# **Session 3**

Multi-population Hui-Walter models

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### Recap

- Fitting models using MCMC is easy with JAGS / runjags
- But we must never forget to check convergence and effective sample size!
- More complex models become easy to implement
  - For example imperfect diagnostic tests, and Hui-Walter models
  - But remember to be realistic about what is possible with your data
  - Also carefully consider the influence of your priors

Multi-population Hui-Walter models

### Hui-Walter models with multiple populations

- Basically an extension of the single-population model
- Works best with multiple populations each with differing prevalence
  - Including an unexposed population works well
  - BUT be wary of assumptions regarding constant sensitivity/specificity across populations with very different types of infections

### Different prevalence in different populations

```
model{
  for(p in 1:Populations){
    Tally[1:4, p] ~ dmulti(prob[1:4, p], TotalTests[p])
    # Test1- Test2- Pop1
    prob[1, p] <- (prev[p] * ((1-se[1])*(1-se[2]))) + ((1-prev[p]) *
\hookrightarrow ((sp[1])*(sp[2])))
    ## snip ##
   prev[p] ~ dbeta(1, 1)
  se[1] ~ dbeta(se_prior[1,1], se_prior[1,2])T(1-sp[1], )
  sp[1] ~ dbeta(sp_prior[1,1], sp_prior[1,2])
  se[2] ~ dbeta(se_prior[2,1], se_prior[2,2])T(1-sp[2], )
  sp[2] ~ dbeta(sp_prior[2,1], sp_prior[2,2])
  #data# Tally, TotalTests, Populations, se prior, sp prior
  #monitor# prev, prob, se, sp
  #inits# prev, se, sp
```

### Multiple populations: assumptions

- We typically assume that the sensitivity and specificity must be consistent between populations
  - Do you have an endemic and epidemic population?
  - Or vaccinated and unvaccinated?
  - If so then the assumptions might not hold!

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- We typically assume that the sensitivity and specificity must be consistent between populations
  - Do you have an endemic and epidemic population?
  - Or vaccinated and unvaccinated?
  - If so then the assumptions might not hold!
- The populations can be artificial (e.g. age groups) but must not be decided based on the diagnostic test results
  - It helps if the prevalence differs between the populations

### Multiple populations: special cases

- A small disease-free group is extremely helpful
  - Contains strong data regarding specificity
  - As long as specificity can be assumed to be the same in the other populations

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- A small disease-free group is extremely helpful
  - Contains strong data regarding specificity
  - As long as specificity can be assumed to be the same in the other populations
- A small experimentally infected group MAY be helpful but it is often dangerous to assume that sensitivity is consistent!

#### **Initial values**

We have to be careful to make sure that the length of initial values for prev in each chain is equal to the number of populations

For example with 5 populations we need:

```
prev <- list(chain1=c(0.1, 0.1, 0.1, 0.9, 0.9), chain2=c(0.9, 0.9, 0.9, \hookrightarrow 0.1, 0.1))
```

#### **Initial values**

We have to be careful to make sure that the length of initial values for prev in each chain is equal to the number of populations

For example with 5 populations we need:

The values you choose for different populations in the same chain can be the same - just make sure you pick different values for the same population between chains (i.e. *over-dispersed* initial values)

Note: specifying your own initial values is technically optional with JAGS, but it is always a good idea (for now at least)!!!

### Incorporating populations with known prevalence

Up to now prevalence has been a parameter, but it can also be (partially) observed:

```
model{
  for(p in 1:Populations){
    Tally[1:4, p] ~ dmulti(prob[1:4, p], TotalTests[p])
    # Test1- Test2- Pop1
      prob[1, p] <- (prev[p] * ((1-sensitivity[1])*(1-sensitivity[2])))</pre>
\hookrightarrow + ((1-prev[p]) * ((sp[1])*(sp[2])))
    ## snip ##
   prev[p] ~ dbeta(1, 1)
  ## snip ##
  #data# Tally, TotalTests, Populations, se prior, sp prior, prev
  #monitor# prev, prob, se, sp
  #inits# prev, se, sp
```

To fix the prevalence of population 1 we could do:

```
Populations <- 5
prev <- rep(NA, Populations)
prev[1] <- 0
prev
## [1] O NA NA NA NA
```

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```
Populations <- 5
prev <- rep(NA, Populations)
prev[1] <- 0
prev
## [1] 0 NA NA NA NA
```

But you also need to account for this in the initial values:

Note: we now have two definitions of prev in R!

### Data and initial value lists

There are actually multiple ways to specify data and initial values to runjags, including via the data and inits arguments

We will use these to keep separate lists of data and initial values (these could also be data frames, or environments)

```
data <- list(
  Tally = Tally,
  TotalTests = apply(Tally, 2, sum),
  Populations = dim(Tally, 2),
  prev = rep(NA, Populations),
  se_prior = matrix(1, ncol=2, nrow=2),
  sp_prior = matrix(1, ncol=2, nrow=2))
data$prev[1] <- 0</pre>
```

```
inits <- list(</pre>
  chain1 = list(
   prev = c(NA, 0.1, 0.1, 0.9, 0.9),
   se = c(0.5, 0.99),
    sp = c(0.5, 0.99)
  ),
  chain2 = list(
    prev = c(NA, 0.9, 0.9, 0.1, 0.1),
    se = c(0.99, 0.5),
    sp = c(0.99, 0.5)
results <- run.jags(..., data = data, inits = inits)
```

```
inits <- list(
 chain1 = list(
   prev = c(NA, 0.1, 0.1, 0.9, 0.9),
   se = c(0.5, 0.99),
   sp = c(0.5, 0.99)
 ),
 chain2 = list(
   prev = c(NA, 0.9, 0.9, 0.1, 0.1),
   se = c(0.99, 0.5),
   sp = c(0.99, 0.5)
results <- run.jags(..., data = data, inits = inits)
```

See the help file for ?run.jags for more details

### Other runjags options

There are a large number of other options to runjags. Some highlights:

- The method can be parallel or background or bgparallel
- You can use extend.jags to continue running an existing model (e.g. to increase the sample size)
- You can use coda::as.mcmc.list to extract the underlying MCMC chains
- Use the summary() method to extract summary statistics
  - See ?summary.runjags and ?runjagsclass for more information

### Using embedded character strings

For simple models we might not want to bother with an external text file. Then we can do:

```
model_string <- "
model{
  Positives ~ dbinom(prevalence, TotalTests)
  prevalence ~ dbeta(1, 1)
  #data# Positives. TotalTests
  #monitor# prevalence
  #inits# prevalence
Positives <- 7
TotalTests <- 10
prevalence <- list(chain1=0.01, chain2=0.99)</pre>
results <- run.jags(model string, n.chains=2)
```

But I would advise that you stick to using a separate text file!

## Setting the RNG seed

If we want to get numerically replicable results we need to add .RNG.name and .RNG.seed to the initial values, and an additional #modules# lecuyer hook to our model definition:

```
model{
  Positives ~ dbinom(prevalence, TotalTests)
  prevalence ~ dbeta(2, 2)

#data# Positives, TotalTests
#monitor# prevalence
#inits# prevalence, .RNG.name, .RNG.seed
#modules# lecuyer
}
```

Then we can propogate R's RNG to JAGS like so:

```
set.seed(2021-06-29)
.RNG.name <- "lecuyer::RngStream"
.RNG.seed <- list(chain1=sample.int(1e6, 1), chain2=sample.int(1e6, 1)))
results <- run.jags(model_string, n.chains=2)</pre>
```

# Practical session 3

### Points to consider

- 1. What are the benefits of including multiple populations?
- 2. How can we define/obtain these populations?
- 3. What happens if our fundamental assumptions about consistent Se/Sp are broken?

### Summary

- Multiple populations helps to estimate Se and Sp
  - Particularly if the prevalences differ
  - A large number of populations with small N may be better as a random effect
- Populations may be artificial
  - But cannot be based on the result of either test
- But if Se / Sp are inconsistent then we will get misleading results
  - In practice, groups with widely varying prevalence rarely have consistent Se / Sp
  - It is possible to allow Se / Sp to differ between populations, but then there is no benefit of combining the data