Chapters 3 + 4 (DRAFT - 3/1/16)

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1 Introducing Neural Networks

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I will now shift focus to supervised learning of the chorales using both non-recurrent and recurrent neural models, seeking to improve upon the baseline models presented in Chapter 2. Neural networks are able to engage in sophisticated decision-making by passing the input forward through the network and making more complex and abstract decisions in the hidden perceptron layers. As demonstrated in the literature review at the beginning of Chapter 2, neural networks are popular in computational musicology for their ability to perform highly complex pattern recognition over large datasets and generalize when given unexpected input patterns. In particular, recurrent neural networks (RNNs) show great promise in sequence labelling because of their ability to incorporate contextual information 13 about previous computations. In the case of musical harmony and the task of next-step harmonic prediction, it is critical to understand the local harmonic progression in order to sense the direction of the music. All chords except the tonic generate a sense of tension that insist upon a goal of resolving to the tonic. Therefore, I hypothesize that is critical for the model to understand the tension generated by previous output harmonies when predicting the next harmony. This hypothesis will be evaluated by use of an "Oracle experiment."

2 Non-Recurrent Models

The "vanilla" neural network chosen as the non-recurrent model was implemented in Lua 21 using torch7 library. The network has 3 layers, with one layer of varying sizes that was 22 adjusted on the basis of evaluation on a validation set. The validation set consisted of 33 23 chorales randomly extracted from the training set. A lookup table was added as a layer of 24 convolution that takes the input as a vector of indexed features and outputs a matrix where 25 each column represents an embedding for a feature in the original input. After passing 26 through the hidden layer, the intermediate output is transformed by a softmax to output a 27 probability distribution over all possible output classes. The criterion used was negative 28 log likelihood (NLL), and an NLL value closer to 0 indicates how strongly the model the correct class as its prediction. The objective is to minimize negative log likelihood during training. 31

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For each subtask, this model was trained on the same input data X and output data Y used in Chapter 2 after GCT was introduced to replace Roman numeral classification. The number of output class for each subtask were 12, 130, 4, 12, and 12, respectively. These models all trained in under a minute, requiring no more than 10 epochs to reach convergence. NLL was reported as an average of over all inputs in the training and test sets.

Table 1: "Vanilla" neural network accuracy.

Task	Training NLL	Acc%	Test NLL	Acc%
Root	0.865	68.92%	1.106	60.86%
Base	1.402	62.10%	1.686	57.83%
Inversion	0.675	73.26%	0.785	69.67%
Alto	1.473	59.22%	1.710	56.27%
Tenor	1.320	52.91%	1.751	40.05%

Update these values. They might have been from the Oracle experiment and were mislabeled.

40 2.1 Full Harmonization

The baseline models and the neural network were also trained on the "full harmonization task", where the output represented a full set of decisions for all subtasks. Each full set of decisions in the training set is assigned a unique class index. For the test set, only inputs that map to an index in the training set are used. To understand why, imagine a model that took an image as input and predicted whether the image depicted a cat, dog, or bird. If during training the model, only images of cats and dogs are shown, then the model will gradually adjust its weights to reflect the fact that bird is never right answer. Therefore, if the model is tested on an image of a bird, it is extremely improbable that the model will guess correctly because of the data it was trained on. Similarly, the neural network will not guess the correct full harmonization class if it never appeared during training.

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The network was trained until convergence around 20 epochs, and the code is in the script eval-sm.lua. Random forests and neural networks continue to outperform the other models, although Random forests consistently achieving a slightly higher accuracy. The results for multinomial naive Bayes, the worst performer on average, were therefore left out.

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Table 2: "Vanilla" neural network accuracy, full harmonization task.

Classifier	Test NLL	Acc%
Multiclass Logistic	_	6.26%
Random Forest	_	31.35%
Neural Network	4.614	26.35%

There are two significant flaws to this approach. First, the accuracy metric here is harsh because by combining a series of decisions into a single class, a much more fine-grained decision must be made to choose the correct class. This could be improved by creating a more sophisticated accuracy metric that took into account its overall accuracy across all subtasks. Second, I hypothesized that the model would be improved significantly if after

the model output a decision for a subtask that that information would be provided as part of the input for the next subtask. This hypothesis reflects the musician's method of harmonization, where, for example, knowing that the next chord should be in terms of its root and base will significantly influence the selection of the alto and tenor pitches.

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A new approach was therefore taken for deciding a full harmonization at each time step.

Figure 1 shows the sequence of decisions that comprises the complete harmonic decision

for a given time step. This decision process acknowledges the *dependent* nature of the

subtasks, and therefore the ordering of their completion influences the model performance.

This ordering decides the harmony in the two subtasks, while the final three decide the

specific notes to voice that harmony. The final two are hypothesized to be interchangeable,

since the Alto and Tenor voices are traditionally inner voices are relatively equal weight.

Let's assume for the sake of shorthand that there are only three subtasks. Then the objective is to select

$$\underset{x,y,z}{\arg\max} P(X=x,Y=y,Z=z|\boldsymbol{X})$$

where X, Y, and Z are each random variables associated with a specific subtask and can only have the value of a class belonging to the variable's subtask, and X represents the initial input data. Let $\hat{x}, \hat{y}, \hat{z}$ be the predicted classes for the 3 subtasks. By the chain rule, we can show that Then by the chain rule,

$$\begin{split} \hat{x}, \hat{y}, \hat{z} &= \argmax_{x,y,z} P(X = x, Y = y, Z = z | \textbf{X}) \\ &= \argmax_{x,y,z} P(X = x | \textbf{X}, Y = y, Z = z) \cdot P(Y = y | \textbf{X}, Z = z) \cdot P(Z = z | \textbf{X}) \end{split}$$

More work needs to be done to evaluate this model and ensure it is working probably.

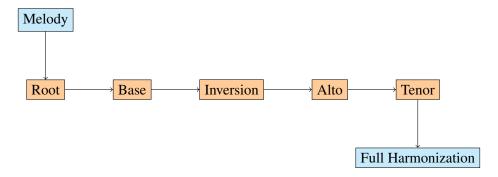
During training, the each subtask is fed the original input data along with the correct classes

for the previous subtasks in the sequence. During test time, its decision for each subtask is

propagated through future decisions. The possible choices of x, y, z are selected from the

combinations of outputs seen in the training set. But as of now, this model achieves around 40% accuracy across subtasks.

Figure 1: Sequence of harmonization subtasks with dependent decision making.



Before, applying RNNs to this task, I wanted to know if having the context of previous

81 3 Recurrent Models

3.1 Oracle experiment

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harmonies would in fact improve the model. An Oracle experiment is so-called termed 84 in the field of natural language processing because there is the addition of an "oracle" 85 in the data that always provides the correct answer. It is used to compare one system to another system by including the "oracle" and evaluating how your model responds when 87 one component of it always provides the correct answer. Such an experiment is performed 88 here to determine whether the neural model presented in the previous section will perform better with this knowledge. If so, it would strongly suggest that the context provided by a 90 recurrent model would improve results. 91 In featurize.py, the final three columns of X describe the correct harmony (root, 92 base, and inversion) at time step t-1. This information simulates the additional informa-93 tion provided in a recurrent model from the computation at the previous time step. The 94 baseline models were re-evaluated on this dataset as well as the neural model, using the same training-test split as a GCT-updated dataset described in Chapter 2.

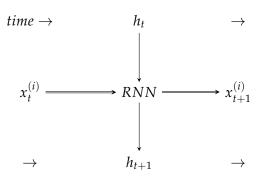
Table 3: Baseline and neural model test accuracy, Oracle experiment

Classifier	Root	Base	Inversion	Alto	Tenor
Multi-Class Logistic	59.75%	56.49%	64.43%	43.36%	38.93%
Multinomial Naive Bayes	52.62%	50.08%	63.05%	38.58%	35.93%
Random Forests	68.85%	61.37%	68.45%	51.96%	49.01%
Neural Network	60.86%	57.83%	69.67%	56.27%	40.05%

TODO: re-run neural network values for Oracle experiment

98 3.2 RNN Implementation

Based on the promising results of the Oracle experiment, I constructed a recurrent neural 99 network in Torch to determine if RNNs would improve accuracy over a sequence of inputs. 100 As discussed in Chapter 1, RNNs include recurrent connections that allow for feedback 101 from the computation that occured at the previous time step. During the forward pass, at 102 each time step in the data sequence, the RNN input layer receives an external input from 103 the ith sequence $x_t^{(i)}$ as well as internal feedback from the hidden layer h_t , and then outputs 104 a distribution x_{t+1} for the next time step. Here, each element of the sequence is a feature 105 vector describing a single melody note, drawn from the same dataset used for previous 106 models. 107



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Each chorale represents an independent sequence that is fed into RNN and outputs a synced sequence of distributions that correspond to the probability of each possibility harmonization at each time step. The most likely harmonization for each time step is chosen by taking the arg max of that time step's output distribution, $x_{t+1}^{(i)}$.

$$\arg\max_{k} x_{t+1}^{(i)} = \arg\max_{k} \begin{vmatrix} x_{t+1_{1}}^{(i)} \\ x_{t+1_{2}}^{(i)} \\ \vdots \\ x_{t+1_{k}}^{(i)} \end{vmatrix}$$

Internally, h_t is a stored as a "memory" of the melody features at time t+1, which will be used to predict the harmonization x_{t+2} .

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As a preprocessing step, each chorale was "padded" to the length of the longest chorale 116 (in this dataset, this was 208 segments). The padding was added to all chorale sequences 117 (both input and output vectors) using a unique "padding" feature in order not to confusing 118 the padding with the actual musical section of the sequence. The output sequence was 119 the same as the full harmonization task described in section 2.1 of Chapter 3, where each 120 feature denotes a full set of harmonic decisions, including the notes for the harmonizing 121 notes as well as a complete harmonic labelling using the GCT notation. Table 4 contains 122 the results. 123

Table 4: Neural and baseline model accuracy, full harmonization task

Model	Train NLL	Train	Test
Multinomial Logistic	_	42.74%	25.15%
Random Forests	_	89.83%	33.41%
LSTM	0.807	38.01%	29.35%

Given that the MFFC frequency is 5%, these results show a significant increase in accuracy over previous results. The random forest model continues to outperform neural models based on accuracy, potentially for reasons related to imbalanced data, as discussed in Chapter 2.

8 4 Chapter 4 - Looking forward

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4.1 Further Exploration: The Bach Inventions

The reality is a model trained to harmonize chorales has limited utility in modern times 130 (although it might have made Bach's work as Kapellmeister a bit easier). Musicians only 131 look to Bach's chorales as early model compositions for 4 voices and for theory-related 132 exercises. Chorales also have both a limited harmonic complexity as well as rhythmic 133 complexity, since they remain harmonically close to the tonic key and are easily segmented 134 into beat-long sections. This simplicity makes the chorales advantageous for statistical learning and allowed my models to output a uniform set of harmonizations over all inputs. 136 But as chorale harmonization is increasingly well-understood as a computational task, it is 137 worth recognizing the ways in which these models can be extended to more general and 138 common musical processes. As one potential application of these models, I will explore 139 the task of composing a counterpoint line given an input melody, and how this might be 140 approached from a computational standpoint. This task is intentionally general and could be applied to a wide variety of well-known musical corpuses. But here, I will focus on Bach's 142 15 Inventions because they are a body of exemplary two-voice counterpoint compositions 143 by the same composer as the Chorales. Despite being written explicitly as musical exercises, 144 they are also more melodically and rhythmically intriguing than the Chorales. 145

46 4.1.1 Added complexity

Generating harmonizations for inventions introduces several new layers of musical complexity that were not considered when harmonizing the chorales. One is rhythmic complexity, since Invention melodies cannot be easily abstracted into units of a single rhythmic
length. One method for describing rhythm in the generated melody is by generating predictions at the level of the smallest rhythmic unit (say a choice of pitch or rest for every 16th
beat), and then determining the duration of the pitch based on the number of iterations that
the same pitch is consecutively output by the model. Eck and Schmidhuber (2002) found

this approach effective for composing blues melodies. An similar but alternative model was 154 proposed by Franklin (2006), where separate LSTMs are trained to decide pitch and dura-155 tion. An additional layer complexity is the large-scale structure of the Invention. Inventions 156 typically consist of a series of thematic statements interleaved with episodes - modulatory 157 sections that are melodically derived from the subject and create transitions between the-158 matic statements in different keys. The remaining sections might be termed "elaborations", 159 which include cadences at the ends of episodes and codettas that occasionally come at the 160 end of an Invention. Each type of section has a specific set of conventions that govern its 161 structure as well as the relationship between the two voices. A final layer of complexity 162 to note is the need for subject identification. In contrast to the Chorales, a single melodic 163 idea (the "invention", or subject) governs the development of the entire work, and it is 164 consistently restated in various transformations. Identification of the subject is essential 165 for determining the melodic, harmonic, and rhythmic material used in the Invention, and 166 features from the subject should be extracted to create contrapuntal melodies. 167

4.1.2 Subject identification

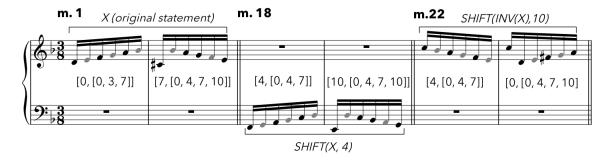
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Bach's Inventions are two-voice compositions, where the lower voice can be characterized as a function of the upper voice. In order for the model to learn the harmonic and rhythmic 170 material that Bach employs in the work, the model should first identify and extract features 171 from the Invention's primary subject. Identifying the subject generally straightforward for 172 the listener, since the primary subject is typically the first statement in the upper voice. 173 However, inventions can contain multiple subjects with varying levels of importance. And 174 in Invention No. 6 in E major, Bach introduces two subjects of equal importance and devel-175 ops them both consistently throughout. Therefore, a better approach might be to identify 176 subjects by selecting melodic ideas based on the frequency with which they are restated. 177 Dreyfus (1996) notes that the frequency of a subject is directly correlated with its impor-178 tance in the Invention - a principle of repetition that is generally true of melodies in Western music. One candidate algorithm for subject identification based on repetition is hierarchal

agglomerative clustering (HAC), which can learn to "cluster" melodic segments based on 181 a supplied distance metric. Nagler (2014) applied HAC to the task of motivic analysis in 182 Schubert's song cycle Die Winterreise and found promising results in extracting the main 183 motive from each song. However, a significant difficulty in subject identification would be 184 the harmonic and rhythmic transformations that are often applied to the subject when it is 185 restated. For this task, it could be useful to encode the melody as a series of intervals rather 186 than pitches in order to identify subjects in their original form as well as their transformed 187 state. 188

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Figure 2: The subject and transformations in Invention No. 4 in D Minor, BWV 775.



4.1.3 Form identification

Once rhythmic and melodic features are extracted from the most prominent subjects, the model can use these to analyze the large-scale structure of the Invention and divide the work into a series of sections. One classifier could be trained to create the general boundaries of each section, while a separate classifier could label each section as a thematic statement (T), episodes (S), and elaborations (E) by analyzing if and how the subject is presented in the upper voice. Complete, sequential statements of the subject suggest a thematic statement, while partial and transformed subject statements will suggest an episode. Elaborations will most likely differentiate themselves by the unique and less repetitive melodic material.

4.1.4 Harmonic identification

Before generating the melody, a useful preprocessing step would be to perform harmonic 200 analysis over the upper voice. The classifier would be trained to accept the upper voice as 201 input and output a sequence of corresponding harmonic encodings. This task is well-suited 202 to the model presented in Chapter 2 and 3, where information about a segment of the melody 203 would be classified as a GCT-encoded harmony. While many pleasant melodies can be gen-204 erated for the counterpoint melody, the most crucial constraint is harmonic agreement. A 205 crucial purpose of the contrapuntal lower voice is to support the upper voice in harmony. 206 The upper voice typically guides the progression, while the lower voice may echo and rein-207 force harmonic transitions, as Figure 3a illustrates. 208

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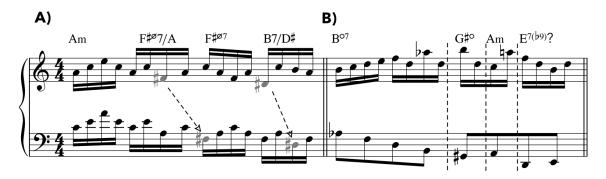
The primary technique for implying harmonies is the use of scalar and triadic passages. Not coincidentally, many of Bach's subjects are constructed to facilitate various transformations (SHIFT, INV, AUGMENT, etc.) and be harmonically indicative. However, given a scalar or triadic passage, it can be difficult to determine which of many potential chords is most strongly implied. There are several important indicators, including the harmony in the previous melodic unit and the beat strength of the notes in the current unit. A recurrent model would likely perform well on this task because of the sequential format of the data (representing the upper voice as a *sequence* of melodic units) and the feedback loop that would provide information about preceding harmonies. The size of each melodic unit, however, is an additional parameter that would require adjustment since the implied harmonies have varying durations (Figure 3b).

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4.1.5 Contrapuntal melodic generation

Using the structural information gathered during preprocessing, a final classifier is trained to generate contrapuntal melodies. The classifier would accept input features describing the current relevant subject, the current section of the form, and the current implied harmony,

Figure 3: Excerpts from Invention No. 13 in A Minor, BWV 784.



as well as melodic features related to the upper voice near time t. The output feature would describe the most likely pitch for time t, with an implied duration of the length of the time 227 step. Consecutive time steps of the same pitch could be merged to represented longer notes. 228 The generalization of this model allows for a wide range of corpuses to be incorporated 229 into the training data. Stylistically similar candidates include Bach's Sinfonias (the 3-230 voice equivalent of the Inventions) and the Fugues. Stylistically separate candidates include 231 Palestrina's masses and motets, which feature significant contrapuntal composition and de-232 velopment of melodic motives in multiple voices. The larger dataset available for training 233 will very likely improve model performance, in comparison to the computationally small 234 dataset of chorales used in this paper. Further work should be done to explore this extension 235 of the harmonization task to various musical corpuses.

7 4.2 Conclusion

In this paper, the objective was to apply a variety of neural and non-neural models to dif-238 ferent musical processes involved in the task of chorale harmonization. These models are 239 meant to supplement existing work on computational approaches to generative and com-240 pletive musical tasks, not to replace human musical analysis or composition. The Random 241 forest model and recurrent neural models proved most effective in learning the various sub-242 tasks associated with harmonization, and in the future they should be evaluated on similar 243 musical tasks, such as the generation of contrapuntal voices. The accuracy results from 244 experiments with these computational models demonstrate a promising ability to learn mu-245 sical structure and connect temporally distant events. 246

4.3 Code and related files

- 248 All code and data related to this paper is freely available on GitHub at
- 249 https://github.com/glasperfan/thesis/.

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