplemental Section S2). The ability to discriminate 165 use of subsampling allowed for characterizing the discrim-129 connectomes across subjects (Hypothesis 1) is an essential 166 inability of networks sampled from within a single acquisition prerequisite for the application of brain imaging towards iden- 167 (Hypothesis 3). While this experiment could not be evalu-131 tifying individual differences¹⁸. In testing hypothesis 1, we 168 ated using reference executions, the networks generated with observe that the dataset is discriminable with a scaled score of 169 dense perturbations showed near perfect discrimination be- $_{133}$ 0.82 (p < 0.001; optimal score: 1.0; chance: 0.04) for both $_{170}$ tween subsamples, with scores of 0.99 and 1.0 (p < 0.005; pipelines in the absence of MCA. We can see that inducing in- 171 optimal: 0.5; chance: 0.5). Given that there was no variability stabilities through MCA preserves the discriminability in the 172 in data acquisition, due to undesired effects such as participant dense perturbtion setting, and and discriminability decreased 173 motion, or preprocessing, the ability to discriminate between 137 slightly but remained above the unscaled reference value of 174 equivalent subsamples in this experiment may only be due 138 0.65 in the sparse case. This lack of significant decrease in 175 to instability or bias inherent to the pipelines. The high varidiscriminability across MCA perturbations suggests its utility 176 ability introduced through sparse perturbations considerably 140 for capturing variance within datasets without compromis- 177 lowered the discriminability towards chance (score: 0.71 and ing the robustness and reliability of the dataset as a whole, $178 \ 0.61$; p < 0.005 for all), further supporting this as an effecand possibly suggests this technique as a cost effective and 179 tive method for obtaining lower-bias estimates of individual 180 connectivity.

Across all cases, the induced perturbations maintained the 153 a score of 1.0 (p < 0.005; optimal score: 0.5; chance: 0.5), 190 the induced variance may be leveraged for the interpretation

Table 1. The impact of instabilities as evaluated through the discriminability of the dataset based on individual (or subject) differences, session, and subsample. The performance is reported as mean discriminability. While a perfectly discriminable dataset would be represented by a score of 1.0, the chance performance, indicating minimal discriminability, is 1/the number of classes. H_3 could not be tested using the reference executions due to too few possible comparisons. The alternative hypothesis, indicating significant discrimination, was accepted for all experiments, with p < 0.005.

			Unscaled Ref.		Scaled Ref.		Dense MCA		Sparse MCA	
Comparison	Chance	Target	Det.	Prob.	Det.	Prob.	Det.	Prob.	Det.	Prob.
<i>H</i> ₁ : Across Subjects	0.04	1.0	0.64	0.65	0.82	0.82	0.82	0.82	0.77	0.75
H_2 : Across Sessions	0.5	0.5	1.00	1.00	1.00	1.00	1.00	1.00	0.88	0.85
<i>H</i> ₃ : Across Subsamples	0.5	0.5					0.99	1.00	0.71	0.61

191 as a robust distribution of possible results.

193 Individual Statistics Are Not

195 is relevant for typical analyses, as low dimensional features are 221 stable for all comparisons (p < 0.0001; exploratory). In stark often more suitable than full connectomes for many analytical 222 contrast, sparse perturbations led to highly unstable featuremethods in practice 11. A separate subset of the NKIRS dataset 223 moments (Figure 2D), such that none contained more than was randomly selected to contain a single non-subsampled ses- 224 5 significant digits of information and several contained less 199 sion for 100 individuals ($100 \times 1 \times 1$) using the pipelines and 225 than a single significant digit, indicating a complete lack of re-200 instrumentation methods to generate connectomes as above. 226 liability. This dramatic degradation in stability for individual 201 Connectomes were generated 20 times each, resulting in a 227 measures strongly suggests that these features may be unre-202 dataset which also contained 8,400 connectomes with the 228 liable as individual biomarkers when derived from a single 203 MCA simulations serving as the only source of repeated mea- 229 pipeline evaluation, though their reliability may be increased 204 surements.

The stability of several commonly-used multivariate graph 231 ilar analysis was performed for univariate statistics which 2006 features 10 were explored and are presented in Figure 2. The 2002 obtained similar findings and can be found in Supplemental 207 cumulative density of the features was computed within in- 233 Section S3. 208 dividuals and the mean cumulative density and associated 209 standard error were computed for across individuals (Fig- 234 Uncertainty in Brain-Phenotype Relationships 214 tion modes.

217 (Figures 2C and 2D). In the face of dense perturbations, the 192 Distributions of Graph Statistics Are Reliable, But 218 feature-moments were stable with more than 10 significant 219 digits with the exception of edge weight when using the deter-194 Exploring the stability of topological features of connectomes 220 ministic pipeline, though the probabilistic pipeline was more 230 when studying their distributions across perturbations. A sim-

216 ity of the first 5 moments of these features was evaluated

210 ures 2A and 2B). There was no significant difference between 235 While the variability of connectomes and their features was 211 the distributions for each feature across the two perturbation 236 summarized above, networks are commonly used as inputs to 212 settings, suggesting that the topological features summarized 237 machine learning models tasked with learning brain-phenotype by these multivariate features are robust across both perturba-238 relationships 18. To explore the stability of these analyses, we 239 modelled the relationship between high- or low- Body Mass

In addition to the comparison of distributions, the stabil- 240 Index (BMI) groups and brain connectivity using standard di-

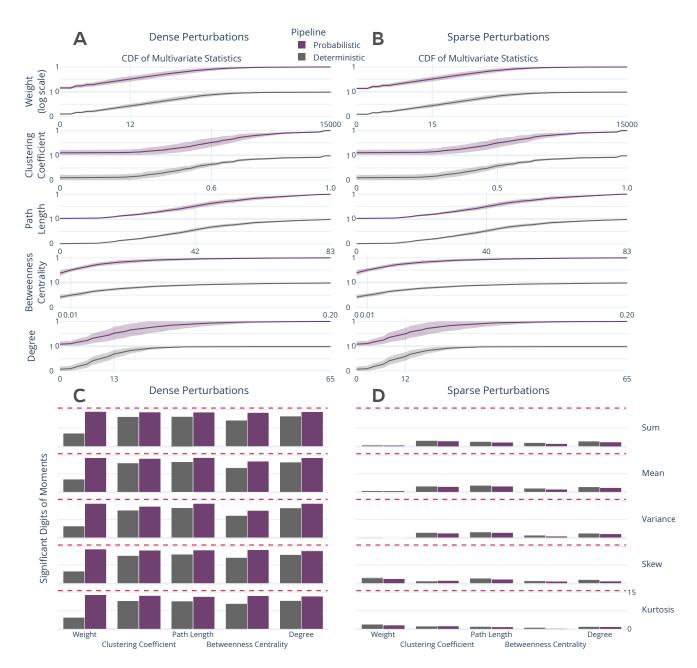


Figure 2. Distribution and stability assessment of multivariate graph statistics. (**A**, **B**) The cumulative distribution functions of multivariate statistics across all subjects and perturbation settings. There was no significant difference between the distributions in A and B. (**C**, **D**) The number of significant digits in the first 5 five moments of each statistic across perturbations. The dashed red line refers to the maximum possible number of significant digits.

mensionality reduction and classification tools ^{12, 13}, and com- ²⁴⁶ from 0.520 – 0.716 and 0.510 – 0.725, respectively, rang- ²⁴⁷ pared this to reference and random performance (Figure 3). ²⁴⁸ performance on the reference dataset. This large variability ²⁴⁸ The analysis was perturbed through distinct samplings of ²⁴⁹ illustrates a previously uncharacterized margin of uncertainty ²⁴⁹ the dataset across both pipelines and perturbation methods. ²⁴⁰ in the modelling of this relationship, and limits confidence in ²⁴⁰ The accuracy and F1 score for the perturbed models varied

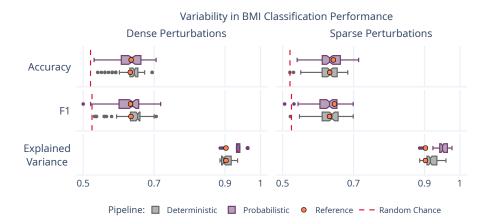


Figure 3. Variability in BMI classification across the sampling of an MCA-perturbed dataset. The dashed red lines indicate random-chance performance, and the orange dots show the performance using the reference executions.

251 reported accuracy scores on singly processed datasets. The 274 Discussion portion of explained variance in these samples ranged from 275 The perturbation of structural connectome estimation pipelines 257 suggest that modelling brain-phenotype relationships is not 260 ensemble modeling techniques.

272 preferred when processing datasets for eventual application in 295 the use of individual estimates. 273 modelling brain-phenotype relationships.

253 88.6% -- 97.8%, similar to the reference of 90.3%, suggest- 276 with small amounts of noise, on the order of machine error, 254 ing that the range in performance was not due to a gain or 277 led to considerable variability in derived brain graphs. Across 255 loss of meaningful signal, but rather the reduction of bias 278 all analyses the stability of results ranged from nearly per-256 towards specific outcome. Importantly, this finding does not 279 fectly trustworthy (i.e. no variation) to completely unreliable 280 (i.e. containing no trustworthy information). Given that the possible, but rather it sheds light on impactful uncertainty that 281 magnitude of introduced numerical noise is to be expected must be accounted for in this process, and supports the use of 282 in computational workflows, this finding has potentially sig-283 nificant implications for inferences in brain imaging as it is One distinction between the results presented here and 284 currently performed. In particular, this bounds the success of 262 the previous is that while networks derived from dense pertur- 285 studying individual differences, a central objective in brain bations had been shown to exhibit less dramatic instabilities 286 imaging 18, given that the quality of relationships between 264 in general, the results here show similar variability in clas- 287 phenotypic data and brain networks will be limited by the 265 sification performance across the two methods. This consis- 288 stability of the connectomes themselves. This issue is accen-266 tency suggests that the desired method of instrumentation may 289 tuated through the crucial finding that individually derived 267 vary across experiments. While sparse perturbations result 290 network features were unreliable despite there being no signif-268 in considerably more variability in networks directly, the two 291 icant difference in their aggregated distributions. This finding 269 techniques capture similar variability when relating networks 292 is not damning for the study of brain networks as a whole, but 270 to this phenotypic variable. Given the dramatic reduction 293 rather is strong support for the aggregation of networks, either 271 in computational overhead, a sparse instrumentation may be 294 across perturbations for an individual or across groups, over

> 296 Underestimated False Positive Rates While the instabil-297 ity of brain networks was used here to demonstrate the lim

298 itations of modelling brain-phenotype relationships in the 335 paradigm shift. Given that MCA is data-agnostic, this tech-299 context of machine learning, this limitation extends to classi- 396 nique could be used effectively in conjunction with, or in 300 cal hypothesis testing, as well. Though performing individual 337 lieu of, realistic noise models to augment existing datasets. 301 comparisons in a hypothesis testing framework will be accom-338 While this of course would not replace the need for repeated 302 panied by reported false positive rates, the accuracy of these 339 measurements when exploring the effect of data collection and rates is critically dependent upon the reliability of the samples and paradigm or study longitudinal progressions of development 304 used. In reality, the true false positive rate for a test would be 341 or disease, it could be used in conjunction with these efforts to 305 a combination of the reported confidence and the underlying 342 decrease the bias of each distinct sample within a dataset. In 306 variability in the results, a typically unknown quantity.

308 measure context, such as that afforded here through MCA, it 345 serve as an alternative solution to capture more biological vari-309 is impossible to empirically estimate the reliability of samples. 346 ability, with the added benefit being the savings of millions of This means that the reliability of accepted hypotheses is also 347 dollars on data collection. 311 unknown, regardless of the reported false positive rate. In 312 fact, it is a virtual certainty that the true false positive rate 313 for a given hypothesis exceeds the reported value simply as 314 a result of numerical instabilities. This uncertainty inherent 315 to derived data is compounded with traditional arguments 316 limiting the trustworthiness of claims³³, and hampers the 317 ability of researchers to evaluate the quality of results. The 318 accompaniment of brain imaging experiments with direct 319 evaluations of their stability, as was done here, would allow 320 researchers to simultaneously improve the numerical stability 321 of their analyses and accurately gauge confidence in them. 322 The induced variability in derived brain networks may be 323 leveraged to estimate aggregate connectomes with lower bias 324 than any single independent observation, leading to learned 325 relationships that are more generalizable and ultimately more 326 useful.

327 Cost-Effective Data Augmentation The evaluation of reli- 364 ability in brain imaging has historically relied upon the expen- 365 compare this to numerical instability. Recently, the nearly sive collection of repeated measurements choreographed by 366 boundless space of analysis pipelines and their impact on out-1331 turbing experiments using MCA both preserved the discrim- 368 approach taken in these studies complement one another and 332 inability of the dataset due to biological signal and decreased 369 explore instability at the opposite ends of the spectrum, with 333 the discriminability due to off-target differences across ac- 370 human variability in the construction of an analysis workflow 334 quisitions and subsamples opens the door for a promising 371 on one end and the unavoidable error implicit in the digital

343 contexts where repeated measurements are typically collected When performing these experiments outside of a repeated-344 to increase the fidelity of the dataset, MCA could potentially

> 348 Shortcomings and Future Questions Given the complex-349 ity of recompiling complex software libraries, pre-processing 350 was not perturbed in these experiments as the instrumentation 351 of the canonical workflow used in diffusion image process-352 ing would have added considerable technical complexity and 353 computational overhead to the large set of experiments per-354 formed here. Other work has shown that linear registration, a 355 core piece of many elements of pre-processing such as motion ³⁵⁶ correction and alignment, is sensitive to minor perturbations⁷. 357 It is likely that the instabilities across the entire processing 358 workflow would be compounded with one another, resulting 359 in even greater variability. While the analyses performed in 360 this paper evaluated a single dataset and set of pipelines, ex-361 tending this work to other modalities and analyses, alongside 362 the detection of local sources of instability within pipelines, 363 is of interest for future projects.

This paper does not explore methodological flexibility or massive cross-institutional consortia^{34,35}. The finding that per- 367 comes in brain imaging has been clearly demonstrated¹. The

372 representation of data on the other. It is of extreme interest 373 to combine these approaches and explore the interaction of 374 these scientific degrees of freedom with effects from software 375 implementations, libraries, and parametric choices.

377 presented here does not invalidate analytical pipelines used in 378 brain imaging, but merely sheds light on the fact that many 379 studies are accompanied by an unknown degree of uncertainty 380 due to machine-introduced errors. The presence of unknown error-bars associated with experimental findings limits the 382 impact of results due to increased uncertainty. The desired 383 outcome of this paper is to motivate a shift in scientific com-384 puting – both in neuroimaging and more broadly – towards a 385 paradigm that favours the explicit evaluation of the trustwor-386 thiness of claims alongside the claims themselves.

Methods

388 Dataset

389 The Nathan Kline Institute Rockland Sample (NKI-RS)²⁹ Finally, it is important to state explicitly that the work 390 dataset contains high-fidelity imaging and phenotypic data 391 from over 1,000 individuals spread across the lifespan. A 392 subset of this dataset was chosen for each experiment to both 393 match sample sizes presented in the original analyses and to 394 minimize the computational burden of performing MCA. The 395 selected subset comprises 100 individuals ranging in age from 396 6 - 79 with a mean of 36.8 (original: 6 - 81, mean 37.8), 397 60% female (original: 60%), with 52% having a BMI over 25 398 (original: 54%).

> Each selected individual had at least a single session 400 of both structural T1-weighted (MPRAGE) and diffusion-401 weighted (DWI) MR imaging data. DWI data was acquired 402 with 137 diffusion directions in a single shell; more informa-403 tion regarding the acquisition of this dataset can be found in 404 the NKI-RS data release²⁹.

> In addition to the 100 sessions mentioned above, 25 indi-406 viduals had a second session to be used in a test-retest analysis. 407 Two additional copies of the data for these individuals were 408 generated, including only the odd or even diffusion direc- $_{409}$ tions (64 + 9 B0 volumes = 73 in either case) such that the 410 acquired data was evenly represented across both portions, and each subsample represented a realistic complete acquisi-412 tion. This allowed for an extra level of stability evaluation to 413 be performed between the levels of MCA and session-level 414 variation.

> In total, the dataset is composed of 100 subsampled ses-416 sions of data originating from 50 acquisitions and 25 indi-417 viduals for in depth stability analysis, and an additional 100 418 sessions of full-resolution data from 100 individuals for sub-419 sequent analyses.

420 Processing

⁴²¹ The dataset was preprocessed using a standard FSL³⁶ work-422 flow consisting of eddy-current correction and alignment. The

423 MNI152 atlas³⁷ was aligned to each session of data via the 457 430 formed once without MCA, and thus is not being evaluated. 464 Random Rounding (RR).

Structural connectomes were generated from preprocessed 465 432 data using two canonical pipelines from Dipy³⁰: deterministic 466 many times to produce a distribution of results. Studying the and probabilistic. In the deterministic pipeline, a constant 467 distribution of these results can then lead to insights on the 434 solid angle model was used to estimate tensors at each voxel 468 stability of the instrumented tools or functions. To this end, and streamlines were then generated using the EuDX algo- 469 a complete software stack was instrumented with MCA and 436 rithm³¹. In the probabilistic pipeline, a constrained spherical 470 is made available on GitHub at https://github.com/ 437 deconvolution model was fit at each voxel and streamlines 471 Verificarlo/fuzzy. 438 were generated by iteratively sampling the resulting fiber orientation distributions. In both cases tracking occurred with 8 440 seeds per 3D voxel and edges were added to the graph based 442 fiber count.

443 444 yses. Fixing this random state led to entirely deterministic 445 repeated-evaluations of the tools, and allowed for explicit 446 attribution of observed variability to limitations in tool preci-447 sion as provoked by Monte Carlo simulations, rather than the 448 internal state of the algorithm.

Perturbations

450 All connectomes were generated with one reference execu-451 tion where no perturbation was introduced in the processing. 452 For all other executions, all floating point operations were 453 instrumented with Monte Carlo Arithmetic (MCA)⁸ through ⁴⁵⁴ Verificarlo⁹. MCA simulates the distribution of errors im-455 plicit to all instrumented floating point operations (flop). This 456 rounding is performed on a value x at precision t by:

where e_x is the exponent value of x and ξ is a uniform ran-424 structural images, and the resulting transformation was ap- 458 dom variable in the range $(-\frac{1}{2},\frac{1}{2})$. MCA can be introduced in 425 plied to the DKT parcellation³⁸. Subsampling the diffusion 459 two places for each flop: before or after evaluation. Perform-426 data took place after preprocessing was performed on full- 460 ing MCA on the inputs of an operation limits its precision, 427 resolution sessions, ensuring that an additional confound was 461 while performing MCA on the output of an operation high-428 not introduced in this process when comparing between down- 462 lights round-off errors that may be introduced. The former is 429 sampled sessions. The preprocessing described here was per- 463 referred to as Precision Bounding (PB) and the latter is called

Using MCA, the execution of a pipeline may be performed

The RR variant of MCA was used for all experiments. 473 As was presented in⁴, both the degree of instrumentation (i.e. 474 number of affected libraries) and the perturbation mode have on the location of terminal nodes with weight determined by 475 an effect on the distribution of observed results. For this work, 476 the RR-MCA was applied across the bulk of the relevant oper-The random state of both pipelines was fixed for all anal- 477 ations (those occurring in BLAS, LAPACK, Python, Cython, and Numpy) and is referred to as dense perturbation. In this 479 case the bulk of numerical operations were affected by MCA.

> Conversely, the case in which RR-MCA was applied across the operations in a small subset of operations (those 482 ocurring in Python and Cython) is here referred to as sparse 483 perturbation. In this case, the inputs to operations within 484 the instrumented libraries were perturbed, resulting in less 485 frequent, data-centric perturbations. Alongside the stated the-486 oretical differences, sparse perturbation is considerably less 487 computationally expensive than dense perturbation.

All perturbations targeted the least-significant-bit for all data (t = 24 and t = 53 in float 32 and float 64, respectively⁹). 490 Perturbing the least significant bit importantly serves as a 491 perturbation of machine error, and thus is the appropriate 492 precision to be applied globally in complex pipelines. Simula-(1) 493 tions were performed 20 times for each pipeline execution for

495 dataset. A detailed motivation for the number of simulations 528 intensity. A Pearson correlation coefficient 40 was computed 496 can be found in³⁹.

497 Evaluation

498 The magnitude and importance of instabilities in pipelines 499 can be considered at a number of analytical levels, namely: 500 the induced variability of derivatives directly, the resulting 501 downstream impact on summary statistics or features, or the 502 ultimate change in analyses or findings. We explore the na-503 ture and severity of instabilities through each of these lenses. 504 Unless otherwise stated, all p-values were computed using 505 Wilcoxon signed-rank tests. To avoid biasing these statistics in 506 this unique repeated-measures context, tests were performed ⁵⁰⁷ across sets of independent observations and then the results 508 were aggregated in all cases.

509 Direct Evaluation of the Graphs

measured directly through both a direct variance quantifica- 542 ing a direct measure of the tool-introduced variability across 512 tion and a comparison to other sources of variance such as 543 perturbations. A distribution was formed by aggregating these 513 individual- and session-level differences.

Graphs, in the form of adja- 545 Class-based Variability Evaluation To gain a concrete un-521 the reference graph, and is defined as⁴:

$$\%Dev(A,B) = \sqrt{\sum_{i=1}^{m} \sum_{j=1}^{n} |a_{ij} - b_{ij}|^2} / \sqrt{\sum_{i=1}^{m} \sum_{j=1}^{n} |a_{ij}|^2}, (2)$$

where A and B each represent a graph, and \square_{ij} are el-523 ements therein corresponding to row and column i and j, 554 see respectively. For these experiments, the A graph always refers set at observation j, where $i \neq i'$ and $j \neq j'$. $_{525}$ to the reference, where B represents a perturbed value. The $_{556}$

494 the 100 sample dataset and 10 times for the repeated measures 527 of differences in observed graphs relative to the original signal 529 in complement to normalized percent deviation to identify 530 the consistency of structure and not just intensity between observed graphs, though the result of this experiment is shown 532 only in Supplemental Section S1.

> Finally, the estimated number of significant digits, s', for 534 each edge in the graph is calculated as:

$$s' = -log_{10} \frac{\sigma}{|\mu|} \tag{3}$$

where μ and σ are the mean and unbiased estimator of 536 standard deviation across graphs, respectively. The upper 537 bound on significant digits is 15.7 for 64-bit floating point 538 data.

The percent deviation, correlation, and number of signifi-540 cant digits were each calculated within a single session of data, The differences between perturbation-generated graphs was 541 thereby removing any subject- and session-effects and provid-544 individual results.

515 cency matrices, were compared to one another using three 546 derstanding of the significance of observed variations we exmetrics: normalized percent deviation, Pearson correlation, 547 plore the separability of our results with respect to understood and edgewise significant digits. The normalized percent devi- 548 sources of variability, such as subject-, session-, and pipelineation measure, defined in⁴, scales the norm of the difference 549 level effects. This can be probed through Discriminability²⁶, between a simulated graph and the reference execution (that 550 a technique similar to ICC²⁴ which relies on the mean of a 520 without intentional perturbation) with respect to the norm of 551 ranked distribution of distances between observations belong-552 ing to a defined set of classes. The discriminability statistic is 553 formalized as follows:

$$Disc. = Pr(\|g_{ij} - g_{ij'}\| \le \|g_{ij} - g_{i'j'}\|)$$
 (4)

where g_{ij} is a graph belonging to class i that was measured

Discriminability can then be read as the probability that an 526 purpose of this comparison is to provide insight on the scale 557 observation belonging to a given class will be more similar to 559 ferent class. It is a measure of reproducibility, and is discussed 594 been presented in the main body of this article. Correction for 560 in detail in²⁶. This definition allows for the exploration of de-595 repeated testing was performed. viations across arbitrarily defined classes that in practice can 562 be any of those listed above. We combine this statistic with 563 permutation testing to test hypotheses on whether differences between classes are statistically significant in each of these set-565 tings. This statistic is similar to ICC²⁴ in a two-measurement setting, however, given the dependence on a rank distribution 567 from all measurements, discriminability scores do not become meaningless by the addition of more samples which are highly similar to the originals, whereas ICC scores would much more 570 rapidly trend towards 1, making discriminability appropriate 571 in this context. The scaling properties of discriminability are 572 described more fully in Supplemental Section S2.

578 dently for each pipeline and perturbation mode.

 H_{A1} : Individuals are distinct from one another Class definition: Subject ID 580 Comparisons: Session (1 subsample), Subsample (1 581 session), MCA (1 subsample, 1 session)

583 H_{A2} : Sessions within an individual are distinct Class definition: Session ID | Subject ID 584 Comparisons: Subsample, MCA (1 subsample)

586 H_{A3} : Subsamples are distinct Class definition: Subsample | Subject ID, Session ID 587 Comparisons: MCA 588

590 periments and 3 reference experiments on 2 pipelines and 2 626 gated across individuals. The number of significant digits 591 perturbation modes, resulting in a total of 30 distinct tests. 627 for each moment of these distributions (sum, mean, variance,

558 other observations within that class than observations of a dif- 593 Section S2, only the bolded comparisons in the list above have

596 Evaluating Graph-Theoretical Metrics

597 While connectomes may be used directly for some analyses, 598 it is common practice to summarize them with structural mea-599 sures, that can then be used as lower-dimensional proxies 600 of connectivity in so-called graph-theoretical studies¹¹. We 601 explored the stability of several commonly-used univariate 602 (graphwise) and multivariate (nodewise or edgewise) features. 603 The features computed and subsequent methods for comparison in this section were selected to closely match those com-605 puted in¹⁰.

606 Univariate Differences For each univariate statistic (edge With this in mind, three hypotheses were defined. For 607 count, mean clustering coefficient, global efficiency, modu-574 each setting, we state the alternate hypotheses, the variable(s) 608 larity of the largest connected component, assortativity, and 575 which were used to determine class membership, and the 609 mean path length) a distribution of values across all perturba-576 remaining variables which may be sampled when obtaining 610 tions within subjects was observed. A Z-score was computed ₅₇₇ multiple observations. Each hypothesis was tested indepen-₆₁₁ for each sample with respect to the distribution of feature 612 values within an individual, and the proportion of "classically significant" Z-scores, i.e. corresponding to p < 0.05, was 614 reported and aggregated across all subjects. There was no 615 correction for multiple comparisons in these statistics, as they 616 were not used to interpret a hypothesis but demonstrate the false-positive rate due to perturbations. The number of signifi-618 cant digits contained within an estimate derived from a single 619 subject were calculated and aggregated. The results of this 620 analysis can be found in Supplemental Section S3.

621 Multivariate Differences In the case of both nodewise (de-622 gree distribution, clustering coefficient, betweenness central-623 ity) and edgewise (weight distribution, connection length) fea-624 tures, the cumulative density functions of their distributions As a result, we tested 3 hypotheses across 6 MCA ex- 625 were evaluated over a fixed range and subsequently aggre-592 While results from all tests can be found within Supplemental 628 skew, and kurtosis) were calculated across observations within

629 a sample and aggregated.

630 Evaluating A Brain-Phenotype Analysis

631 Though each of the above approaches explores the instabil-632 ity of derived connectomes and their features, many modern 633 studies employ modeling or machine-learning approaches, for 634 instance to learn brain-phenotype relationships or identify dif-635 ferences across groups. We carried out one such study and ex-636 plored the instability of its results with respect to the upstream 637 variability of connectomes characterized in the previous sec-638 tions. We performed the modeling task with a single sampled 639 connectome per individual and repeated this sampling and 640 modelling 20 times. We report the model performance for each sampling of the dataset and summarize its variance.

642 **BMI Classification** Structural changes have been linked to 652 the training set for each fold within the cross validation of 688 Concordia.ca. 653 the original graphs; this resulted in a feature of 20 compo-654 nents. We trained the model using k-fold cross validation, with k = 2, 5, 10, and N (equivalent to leave-one-out; LOO).

656 Data & Code Provenance

658 of Reliability and Reproducibility (http://fcon_1000.694 ship with Health Canada, for the Canadian Open Neuroscience 659 projects.nitrc.org/indi/enhanced/), including 695 Platform initiative. 660 both the imaging data as well as phenotypic data which may be obtained upon submission and compliance with a Data Us- 696 References age Agreement. The connectomes generated through simula- $_{663}$ tions have been bundled and stored permanently (https:// 664 doi.org/10.5281/zenodo.4041549), and are made 700

665 available through The Canadian Open Neuroscience Platform 666 (https://portal.conp.ca/search, search term "Kiar"). All software developed for processing or evaluation is 668 publicly available on GitHub at https://github.com/ 669 gkpapers/2020ImpactOfInstability. Experiments 670 were launched using Boutiques⁴² and Clowdr⁴³ in Compute 671 Canada's HPC cluster environment. MCA instrumentation 672 was achieved through Verificarlo⁹ available on Github at 673 https://github.com/verificarlo/verificarlo. 674 A set of MCA instrumented software containers is available 675 **on Github at** https://github.com/gkiar/fuzzy.

676 Author Contributions

677 GK was responsible for the experimental design, data pro-678 cessing, analysis, interpretation, and the majority of writing. obesity in adolescents and adults⁴¹. We classified normal- 679 All authors contributed to the revision of the manuscript. YC, ead weight and overweight individuals from their structural net- 680 POC, and EP were responsible for MCA tool development and works (using for overweight a cutoff of BMI $> 25^{13}$). We 681 software testing. AR, GV, and BM contributed to experimentally reduced the dimensionality of the connectomes through prin- 682 tal design and interpretation. TG contributed to experimental cipal component analysis (PCA), and provided the first N- 683 design, analysis, and interpretation. TG and ACE were re-648 components to a logistic regression classifier for predicting 684 sponsible for supervising and supporting all contributions BMI class membership, similar to methods shown in 12,13. 685 made by GK. The authors declare no competing interests for 650 The number of components was selected as the minimum set 686 this work. Correspondence and requests for materials should $_{ text{651}}$ which explained > 90% of the variance when averaged $_{ text{across}}$ $_{ text{687}}$ be addressed to Tristan Glatard at tristan.glatard@

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S1. Graph Correlation

The following presents a quantification of deviations of generated connectomes from the reference execution, similar to shown in Figure 1. However, in this case, the "percent deviation" measure was replaced with the Pearson correlation coefficient. The correlations between observed graphs (Figure S1) across each grouping follow the same trend to as percent deviation, as shown in Figure 1. However, notably different from percent deviation, there is no significant difference in the correlations between dense or sparse instrumentations. By this measure, the probabilistic pipeline is more stable in all cross-MCA and cross-directions except for the combination of sparse perturbation and cross-MCA (p < 0.0001 for all; exploratory).

The marked lack in drop-off of performance across these settings, inconsistent with the measures show in Figure 1 is likely due to the nature of the measure and the structure of graphs being compared. Given that structural graphs are sparse and contain considerable numbers of zero-weighted edges, the presence or absense of edges dominated the correlation measure where it was less impactful for the others. For this reason and others 44, correlation is not a commonly used measure in the context of structural connectivity, and thus this analysis was demoted to the supplement material.

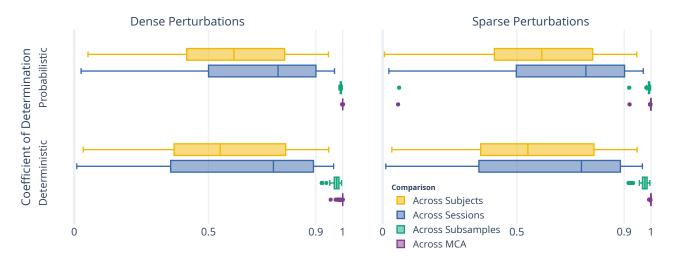


Figure S1. The correlation between perturbed connectomes and their reference.

S2. Complete Discriminability Analysis

Table S1. The complete results from the Discriminability analysis, with results reported as mean \pm standard deviation Discriminability. As was the case in the condensed table, the alternative hypothesis, indicating significant separation across groups, was accepted for all experiments, with p < 0.005.

				Unscaled Re	eference	Dense Pertu	rbations	Sparse Perturbations		
Exp.	Subj.	Sess.	Samp.	Det.	Prob.	Det.	Prob.	Det.	Prob.	
1.1	All	All	1	0.64 ± 0.00	0.65 ± 0.00	0.82 ± 0.00	0.82 ± 0.00	0.77 ± 0.00	0.75 ± 0.00	
1.2	All	1	All	1.00 ± 0.00	1.00 ± 0.00	1.00 ± 0.00	1.00 ± 0.00	0.93 ± 0.02	0.90 ± 0.02	
1.3	All	1	1			1.00 ± 0.00	1.00 ± 0.00	0.94 ± 0.02	0.90 ± 0.02	
2.4	1	All	All	1.00 ± 0.00	1.00 ± 0.00	1.00 ± 0.00	1.00 ± 0.00	0.88 ± 0.12	0.85 ± 0.12	
2.5	1	All	1			1.00 ± 0.00	1.00 ± 0.00	0.89 ± 0.11	0.84 ± 0.12	
3.6	1	1	All			0.99 ± 0.03	1.00 ± 0.00	0.71 ± 0.07	0.61 ± 0.05	

The complete discriminability analysis includes comparisons across more axes of variability than the condensed version.
The reduction in the main body was such that only axes which would be relevant for a typical analysis were presented. Here,
each of Hypothesis 1, testing the difference across subjects, and 2, testing the difference across sessions, were accompanied
with additional comparisons to those shown in the main body.

Subject Variation Alongside experiment 1.1, that which mimicked a typical test-retest scenario, experiments 1.2 and 1.3 could be considered a test-retest with a handicap, given a single acquisition per individual was compared either across subsamples or simulations, respectively. For this reason, it is unsurprising that the dataset achieved considerably higher discriminability scores.

Session Variation Similar to subject variation, the session variation was also modelled across either both or a single subsample in experiments 2.4 and 2.5. In both of these cases the performance was similar, and the finding that sparse perturbations reduced the off-target signal was consistent.

863 S2.1 Scaling of discriminability with N

When samples were added to the dataset across perturbed executions, the discriminability statistic inflated to a plateau even when no information was added (e.g. the dataset was replicated). This effect is demonstrated for the reference executions and is shown in Figure S2. As we can see, the reference discriminability scores without data duplication (unscaled) were 0.64 and 0.65 for the deterministic and probabilistic pipelines, respectively. After duplicating the dataset 20 times, matching the size of the 20-sample perturbed dataset, we can see that this (scaled) score plateaus at 0.82 for both pipelines. For consistency, in the main body of the text the reference execution performance was communicated as the scaled quantity.

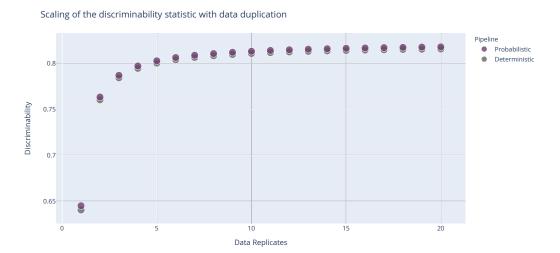


Figure S2. Scaling behaviour of the discriminability statistic with data duplication.

S3. Univariate Graph Statistics

Figure S3 explores the stability of univariate graph-theoretical metrics computed from the perturbed graphs, including modularity, global efficiency, assortativity, average path length, and edge count. When aggregated across individuals and perturbations, the distributions of these statistics (Figures S3A and S32B) showed no significant differences between perturbation methods for either deterministic or probabilistic pipelines, consistent with the comparison of the cumulative density of the multivariate statistics compared in 2.

However, when quantifying the stability of these measures across connectomes derived from a single session of data, the two perturbation methods show considerable differences. The number of significant digits in univariate statistics for dense perturbation instrumented connectome generation exceeded 11 digits for all measures except modularity, which contained more than 4 significant digits of information (Figure S3C). When detecting false-positives from the distributions of observed statistics for a given session, the rate (using a threshold of p = 0.05) was approximately 2% for all statistics with the exception of modularity which again was less stable with an approximately 10% false positive rate. The probabilistic pipeline is significantly evaluating these features from connectomes generated in the sparse perturbation setting, no statistic was stable with more than significant digits or a false positive rate lower than nearly 6% (Figure S3D). The deterministic pipeline was more stable than the probabilistic pipeline in this setting (p < 0.0001; exploratory).

Two notable differences between the two perturbation methods are, first, the uniformity in the stability of the statistics, and second, the dramatic decline in stability of individual statistics in the sparse perturbation setting despite the consistency in the overall distribution of values. This result is consistent with that obtained from the multivariate exploration performed in the body of this article. It is unclear at present if the discrepancy between the stability of modularity in the pipeline perturbation context versus the other statistics suggests the implementation of this measure is the source of instability or if it is implicit to the measure itself. The dramatic decline in the stability of features derived from sparse perturbed graphs despite no difference in their overall distribution both shows that while individual estimates may be unstable the comparison between aggregates or groups may be considered much more reliable; this finding is consistent with that presented for multivariate statistics.

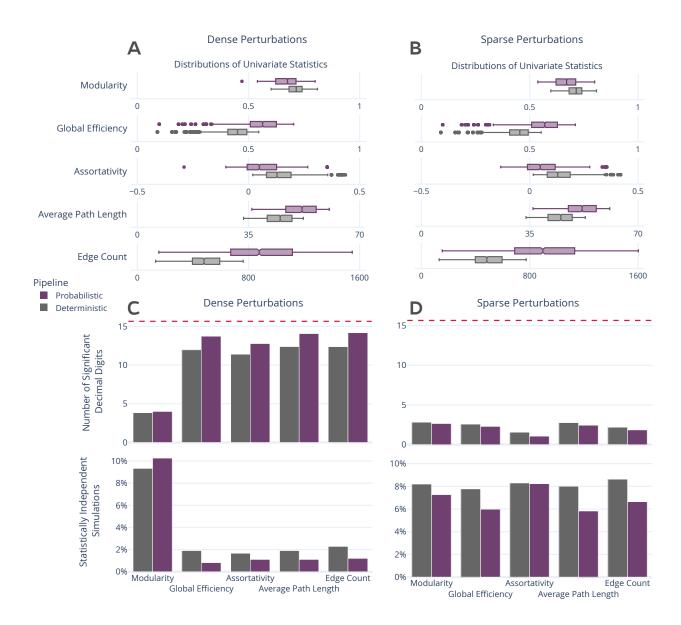


Figure S3. Distribution and stability assessment of univariate graph statistics. (**A**, **B**) The distributions of each computed univariate statistic across all subjects and perturbations for dense and sparse settings, respectively. There was no significant difference between the distributions in A and B. (**C**, **D**; top) The number of significant decimal digits in each statistic across perturbations, averaged across individuals. The dashed red line refers to the maximum possible number of significant digits. (**C**, **D**; bottom) The percentage of connectomes which were deemed significantly different (p < 0.05) from the others obtained for an individual.