

# **ELEC 221 Lecture 20**

## **Modulation and communication systems**

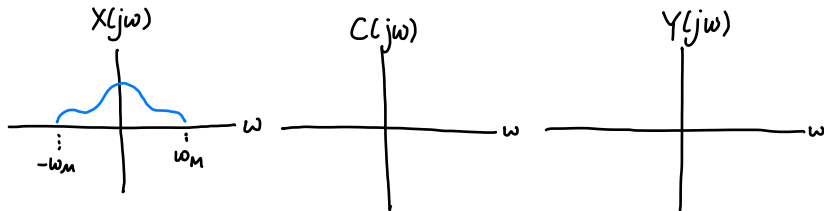
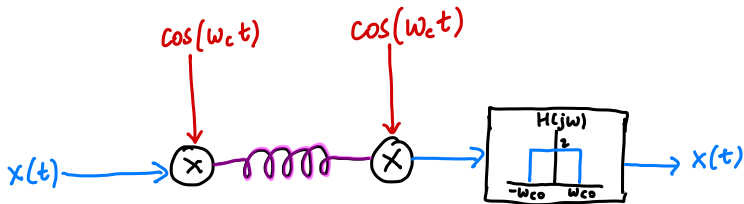
Thursday 21 November 2024

# Announcements

- Assignment 4 due Saturday 23:59
- Tutorial assignment 4 due Monday 23:59
- Monday tutorial assignment 5: prepare five 1-2s audio samples
- No office hours tomorrow; Tuesday class on Zoom
- Quiz 9 on Tuesday

## Last time

We did sinusoidal amplitude modulation with a real carrier signal:



We distinguished between synchronous and asynchronous modulation.

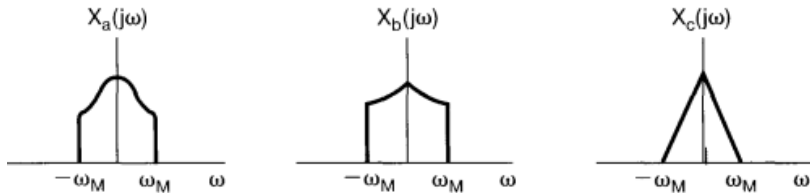
Partially an “infotainment” lecture.

Learning outcomes:

- describe frequency- and time-division multiplexing
- perform single-sideband modulation
- explain (at a high level!) how cell phone communication works

# Frequency-division multiplexing (FDM)

Suppose we have more than one signal we wish to transmit:



Modulation can help us send them at the same time!

Image credit: Oppenheim 8.3

# Frequency-division multiplexing (FDM)

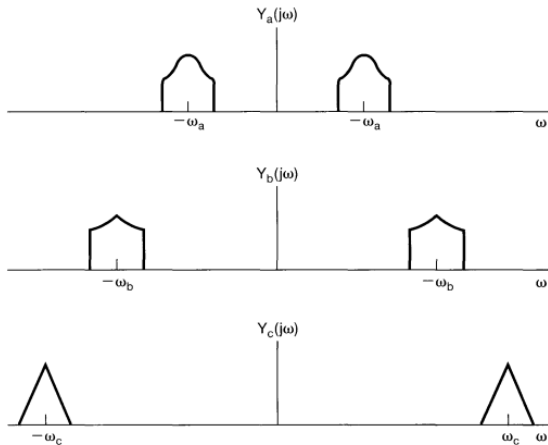
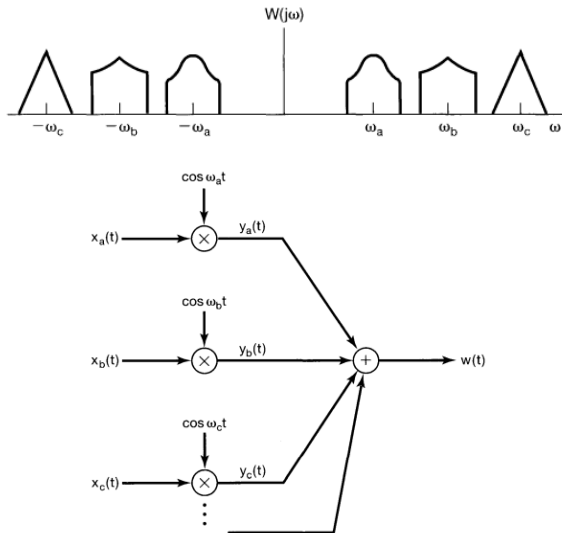


Image credit: Oppenheim 8.3

# Frequency-division multiplexing (FDM)

This is called *frequency-division multiplexing*.



# Frequency-division multiplexing (FDM)

How to separate out the channels?

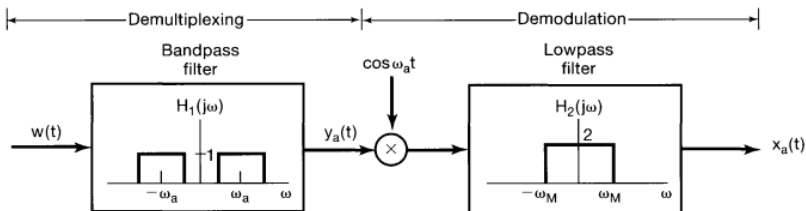
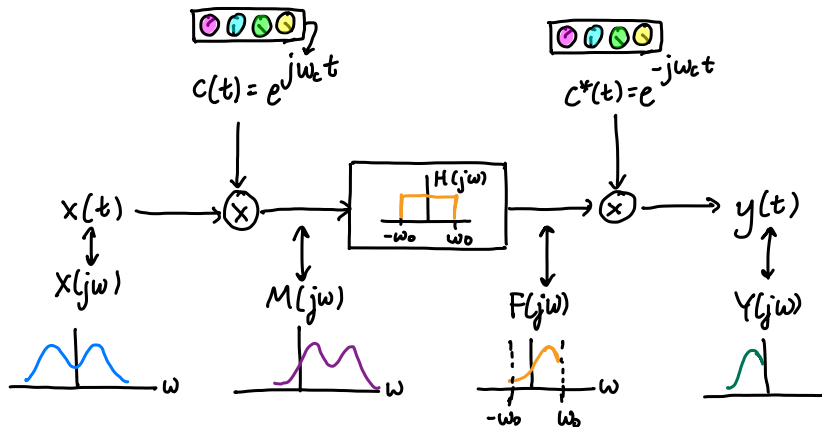


Image credit: Oppenheim 8.3



## Example: frequency-selective filtering with variable centre frequency



# Real-world example: radio



“Superheterodyne receiver” (Tutorial assignment 5!)

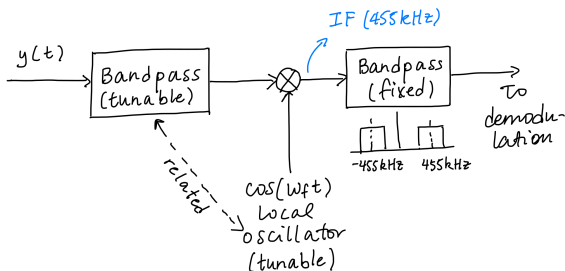
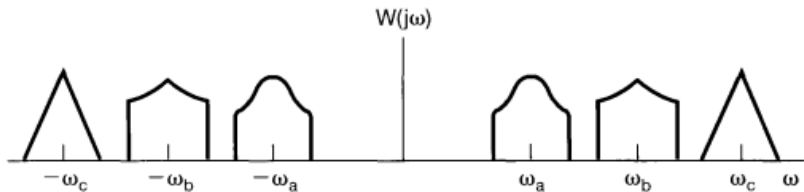


Image: <https://www.euronics.ee/UserFiles/Products/Images/162391-panasonic-rf-2400d-radio.png>

# Single-sideband modulation (SSB)

This is inefficient...

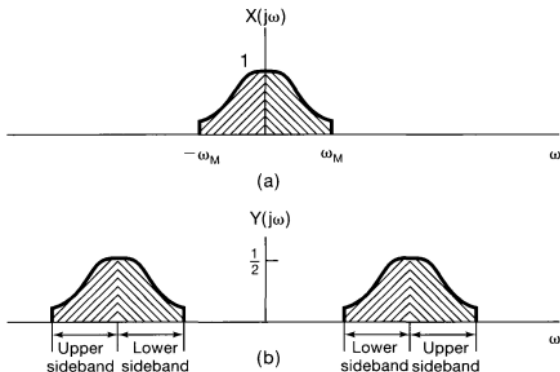


We are using twice as much bandwidth as we need to!

Image credit: Oppenheim 8.3

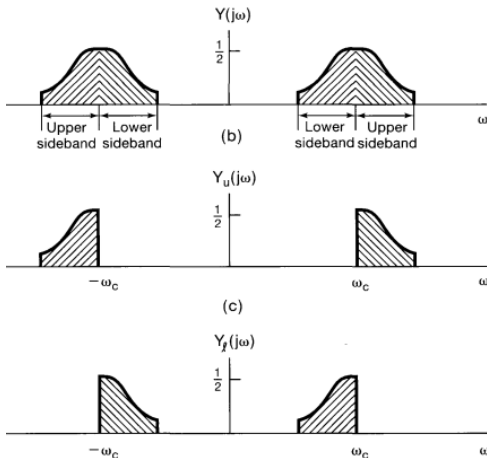
# Single-sideband modulation (SSB)

A modulated signal's spectrum can be divided into upper/lower *sidebands*:



# Single-sideband modulation (SSB)

In single-sideband modulation, keep and transmit only one band:

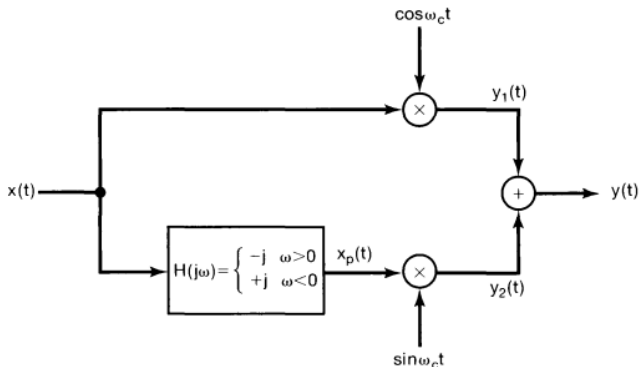


How do you think this is done? How to demodulate?

# Single-sideband modulation (SSB)

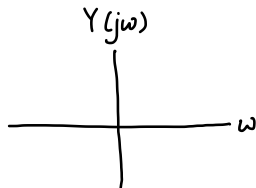
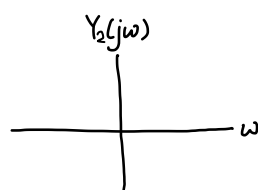
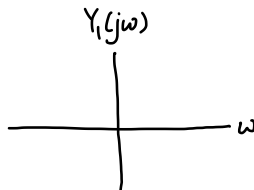
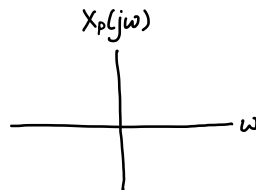
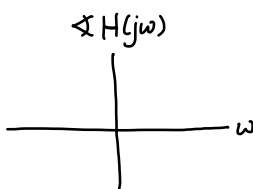
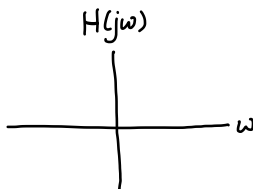
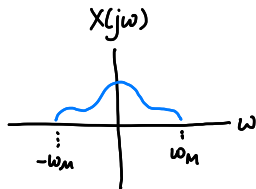
# Single-sideband modulation (SSB)

Alternative: “90° phase-shift network”



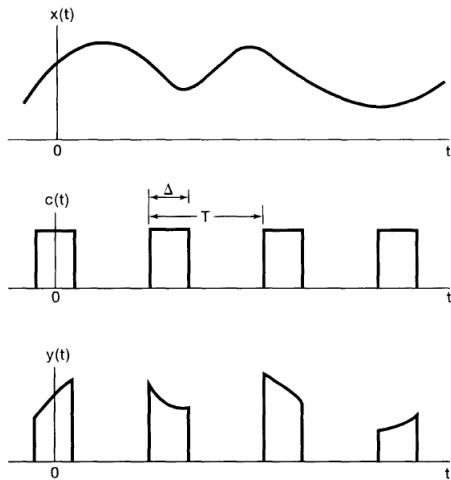
Exercise: see how this works by analyzing what happens to the spectra of  $x_p(t)$ ,  $y_1(t)$ ,  $y_2(t)$ , and  $y(t)$  in the frequency domain.

## Single-sideband modulation (SSB)



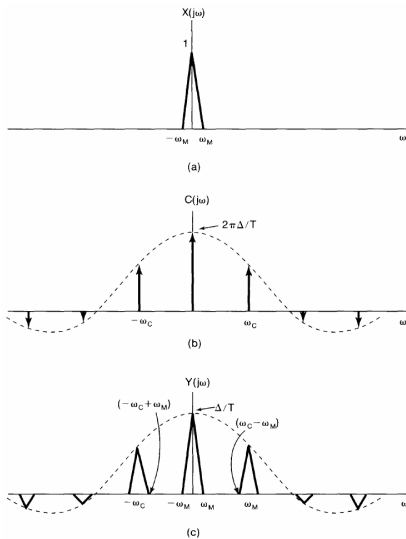


## AM with pulse-train carrier



**Figure 8.23** Amplitude modulation of a pulse train.

# AM with pulse-train carrier



# Time-division multiplexing

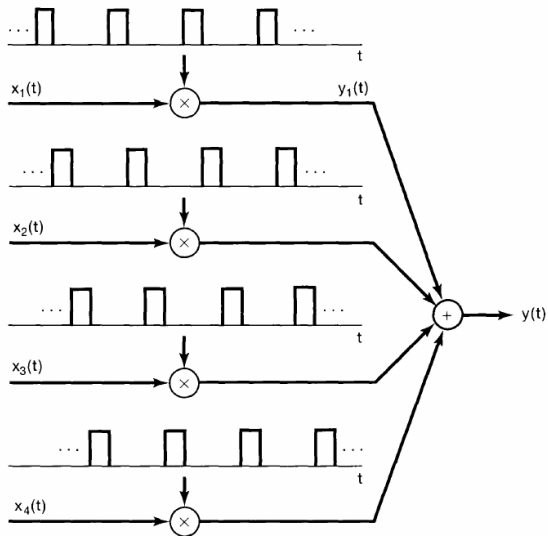
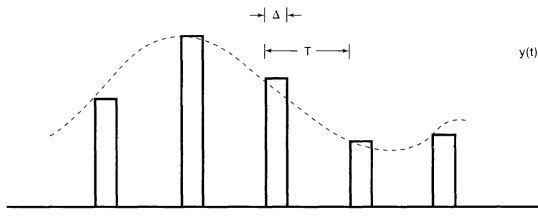
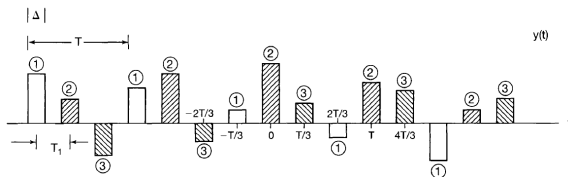


Image credit: Oppenheim 8.5

# Pulse-amplitude modulation (PAM)



**Figure 8.26** Transmitted waveform for a single PAM channel. The dotted curve represents the signal  $x(t)$ .



Discretized version (pulse code modulation) widely used for digital data transmission.

## Example: TDM

- 8.12.** Consider a set of 10 signals  $x_i(t)$ ,  $i = 1, 2, 3, \dots, 10$ . Assume that each  $x_i(t)$  has Fourier transform such that  $X_i(j\omega) = 0$  for  $|\omega| \geq 2,000\pi$ . All 10 signals are to be time-division multiplexed after each is multiplied by a carrier  $c(t)$  shown in Figure P8.12. If the period  $T$  of  $c(t)$  is chosen to have the maximum allowable value, what is the largest value of  $\Delta$  such that all 10 signals can be time-division multiplexed?

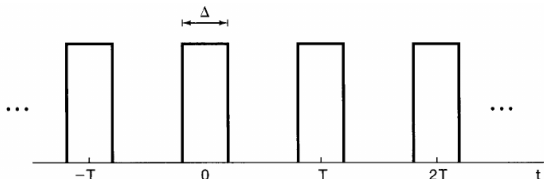


Figure P8.12

# Frequency modulation

Model frequency modulation as

where  $\theta(t)$  depends on a modulating signal  $x(t)$ .

*Phase modulation:*

*Frequency modulation.*

# Frequency modulation

Phase modulation with  $x(t)$  is equivalent to frequency modulation with  $dx(t)/dt$ :

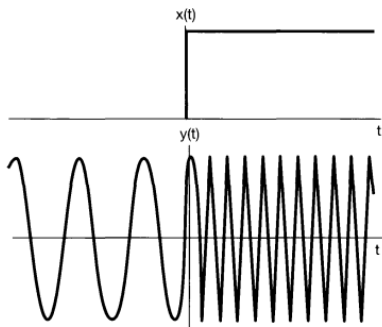
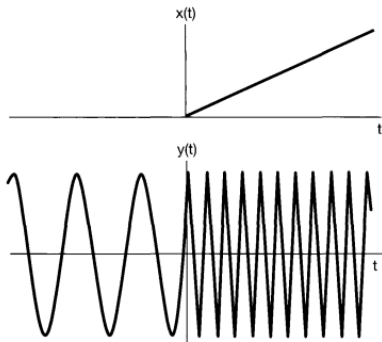


Image credit: Oppenheim 8.7

# Frequency modulation with a square wave

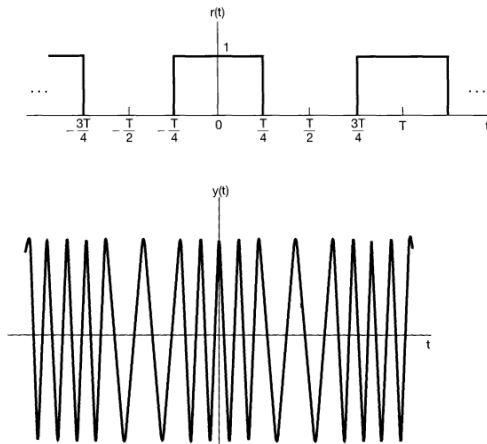
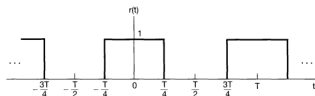


Image credit: Oppenheim 8.7



# Frequency modulation with a square wave



Suppose the square wave changes the frequency between  $\omega_c + \Delta\omega$  and  $\omega_c - \Delta\omega$ .

We can write

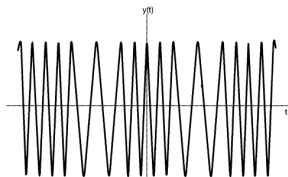


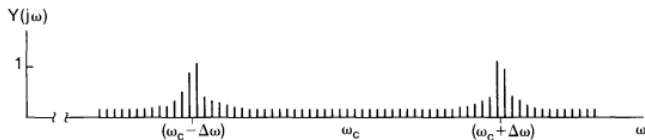
Image credit: Oppenheim 8.7

What are we doing to these signals?

# Frequency modulation with a square wave

This is two AM signals!

Their combined spectrum is the sum of the individual spectra:

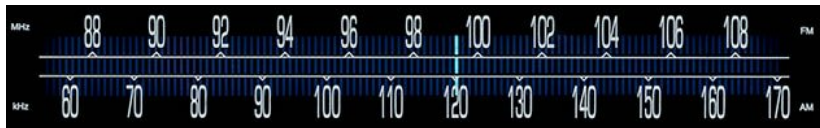


# Frequency modulation

Main takeaways:

- FM is more complicated to analyze than AM
- FM radio uses more bandwidth than AM radio

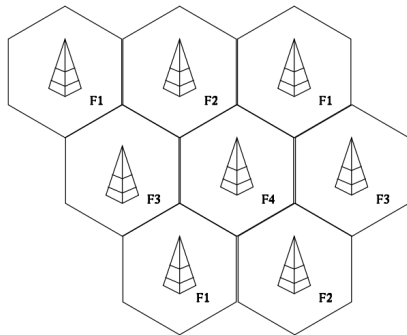
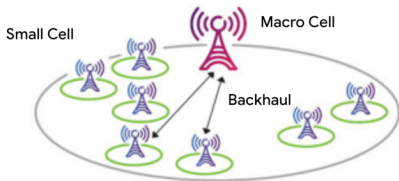
FM radio is allocated the frequencies between 88-108 MHz.



Channels are allocated 200kHz each; the station frequency is the centre of this band (all FM stations end in odd decimals!).

# Infotainment: cell phone communication systems

A cell phone is basically just a really fancy radio.





# Infotainment: cell phone communication systems

## 3500 MHz band spectrum auction

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From: [Innovation, Science and Economic Development Canada](#)

### Backgrounder

#### 3500 MHz band

The Government of Canada is committed to ensuring that Canadians have access to high-quality wireless services and benefit from ubiquitous coverage and affordable prices. In a globalized world, the **deployment of 5th generation—or “5G”—telecommunications standards and technologies** is essential to Canada’s economic competitiveness. The deployment of 5G will also help ensure that Canadians continue to benefit from world-class wireless infrastructure.

In June 2018, Innovation, Science and Economic Development Canada (ISED) released [Spectrum Outlook 2018 to 2022](#), which included plans to release spectrum that would support 5G services. The Outlook indicated that releasing the 3450–3650 MHz band (referred to as the 3500 MHz band), a key band for 5G, was a high priority. In June 2019, ISED published the [Decision on Revisions to the 3500 MHz Band to Accommodate Flexible Use and Preliminary Decisions on Changes to the 3800 MHz Band](#) as the first step toward making this band available.

Through the release of the [Policy and Licensing Framework for Spectrum in the 3500 MHz Band](#), ISED is setting the rules for the upcoming spectrum auction, the next step toward making this band available for 5G services.

#### Spectrum to be auctioned

**ISED is making 200 MHz of spectrum available in the 3500 MHz band for “flexible use” licensing** that allows licensees to choose the type of services they will deploy, such as mobile (5G) or fixed wireless services (e.g. Internet-to-the-home). Through the transition process, existing licensees are eligible

Image credit: <https://www.canada.ca/en/innovation-science-economic-development/news/2020/03/>

Different “generations” of service use different bands.

Higher frequencies enable transmission of more information (more available bandwidth), at the cost of working better for shorter distances.

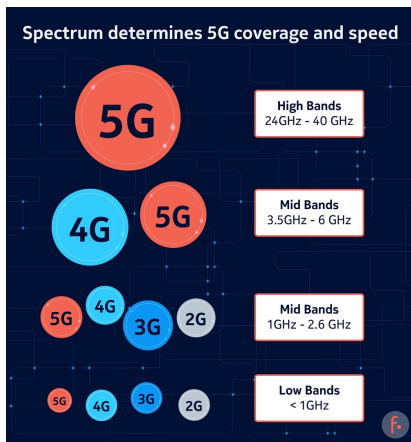


Image credit: <https://www.nokia.com/networks/insights/spectrum-bands-5g-world/>

Learn more:

[https://en.wikipedia.org/wiki/Cellular\\_network](https://en.wikipedia.org/wiki/Cellular_network)

[https://www.myamplifiers.com/articles/  
lte-frequency-bands-of-us-and-canada-carriers/](https://www.myamplifiers.com/articles/lte-frequency-bands-of-us-and-canada-carriers/)

[https://en.wikipedia.org/wiki/LTE\\_frequency\\_bands](https://en.wikipedia.org/wiki/LTE_frequency_bands)

<https://www.nokia.com/networks/insights/spectrum-bands-5g-world/>



# For next time

## Content:

- the Laplace transform

## Action items:

1. Assignment 4 due Saturday 23:59
2. Tutorial assignment 4 due Monday 23:59
3. Tutorial assignment 5 on Monday
4. Quiz 9 on Tuesday (class on Zoom)

## Recommended reading:

- From this class: Oppenheim 8.5-8.6
- Suggested problems: 8.7-8.10, 8.28-8.30, 8.40
- For next class: Oppenheim 9.0-9.4