

1.

```
python3 mai... Ask Assistant 57s • Just now
> Environment updated. Reloading shell...
Converged in 95 iterations

Numerical solution matrix u(x,y):
      0.000      0.314      0.628      0.942      1.257      1.571
x\y
0.000  1.000000  0.951057  0.809017  0.587785  0.309017  0.0
0.314  0.951057  0.753225  0.564621  0.368084  0.172806  0.0
0.628  0.809017  0.555908  0.347640  0.176348  0.053086  0.0
0.942  0.587785  0.333231  0.132647 -0.004976 -0.058882  0.0
1.257  0.309017  0.085806 -0.086863 -0.182347 -0.166748  0.0
1.571  0.000000 -0.173197 -0.305633 -0.353912 -0.269910  0.0
1.885 -0.309017 -0.424258 -0.511151 -0.511645 -0.364162  0.0
2.199 -0.587785 -0.645220 -0.686178 -0.642021 -0.441312  0.0
2.513 -0.809017 -0.814475 -0.809947 -0.724389 -0.486321  0.0
2.827 -0.951057 -0.915787 -0.858894 -0.725487 -0.467874  0.0
3.142 -1.000000 -0.951057 -0.809017 -0.587785 -0.309017  0.0
```

2.

```
python3 mai... Ask Assistant 1s • Just now
> Environment updated. Reloading shell...
      0.5      0.6      0.7      0.8      0.9      1.0      1.1
t \ r
0.0  0.000000e+00  2.000000e+01  4.000000e+01  6.000000e+01  8.000000e+01  1.000000e+02  120.0
0.5  3.359000e+02  4.366700e+02  3.971400e+02  3.725000e+02  3.577800e+02  3.500000e+02  120.0
1.0 -1.266307e+04 -1.646199e+04  1.684350e+03  1.305040e+03  1.069580e+03 -2.891389e+04  140.0
1.5  2.212421e+06  2.876147e+06 -2.155387e+06  1.448336e+04 -3.927286e+06  7.344946e+06  160.0
2.0 -5.804072e+08 -7.545294e+08  8.724695e+08 -7.777834e+08  1.948729e+09 -2.295236e+09  180.0
2.5  1.842459e+11  2.395197e+11 -4.089916e+11  5.547262e+11 -8.798988e+11  8.029253e+11  200.0
3.0 -7.224091e+13 -9.391318e+13  2.039340e+14 -3.029171e+14  3.905248e+14 -3.044164e+14  220.0
3.5  3.286372e+16  4.272284e+16 -1.022495e+17  1.511914e+17 -1.731678e+17  1.221745e+17  240.0
4.0 -1.593741e+19 -2.071863e+19  5.066787e+19 -7.262787e+19  7.708801e+19 -5.098513e+19  260.0
4.5  7.841578e+21  1.019405e+22 -2.474809e+22  3.426023e+22 -3.449624e+22  2.184950e+22  280.0
5.0 -3.839314e+24 -4.991108e+24  1.193394e+25 -1.601250e+25  1.551710e+25 -9.536954e+24  300.0
5.5  1.860706e+27  2.418918e+27 -5.695406e+27  7.446484e+27 -7.012469e+27  4.217357e+27  320.0
6.0 -8.925828e+29 -1.160358e+30  2.696220e+30 -3.452948e+30  3.181660e+30 -1.882852e+30  340.0
6.5  4.244362e+32  5.517671e+32 -1.268492e+33  1.598312e+33 -1.448305e+33  8.466524e+32  360.0
7.0 -2.004089e+35 -2.605316e+35  5.939584e+35 -7.389840e+35  6.610286e+35 -3.828027e+35  380.0
7.5  9.418825e+37  1.223407e+38 -2.771070e+38  3.414044e+38 -3.023460e+38  1.738150e+38  400.0
8.0 -4.400347e+40 -5.720451e+40  1.289237e+41 -1.576385e+41  1.385228e+41 -7.918353e+40  420.0
8.5  2.050791e+43  2.666028e+43 -5.985411e+43  7.275779e+43 -6.355009e+43  3.616628e+43  440.0
9.0 -9.533684e+45 -1.239379e+46  2.774252e+46 -3.357109e+46  2.918537e+46 -1.655198e+46  460.0
9.5  4.423424e+48  5.750451e+48 -1.284258e+49  1.548646e+49 -1.341435e+49  7.587205e+48  480.0
10.0 -2.049316e+51 -2.664111e+51  5.939345e+51 -7.142712e+51  6.169526e+51 -3.482169e+51  500.0
```

3.

```
python3 mai...
> Environment updated. Reloading shell...
Converged after 128 iterations.

Numerical result (Temperature field T(r, 0)):
Partial output (first 10 r rows x first 10 0 columns):
      0.00      50.00      50.00      50.00      50.00      50.00      50.00      50.00      50.00      50.00
0.00  14.82  28.85  41.88  53.62  63.84  72.46  79.49  85.05  89.32
0.00  14.80  29.08  42.38  54.32  64.69  73.38  80.44  85.98  90.19
0.00  15.03  29.51  42.96  55.01  65.42  74.11  81.11  86.57  90.69
0.00  15.26  29.95  43.57  55.72  66.16  74.83  81.77  87.14  91.16
0.00  15.50  30.41  44.18  56.43  66.91  75.56  82.43  87.71  91.63
0.00  15.75  30.87  44.81  57.16  67.67  76.29  83.09  88.27  92.08
0.00  16.01  31.35  45.46  57.90  68.44  77.03  83.75  88.83  92.53
0.00  16.27  31.85  46.12  58.66  69.22  77.77  84.41  89.38  92.97
0.00  16.54  32.36  46.80  59.44  70.02  78.51  85.06  89.92  93.40
```

4.

```
Numerical solution p(x, t):
x \ t |      0.00      0.10      0.20      0.30      0.40      0.50
-----
0.00 |  1.000  1.000  1.000  1.000  1.000  1.000
0.10 |  0.809  1.024  1.039  1.039  1.024  1.000
0.20 |  0.309  0.848  1.062  1.062  1.039  1.000
0.30 | -0.309  0.348  0.871  1.062  1.039  1.000
0.40 | -0.809 -0.285  0.348  0.848  1.024  1.000
0.50 | -1.000 -0.809 -0.309  0.309  0.809  1.000
0.60 | -0.809 -1.024 -0.848 -0.348  0.285  2.000
0.70 | -0.309 -0.848 -1.062 -0.871  0.843  2.000
0.80 |  0.309 -0.348 -0.871  0.129  0.843  2.000
0.90 |  0.809  0.285  0.843  0.843  1.285  2.000
1.00 |  2.000  2.000  2.000  2.000  2.000  2.000
```