

# Internal Migration and the Microfoundations of Gravity

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Does it matter how we understand these two facts?



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  - Tractable
  - Easily matches both facts
  - Natural extension of the trade literature



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- Third fact about internal migration:
  3. Return migration is extremely common
  - 3'.  $t$ -year migration rate is proportional to  $\sqrt{t}$ 
    - Suggestive of persistent preferences?

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4. Compare to a moving cost model
  - Different implications for macro misallocation, long-run population elasticities, speed of adjustment

# Contributions to the Literature

- Spatial dynamics
  - Rise and decline of regional economies  
Blanchard and Katz (1992); Caliendo, Dvorkin and Parro (2019); Allen and Donaldson (2020); Morris-Levenson and Prato (2022); Glaeser and Gyourko (2005); Liu, Klieman and Redding (2021); Amior and Manning (2018); Davis, Fisher and Veracierta (2021)
  - Macro adaptation to external shocks  
Tombe and Zhu (2019); Hao, Sun, Tombe and Zhu (2020); Eckert and Peters (2018); Giannone (2017); Heise and Porzio (2021); Bryan and Morten (2019); Cruz and Rossi-Hansberg (2021); Oliveira and Pereda (2020)
- How to model migration
  - Modifications of the dynamic logit  
Kennan and Walker (2011); Kaplan and Schulhofer-Wohl (2017); Giannone, Li, Paixao and Pang (2020); Porcher (2020); Mangum and Coate (2019); Monras (2018); Coen-Pirani (2010); Davis et al. (2021)
  - Persistent preferences  
Bayer and Juessen (2012)
  - Empirical evidence  
Saks and Wozniak (2011); Farrokhi and Jinkins (2021); Koşar, Ransom and Van der Klaauw (2021); Fujiwara, Morales and Porcher (2022)
- Multinomial probits
  - Butler and Moffitt (1982); Keane (1992); Geweke, Keane and Runkle (1994)

## 3 Facts about Internal Migration

# Data

- Gies Consumer and Small Business Credit Panel (GCCP)
  - Credit data from one of the leading providers of credit reports
  - 1 percent of Americans with credit reports
  - Includes state of residence
  - Panel data, 2004-2018
- IRS Migration Data
  - Based on tax filings
  - Aggregated flows of state-to-state migration

## Fact #1

### Migration is rare



### Comparison of interstate migration rates in IRS and GCCP

## Fact #2

## Migration follows a gravity pattern

Poisson regression:

$$\log m_{i \rightarrow j} = \beta \log \text{distance}_{ij} + \alpha \log p_i + \gamma \log p_j + \epsilon_{ij}$$

	(1)	(2)
	Migration (IRS)	Migration (Credit)
Log Distance	-0.736*** (0.0572)	-0.744*** (0.0515)
Log Origin Population	0.900*** (0.0832)	0.923*** (0.0797)
Log Destination Population	0.822*** (0.0976)	0.893*** (0.0799)
Observations	2550	2550

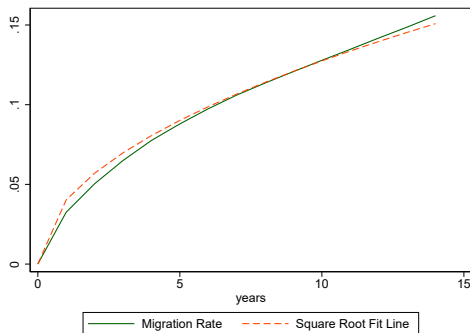
Standard Errors are two-way clustered by origin and destination states

\*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$



## Fact #3 (New)

$t$ -year interstate migration rate is proportional to  $\sqrt{t}$



- Implies a high rate of return or onward migration
- Suggestive of persistent preferences

## The SPACE Model



# Model

$I$  locations indexed by  $i$ , continuum of individuals indexed by  $n$ , and discrete time indexed by  $t$ :

- Agents choose location that maximizes utility

$$u_{nt} = \max_i u_{int} = \max_i v_{it} + \epsilon_{int}$$

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- Spatially and Persistently Auto-Correlated Epsilons (SPACE)

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- Square root fact

### Proposition 2

As  $\rho \rightarrow 1$ , the  $t$ -year migration rate is proportional to  $\sqrt{t}$

# Parameterization

- Two parameters: persistence  $\rho$ , and spatial correlation  $A$
- Target: migration rate, gravity equation
- Simulate 10 million people for two periods, fifty U.S. states and D.C.
  - $v_i$  matches population

## Matching the Facts Quantitatively

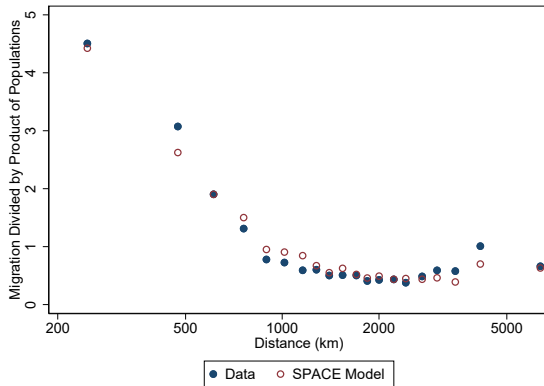
- Persistence:  $\rho = .9996$ ,
- Spatial correlation:  $A = .000299 \text{ km}^{-1}$
- Hits 3.34 percent migration rate

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	Migration (IRS)	Migration (Credit)	Simulated Migration
Log Distance	-0.736*** (0.0572)	-0.744*** (0.0515)	-0.744*** (0.0396)
Log Origin Population	0.900*** (0.0832)	0.923*** (0.0797)	0.892*** (0.0486)
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Observations	2550	2550	2550

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# Gravity

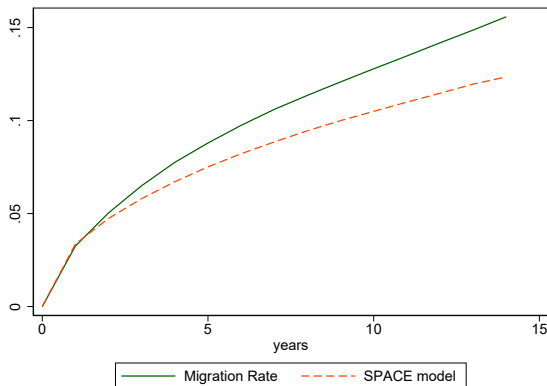


- Curvature is untargeted

# Square Root Fact

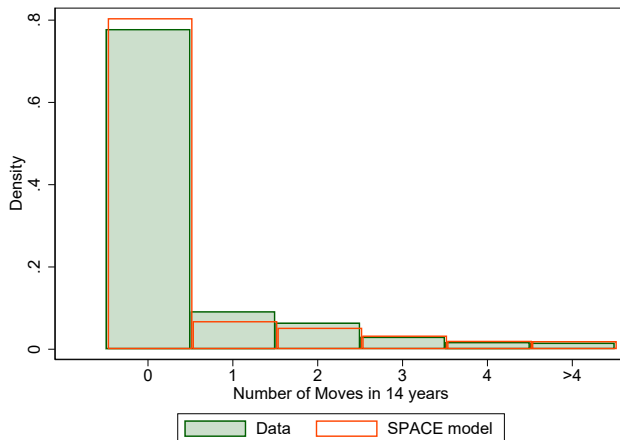
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As  $\rho \rightarrow 1$ , the  $t$ -year migration rate is proportional to  $\sqrt{t}$ .



5-year Calibration

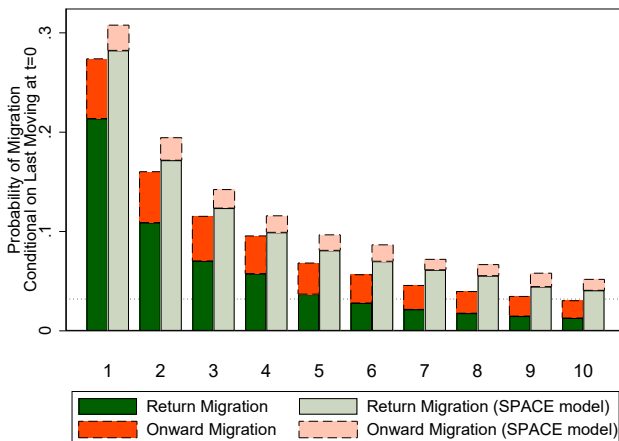
# Frequency of Migration



5-year Calibration

# Return Migration

- Conditional probability of moving after previous move



## Implications of the Model



## Is the model useful?

- Population elasticities critical for a variety of questions in the literature
- One reason for skepticism: multinomial probits do not have a closed-form solution for these elasticities as a function of parameters

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### Proposition 3

As  $\rho \rightarrow 1$ , the semi-elasticity of the population in  $i$  with respect to  $u_j$  is

$$\frac{\partial \log p_i}{\partial v_j} = - \lim_{\rho \rightarrow 1} \frac{m_{i \rightarrow j}}{p_i} \frac{1}{\sqrt{1 - \Sigma_{ij}}} \sqrt{\frac{\pi}{1 - \rho^2}}$$

- If you know migration, distance, and the parameters, sufficient to calculate these elasticities

# Why do we care about Population Elasticities?

## 1. Counterfactuals:

- How much adjustment is there to the China shock? (Caliendo et al., 2019)
- Where will people move in response to global warming? (Cruz and Rossi-Hansberg, 2021)
- Answers from these elasticities:

$$\frac{\partial \log p_i}{\partial v_j} = - \lim_{\rho \rightarrow 1} \frac{m_{i \rightarrow j}}{p_i} \frac{1}{\sqrt{1 - \Sigma_{ij}}} \sqrt{\frac{\pi}{1 - \rho^2}}$$

$$\frac{\partial \log p_i}{\partial v_i} = \lim_{\rho \rightarrow 1} \sum_{j \neq i} \left[ \frac{m_{i \rightarrow j}}{p_i} \frac{1}{\sqrt{1 - \Sigma_{ij}}} \sqrt{\frac{\pi}{1 - \rho^2}} \right]$$

- More gross migration = more elastic population
- Higher migration rate  $i$  to  $j$  = higher cross-elasticity

# Why do we care about Population Elasticities?

## 2. Speed of adjustment

- How fast does the economy react? (Liu et al., 2021)
- Population reacts immediately; short-run and long-run elasticities are the same

# Why do we care about Population Elasticities?

## 3. Welfare:

- To second order:

$$d\mathbb{E}u \approx \underbrace{p \cdot dv}_{\text{Direct effect}} + \underbrace{\frac{1}{2} dv^T \frac{\partial p}{\partial v} dv}_{\text{Migratory insurance}}$$

- High gross migration of shocked places = more insurance
- Higher migration between shocked places = less insurance
- Quantitative analysis in paper: spatial correlation of utility changes 1980-2018 meant there was only 50 percent of the insurance as if the utility changes had been randomly spatially located

## Comparison to the Standard Model



## 2 types of comparison

- Comparison based on simplicity
  - Fewer state variables
  - Naturally hits dynamics
  - Naturally matches short-run migration elasticities
  - Argument for model being more feasible to compute
  - Argument for the truth of the model only from Occam's Razor
- Comparison of implications
  - Misallocation
  - Dynamics
  - Long-run population elasticities
  - Could be used to falsify one model or the other
  - If these were easy to measure, would not need spatial dynamic models

# Conclusion



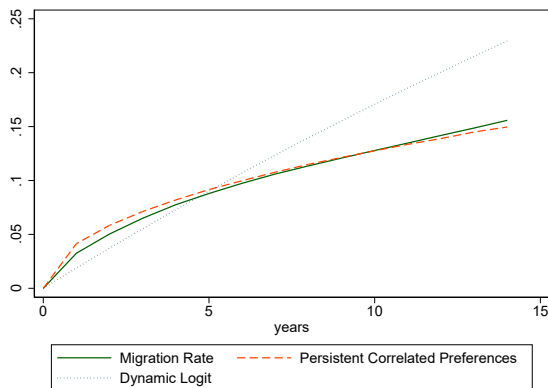
- Persistent preferences help to match dynamic moments of migration *and* gravity
- SPACE model has important implications for counterfactuals and welfare
- SPACE model has several advantages over dynamic logit and different implications



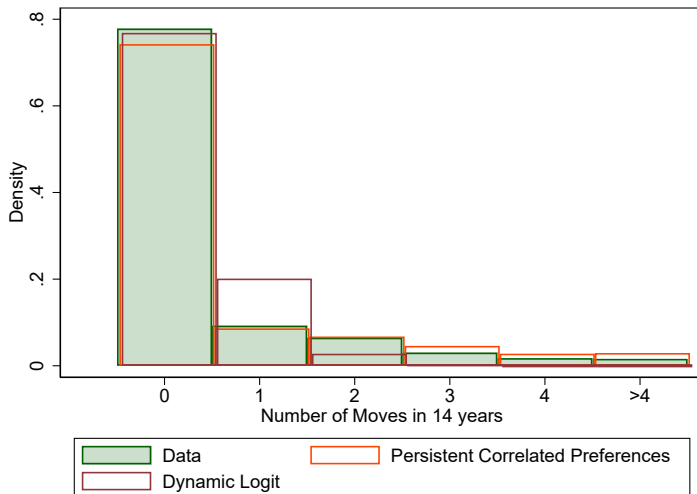
# Square Root Rule, 5-year calibration

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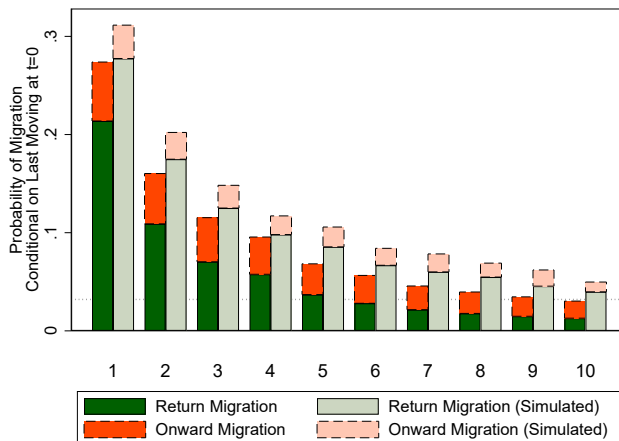


# Frequency of Migration, 5-year calibration

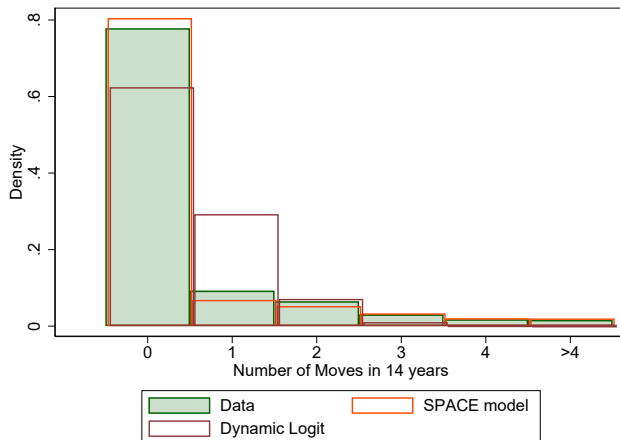


# Return Migration, 5-year calibration

- Conditional probability of moving after previous move

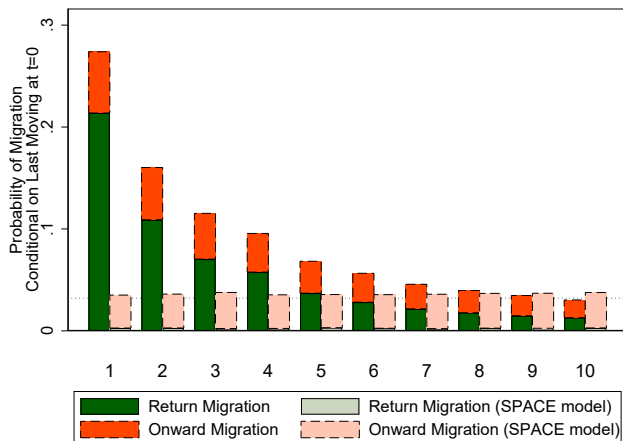


# Frequency of Moves, Dynamic Logit Model

[Return](#)

# Return Migration, Dynamic Logit Model

- Conditional probability of moving after previous move



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