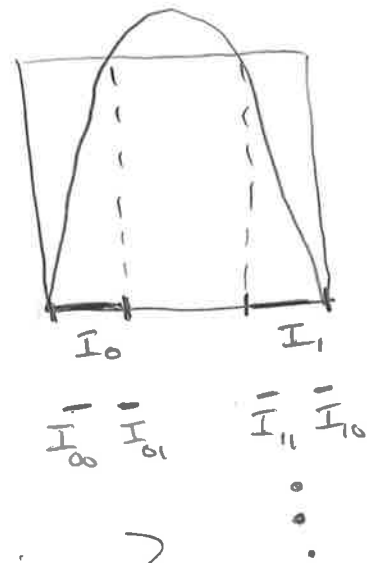


Recall for $n > 2 + \sqrt{5}$

$$|F'_n(x)| > 2 > 1 \quad x \in I_0 \cup I_2$$



$$I_{s_0 \dots s_n} \stackrel{\text{def.}}{=} \{x \in [0,1] \mid F^j(x) \in I_{s_j} \quad 0 \leq j \leq n\}$$

Closed interval.

$$I_{s_0 \dots s_{n+1}} \subset I_{s_0 \dots s_n} \quad \text{nested closed intervals}$$

$$\text{length}(I_{s_0 \dots s_n}) < \frac{1}{\lambda^{n+1}}$$

Let $x \in \Lambda$

$S(x) \in \Sigma_2$ $S(x) = (s_0, s_1, \dots)$ "Itinerary for x ".

$$F^j(x) \in I_{s_j} \quad j \geq 0$$

$$X \in I_{s_0, s_n} \quad \forall n \geq 0$$

$$\text{So } x \in \bigcap_{n \geq 0} I_{s_0 \dots s_n}$$

But $\left\{ I_{s_0 \dots s_n} \right\}_{n=0}^{\infty}$ is a nested sequence of non-empty closed intervals whose diameters shrink to zero

so $\bigcap_{n \geq 0} I_{s_0 \dots s_n}$ is a singleton.

In fact, $\bigcap_{n \geq 0} I_{s_0 \dots s_n} = \{x\}$

which we will identify with x when convenient.

Theorem 1.7.2 $S: \Lambda \rightarrow \Sigma_2$ is a homeomorphism

Theorem 1.7.3 $S \circ F_u = \sigma \circ S$

so S is a topological conjugacy twist $F_u \stackrel{S}{\mapsto} \sigma$

so The dynamics of $F: \Lambda \rightarrow \Lambda$ are exactly the same as $\sigma: \Sigma_2 \rightarrow \Sigma_2$