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1  function g = pool_adjacent_violators(h,inc)
2  % Compute the isotonic regression of an histogram h.
3  % inc = boolean value saying if we want the non-decreasing (inc = 1) or
4  % decreasing regression
5
6  % Copyright (c) 2016 Julie Delon
7
8
9  if (inc ==0)
10     g = h;
11     for i =1:length(h)
12         som = g(i);
13         for j = i-1:-1:1
14             if(j==1 || (g(j)*(i-j) >=som))
15                 som=som/(i-j);
16                 for k=j+1:i
17                     g(k)=som;
18
19                 end
20                 break;
21
22             end
23             som =som+ g(j);
24         end
25     end
26 end
27
28 if (inc ==1)
29     g = h;
30     for i =length(h)-1:-1:1
31         som = g(i);
32         for j = i+1:length(h)
33             if(j==length(h) || (g(j)*(j-i) >=som))
34                 som=som/(j-i);
35                 for k=i:j-1
36                     g(k)=som;
37
38                 end
39                 break;
40
41             end
42             som=som+ g(j);
43         end
44     end
45 end
46 end
47
48
49 function max_entrop = max_entropy(h,a,b,e,inc)
50
51 % Compute the maximum entropy of the histogram h(a:b) for the increasing or decreasing hypothesis
52 % inc = boolean value indicating if we test the increasing or
53 % decreasing hypothesis
54 % h = histogram
55 % e = parameter used to compute the entropy
56
57 % See
58
59 % Copyright (c) 2016 Julie Delon
60
61
62 g=h(a:b);
63 decreas=pool_adjacent_violators(g,inc);
64 L=length(g);
65
66 % integrate signals
67 g = cumsum(g);
68 decreas = cumsum(decreas);
69
70 % meaningfulness threshold
71 N = g(L);
72 seuil=(log(L*(L+1)/(2))+e*log(10))/N;
73
74 % search the most meaningful segment (gap or mode)
75 max_entrop=0.;
76 for i=1:L
77     for j = i:L
78         if (i==1)
79             r=g(j);
80         else
81             r = g(j) - g(i-1);
82         end
83         r=r/N;
84         if (i==1)
85             p = decreas(j);

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86         else
87             p = decreas(j) - decreas(i-1);
88         end
89         p=p/N;
90
91         v=entrop(r,p);
92
93         if(v>max_entrop)
94             max_entrop=v;
95         end
96
97     end
98 end
99
100 max_entrop=(max_entrop-seuil)*N;
101
102
103 function v = entrop(x,y)
104 % function computing the entropy between x and y. x and y must be in the interval [0,1]
105
106 if (x==0.) v=-log10(1-y);
107 elseif (x==1.0) v = -log10(y);
108 else v= (x*log10(x/y)+(1.0-x)*log10((1.0-x)/(1.0-y)));
109 end
110
111
112
113 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
114 % The following functions implement the Fine to Coarse Histogram Segmentation described in
115 % // J. Delon, A. Desolneux, J-L. Lisani and A-B. Petro, A non
116 % parametric approach for histogram segmentation, IEEE Transactions
117 % on Image Processing, vol.16, no 1, pp.253-261, Jan. 2007. //
118 %
119 % Usage :
120 % u = double(imread('..images/lena.png'));
121 % H = hist(u(:),0:255);
122 % idx=FTC_Seg(H,0);
123 % idx should contain the list of all minima separating the modes of
124 % H
125
126 % Copyright (c) 2016 Julie Delon
127 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
128
129 function idx = FTC_Seg(H,e)
130
131 % FTC_seg
132
133 % H = the integer-valued histogram to be segmented.
134
135 % e = parameter of the segmentation
136 % (corresponds to e = -log10(epsilon) in the paper)
137 % large e => coarse segmentation
138 % small e => fine segmentation
139
140
141
142
143
144 lH = length(H);
145
146 %% find the list of local minima and maxima of H
147 [p,idx_max] = findpeaks(H);
148 [p,idx_min] = findpeaks(-H);
149 idx = sort([idx_min,idx_max]);
150 if (idx(1)~=1) idx = [1,idx]; end
151 if (idx(end)~=lH) idx = [idx,lH]; end
152
153
154 % find if idx starts with a minimum or a maximum
155 if H(idx(1)) < H(idx(2))
156     begins_with_min = 1;
157 else
158     begins_with_min = 0;
159 end
160
161 %% FILL THE LIST OF ENTROPIES FOR ALL MODES
162 % The merging of two contiguous modes [a,b] and [b,c] can be done in two ways,
163 % either by using the maximum M1 on [a,b] and by testing the decreasing hypothesis on [M1,c],
164 % or by using the maximum M2 on [b,c] and by testing the increasing hypothesis on [a,M2].
165 % For each configuration, we compute the entropy of the worst interval against the considered hypothesis.
166
167 K = length(idx);
168 val=zeros(1,K-3);
169
170 % Loop on all optimas

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171 for k = 1:K-3
172
173     % decide if we want to test the increasing or decreasing hypothesis on
174     % [idx(k),idx(k+3)]
175
176     if ((begins_with_min && mod(k,2)==1)|(~begins_with_min && mod(k,2)==0))
177         inc = 1;
178     else inc = 0;
179     end
180
181     % compute the max entropy on the interval [k,k+3]
182     val(k) = max_entropy(H,idx(k),idx(k+3),e,inc);
183
184 end
185
186
187
188
189 %%%%%%%%%% MERGING of MODES
190
191 [valmin, kmin] = min(val); %[idx(kmin), idx(kmin+3)] is the first interval to merge
192
193 while(~isempty(val) && valmin<0)
194
195     % update the list of min, max
196     idx = [idx(1:kmin),idx(kmin+3:end)];
197     val = [val(1:min(kmin,end)),val(kmin+3:end)];
198     val = val(1:length(idx)-3);
199
200     % update max_entropy around the removed optima
201     for j=max(kmin-2,1):min(kmin,length(val))
202
203         % decide if increasing or decreasing
204         if (begins_with_min && mod(j,2)==1)|(~begins_with_min && mod(j,2)==0)
205             inc = 1;
206         else inc = 0;
207         end
208
209         % update the max entropy on the interval [k,k+3]
210         val(j) = max_entropy(H,idx(j),idx(j+3),e,inc);
211     end
212
213     [valmin, kmin] = min(val);
214
215
216 end
217
218 if (begins_with_min)
219     idx = idx(1:2:end);
220 else
221     idx = idx(2:2:end);
222 end
223
224
225 %% Display the segmentation
226 bar(H,'r');
227 hold on;
228 for k = 1:length(idx)
229     line([idx(k) idx(k)], [0 max(H(:))]);
230 end
231 hold off;
232
233
234 end
235
236
237
238
239
240

```